Package paracol:

Yet Another Multi-Column Package to Typeset Columns in Parallel

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PART I

User's Manual

Abstract

This package provides a LATEX environment named paracol in which you may switch and synchronize columns by a command \switchcolumn and by internal environments column, nthcolumn, leftcolumn and rightcolumn.

1 Introduction

This document describes the usage of yet another multi-column package named paracol. The unique feature of the package is that columns are typeset in parallel.

Suppose you are writing a bilingual document whose left column is written in a language, say English, and right column has the translation of the left column in another language, e.g., Japanese. With the paracol package you may write an English part of arbitrarily length and then *switch* to its Japanese counterpart to place both parts side by side. Of course you may return to the English writing similarly.

The column-switching is always allowed when you complete an outermost level paragraph. You may be unaware whether a column is broken into multiple pages before switching because the package automatically goes back and forward to the correct page and vertical position when you switch the column. Moreover, you may synchronize columns so that the tops of the first paragraphs after switching in all columns are vertically aligned. At a synchronization point, you may give a single-column text, for example a common section header, optionally. You may also switch single-column and multi-column in a page arbitrary.

\begin{paracol}{2}[\section{Introduction}]
\hbadness5000

This document describes the usage of yet another multi-column package named \textsf{paracol}. The unique feature of the package is that columns are typeset {\em in parallel.}

Suppose you are writing a bilingual document whose left column is written in a language, say English, and right column has the translation of the left column in another language, e.g. Japanese. With the \textsf{paracol} package you may write an English part of arbitrary length and then {\em switch} to its Japanese counterpart to place both parts side by side. Of course you may return to the English writing similarly.

The column switching is always allowed when you complete an outermost level paragraph. You may be unaware whether a column is broken into multiple pages before switching because the package automatically goes back and forward to the correct page and

This manual itself is an example of two-column documents typeset by paracol. Since the author is not familiar with languages other than English and Japanese and the latter should be hardly understood by most of readers, the right column is the translation of the left English column into a computational language. That is, the right column is the IATEX source code of the left column¹.

vertical position when you switch the column. Moreover, you may {\em synchronize} columns so that the tops of the first paragraphs after switching in all columns are vertically aligned. At a synchronization point, you may give a single-column text, for example a common section header, optionally. You may also switch single-column and multi-column in a page arbitrary.

This manual itself is an example of two-column documents typeset by \textsf{paracol}. Since the author is not familiar with languages other than English and Japanese and the latter should be hardly understood by most of readers, the right column is the translation of the left English column into a computational language. That is, the right column is the \LaTeX{} source code of the left column% \footnote{Not really but its essence is shown.}.

\switchcolumn

 $\begin{verbatim} Here is the source of above. \\ \end{verbatim}^1$

2 Basic Usage

Loading the package is very simple. What you have to do is \usepackage{paracol} in the preamble. Note that paracol can be used with \LaTeX 2 ε and does not work with \LaTeX 2.09.

The fundamental means of parallel-column typesetting are the environment paracol and the command \switchcolumn. The paracol environment needs an argument to specify the number of columns. Thus the following is the basic construct for twoparallel-column documents.

\begin{paracol}{2}
left column text
\switchcolumn

\switchcolumn*[\section{Basic Usage}]
Loading the package is very simple. What
you have to do is |\usepackage{paracol}|
in the preamble. ...²
\switchcolumn

source

\switchcolumn*

The fundamental means of parallel-column typesetting are the environment |paracol| and the command |\switchcolumn|. ... \switchcolumn

source

¹Not really but its essence is shown.

¹This verbatim construct is simply referred as to "source" hereafter.

²Hereafter, a part of the source code may be omitted like this.

right column text
\switchcolumn
left column text
\switchcolumn
right column text
\switchcolumn
\text
\end{paracol}

The \switchcolumn command may have an optional argument to specify the column number (zero origin) to start. That is, \switchcolumn[0] means to switch to the leftmost column, \switchcolumn[1] is to start the second column and so on. Thus the \switchcolumn without the optional argument may be considered as \switchcolumn[$i+1 \mod n$] where i is the ordinal of the column you are leaving from and n is the number of columns given to paracol environment.

\switchcolumn[1]*
source
\switchcolumn[0]
The |\switchcolumn| command may have an
optional argument to specify the column
number (zero origin) to start. ...

3 Column Synchronization

The \switchcolumn command may also be followed by a '*' to synchronize columns. After you switch from a column to another by \switchcolumn* (or \switchcolumn[i]*), all the columns are vertically aligned at the bottom of the deepest one preceding the command. For example, the previous section has three \switchcolumn* commands at which left and right columns are vertically aligned.

The starred version of \switchcolumn may have an optional argument to specify a single-column spanning text whose bottom is the vertical alignment point of columns. For example, \section commands in this manual are given as optional arguments of \switchcolumn* like;

\switchcolumn*[\section{Basic Usage}]
The paracol environment may also start with a spanning text by specifying it as the optional argument of \begin{paracol}. For example, at the beginning of this document, the author put;

\begin{paracol}{2}[\section{Introduction}]

\switchcolumn[0]*[%
 \section{Column Synchronization}
 \label{sec:sync}]
The |\switchcolumn| command may also be followed by a '|*|' to {\em synchronize} columns. ...

The {\em starred} version of |\switchcolumn| may have an optional argument to specify a multi-column text whose bottom is the vertical alignment points of the columns. ... \switchcolumn source

4 Environments for Columns

4.1 Environment column

The \switchcolumn is simple but you may prefer to pack the contents of a column in an environ-

4.1 Environment column

\begin{column*}[%
 \section{Environments for Columns}

ment. The column environment is available for this well-structuralization of LATEX sources for parallel-columned documents. A construct;

\begin{column}
text for a column
\end{column}

is (almost) equivalent to;

\switchcolumn text for a column

The column* environment is also available for the column synchronization and may have an optional argument for spanning text.

4.2 Environment nthcolumn

The \switchcolumn can start an arbitrarily specified column with the column number given through its optional argument, but the column environment cannot do it. If you want to start *i*-th column, you have to do \begin{nthcolumn}{i} (or nthcolumn* with an optional argument to synchronize).

4.3 Environments leftcolumn and rightcolumn

The environments leftcolumn and rightcolumn (and their starred versions with an optional argument) are available as more convenient means than saying \begin{nthcolumn}{0} to switch to the left(most) column and \begin{nthcolumn}{1} to the right (but may not be rightmost) one.

\label{sec:env}]
\subsection{Environment \texttt{column}}
The |\switchcolumn| is simple but you may
prefer to pack the contents of a column in
an environment. ...
\end{column*}
\begin{column}
source
\end{column}

4.2 Environment nthcolumn

\begin{nthcolumn*}{1}
source
\end{nthcolumn*}

\begin{leftcolumn*}

\begin{nthcolumn}{0}
\subsection{Environment \texttt{nthcolumn}}
The |\switchcolumn| can start an
arbitrarily specified column with the
column number given through its optional
argument, but the |column| environment
cannot do it. ...
\end{nthcolumn}

4.3 Environment leftcolumn and rightcolumn

\subsection{%
 Environments \texttt{leftcolumn} and\\
 \texttt{rightcolumn}}
The environments |leftcolumn| and
|rightcolumn| (and their starred versions
with an optional argument) are available as
more convenient means than saying
|\begin{nthcolumn}{0}| to switch to the
left(most) column and ...
\begin{figure*}...\end{figure*}
\begin{figure*}...\end{figure*}
\end{leftcolumn*}
\begin{rightcolumn}
source and a figure env
\end{rightcolumn}

double-column figure #1

Figure 1: A Double-Column Figure

single-column figure #1

Figure 2: A Single-Column Figure

single-column figure #2

Figure 3: Another Single-Column Figure

5 Floats, Footnotes and Counters

5.1 Figures and Tables

As shown in this page, double-column figures/tables (or those spanned multiple columns if you have three or more) may be placed by figure* and table* environments as usual². A single-column figure/table will be placed in the column in which you put figure and table. For example, the body of a figure environment in a leftcolumn environment is always placed in a left column. That is, even if the column of the current page does not have enough room to place the figure, it will not be thrown to the right column but will be placed in the left column of the next page³.

Another caution about float placement is that you have to be careful when you try to put a top-float explicitly with t-option or implicitly without placement option (i.e., tbp in most classes) and to synchronize columns. The rule is as follows; after you synchronize columns in a page, the page cannot have top-floats any more. When you synchronize columns, paracol fixes a virtual horizontal line in the page as the synchronization barrier. Thus no top-floats can-

Table 1: A Single-Column Table

An	example	of
single	column	table

5.1 Figures and Tables

\begin{leftcolumn*}[\section{%
 Floats, Footnotes and Counters}]
\begin{table}[b]
\caption{A Single-Column Table}
\centerline{\begin{tabular}[t]{|1|c|r|}
 \hline
 An&example&of\\hline
 single&column&table\\hline
 \end{tabular}}
\end{tabular}
\end{table}
\subsection{Figures and Tables}
As shown in this page, double-column
figures\slash tables (or those spanned
multiple columns if you have three or more
columns) may be placed by |figure*| and

5.2 Footnotes and Marginal Notes

table* environments as usual 3 .

Footnotes are also put at the bottom of the column in which |\footnote| commands and their references reside (like this\footnote{...}), as shown in page~2 and this page. Marginal notes behave similarly like what you are seeing in the left margin

Table 2: Another Single-Column Table

Another	example
of	single
column	table

²See Section 11 for the appearance order issue of double-column floats.

 $^{^3\}mathrm{Or}$ some farther page if IATEX cannot solve the placement problem wisely.

³Another example of footnote.

not be added above the line⁴. Therefore, the author put two figure environments for the figures shown in this page into the leftcolumn* and rightcolumn environment for the previous section.

5.2 Footnotes and Marginal Notes

Footnotes are also put at the bottom of the column in which \footnote commands and their references reside (like this⁵), as shown in page 6 and this page. Marginal notes behave similarly like what you are seeing in the left margin of this sentence and the right marginal note in this page⁶.

5.3 Local and Global Counters

An

of

example

marginal

note.

You probably found that the numbering of figures and tables is *global* while that of footnotes are *local*. That is, the figure in the right column of the previous page has number 3 following its left-column counterpart Figure 2. The tables in the page are also numbered as 1 and 2 crossing the column boundary. However, the footnotes in each column have their own numbering sequence. Moreover, the footnote numbers in left columns are typeset in roman font while those in right columns have italic shapes. Similarly, subsection numbering is local and the headings in right columns have typewriter-face numbers.

This happens because the author declared the counters figure and table are *global* in the preamble of this document by saying;

\globalcounter{figure}
\globalcounter{table}

and do nothing about footnote and subsection counters. By default, all the counters except for page are local to columns. The value of a local counter of a column is saved somewhere when you leave the column, and it is restored when you revisit the column. The initial values of the local counters are the values they have at \begin{paracol}. After you close the paracol environment, the values of the leftmost

another figure with [t] option
 to fill space

Figure 4: Another Figure with [t] Option

of this sentense\marginpar{\raggedright An example of marginal note.} and the right marginal note in this page\footnote{...}....

Another example of marginal

note.

5.3 Local and Global Counters

You probably found that the numbering of figures and tables is \emph{global} while that of footnotes are \emph{local}...\end{leftcolumn*} \begin{rightcolumn} source. \end{rightcolumn}

a figure with [b] option to fill space

Figure 5: A Figure with [b] Option

⁴Even if you have enough space above, sorry.

 $^{^5{\}rm Unless}$ you specify to make footnotes page-wise as explained in Section 7.6 and 8.

⁶If you have three or more columns, marginal notes of the second or succeeding columns are placed in the right margin in default setting. The paracol package solves the placement problem of marginal notes from two or more columns sharing a side margin by moving some of them down if they conflict over the space with each other.

column are used for the rest of your document until you start new paracol environment. On a restart, local counters in a column have the values they had at the last \end{paracol}, except for those which have been modified outside the environment because the modifications are broadcasted to local counters in all columns. You will see the effect of this interenvironment counter value conservation in the footnote numbers in the right column in page 9 and 13.

This broadcasting of a local counter value can be done explicitly in paracol environments by a command \synccounter{ctr}. This command makes ctr in all columns have the value of that in the column in which the command appears. In addition, another command \syncallcounters performs this broadcasting for all local counters.

If you make a counter global by the command \globalcounter, the save/restore operations are not performed to the counter and thus it is globally incremented by \[ref]stepcounter or commands such as \caption and \section. Note that the value of a global counter depends on the place where it is incremented (or set) in the source code rather than where it appears in the output. Thus if the author put a table environment here to increment table counter, the right-column table at the bottom of page 9 would be Table 3 because its table environment does not appear yet in the source code. Note that, however, though the counter page is global as expected, its numbering is consistent among all columns as far as you refer to the value by \pageref{label} and/or see the values in table of contents, etc.

Another counter which the author made global in this document is section. As explained in Section 3, an optional spanning text of column-switching is considered as in the leftmost column. Since \section commands in this document are always given in spanning texts, so far, it seems unnecessary to make section global because it is incremented correctly in the leftmost column. However, the stepping section has a side effect to reset its descendent counter subsection and referred to from \thesubsection command. Thus if section were local, the rightcolumn subsections in Section 4 would be numbered as "0.1", "0.2" and "0.3" because the local value of section would be zero. Moreover, the right-column subsections of this section would be "0.4", "0.5" and "0.6" because stepping section local to the left column would not reset subsection local to the right column.

a figure with [p] option to fill space

Figure 6: A Figure with [p] Option

another figure with [p] option to fill space

Figure 7: Another Figure with [p] Option

yet another figure with [p]
 option to fill space

Figure 8: Yet Another Figure with [p] Option

fourth figure with [p]
 option to fill space

Figure 9: Forth Figure with [p] Option

You may give a local appearance to a counter ctr for the i-th column (zero origin) by a command;

```
\define the counter \{ctr\}\{i\}\{def\}
```

where def is to be the body of the local definition of thectr. For example, the preamble of this document has the following to give non-default defitions to thefootnote and thesubsection for right columns.

```
\definethecounter{footnote}{1}{%
  \textit{\arabic{footnote}}}
\definethecounter{subsection}{1}{%
  \texttt{%
  \arabic{section}.\arabic{subsection}}}
```

yet another figure with [t]
 option to fill space

Figure 10: Yet Another Figure with [t] Option

6 Closing paracol Environment and Page Flushing

The final example shown here is this single-column text which the author put after the paracol environment above is closed. As you are seeing, a paracol environment can be finished at any vertical position in a page and can be followed by ordinary single column texts.

The environment may also be restarted anywhere you like as shown here.

The last issue is to flush a page. The ordinary \newpage command works as you expect. If you say \newpage in the left column in a page, the contents following it will appear in the left column in the next page. Note that this does not affect the layout of the right column.

To flush all columns in a page, a command \flushpage is available. This command in i-th column is almost equivalent to;

```
\sum_{i=1}^{n} *[\sum_{i=1}^{n} *[
```

but more robust⁷. The ordinary page breaking command \clearpage may also be used to flush all columns and to start a fresh page, but it has a side effect to put all figures and tables which are not yet output.

\begin{paracol}{2}
\begin{leftcolumn}
The environment may also be restarted
anywhere you like as shown here. ...
\end{leftcolumn}
\begin{rightcolumn}
source
\end{rightcolumn}
\end{paracol}
Now the aurthor will do ...

Now the author will do \flushpage shortly to start a real binlingual example from the next page, after showing another example of closing paracol environments in this sentence and of restarting in the next one, in which unbalanced column width is demonstrated using \columnratio command shown in Section 7.3.

O.K., we have restarted paracol environment and we will see the effect of \flushpage now!!

\columnratio{0.6}
\begin{paracol}{2}
\begin{leftcolumn}
0.K., ...
\end{leftcolumn}

\begin{rightcolumn} source

\end{rightcolumn}

⁷For example \switchcolumn* may flush a page for the synchronization and thus \newpage may leave an empty page.

An Die Freude/To Joy Friedrich Schiller

The following is the libretto of the fourth movement of Beethoven's Ninth Symphony, his adaptation of Schiller's ode "An Die Freude" (or "To Joy" in English). Beethoven's additions and revisions are indicated in italics.

O Freunde, nicht diese Töne! Sondern laßt uns angenehmere anstimmen und freudenvollere⁸. Oh friends, no more of these sad tones! Let us rather raise our voices together In more pleasant and joyful tones⁴.

Freude!

Freude, schöner Götterfunken Tochter aus Elysium, Wir betreten feuertrunken, Himmlische, dein Heiligtum! Deine Zauber binden wieder, Was die Mode streng geteilt; Alle Menschen werden Brüder⁹, Wo dein sanfter Flügel weilt

Wem der große Wurf gelungen, eines Freundes Freund zu sein; Wer ein holdes Weib errungen, mische seinen Jubel ein! Ja, wer auch nur eine Seele sein nennt auf dem Erdenrund! Und wer's nie gekonnt, der stehle weinend sich aus diesem Bund!

Freude trinken alle Wesen an den Brüsten der Natur; Alle Guten, alle Bösen folgen ihrer Rosenspur. Küsse gab sie uns und Reben, einen Freund, geprüft im Tod; Wollust ward dem Wurm gegeben, und der Cherub steht vor Gott.

Froh, wie seine Sonnen fliegen durch des Himmels prächt'gen Plan,

Laufet, Brüder, eure Bahn, freudig, wie ein Held zum Siegen.

Joy!
Joy, thou shining spark of God,
Daughter of Elysium,
With fiery rapture, goddess,
We approach thy shrine.
Your magic reunites
That which stern custom has parted;
All humans will become brothers⁵
Under your protective wing.

Let the man who has had the fortune
To be a helper to his friend,
And the man who has won a noble woman,
Join in our chorus of jubilation!
Yes, even if he holds but one soul
As his own in all the world!
But let the man who knows nothing of this
Steal away alone and in sorrow.

All the world's creatures drink
From the breasts of nature;
Both the good and the evil
Follow her trail of roses.
She gave us kisses and wine
And a friend loyal unto death;
She gave the joy of life to the lowliest,
And to the angels who dwell with God.

Joyous, as his suns speed Through the glorious order of Heaven, Hasten, brothers, on your way, Joyful as a hero to victory.

Bettler werden Fürstenbrüder,

 $^{^8\}mathrm{If}$ I had been a good student in my German class, I could find the German translation of the right column footnote 4 is "Dieser Teil wurde van Beethoven hinzugefügt" by myself without the kind help from a user.

⁹Original: Was der Mode Schwert geteilt;

⁴This part was added by Beethoven. ⁵Original: What custom's sword has parted;

Seid umschlungen, Millionen! Diesen Kuß der ganzen Welt! Brüder, über'm Sternenzelt muß ein lieber Vater wohnen.

Be embraced, all ye millions! With a kiss for all the world! Brothers, beyond the stars Surely dwells a loving Father.

Ihr stürzt nieder, Millionen? Ahnest du den Schöpfer, Welt? Such'ihn überm Sternenzelt! Über Sternen muß er wohnen.

Do you kneel before him, oh millions? Do you sense the Creator's presence? Seek him beyond the stars! He must dwell beyond the stars.

7 Reference Manual

7.1 Environment paracol

 $\begin{paracol}{finite} body \ \end{paracol}$

The environment paracol contains body typeset in num columns in parallel. The optional text is put spanning all columns prior to the multi-columned body.

- The environment may start from any vertical position in a page, i.e., not necessary at the top of a page. The single-column pre-environment stuff of the starting page in which \begin{paracol} lies are naturally connected to the beginning part of body in each column, unless the page has footnotes or bottom floats. If these kinds of bottom stuff exist, they are put above the multi-columned body, or the spanning text if provided, with a vertical skip of \textfloatsep separating them if bottom floats exist, or of \belowfootnoteskip described in Section 7.6 if only footnotes exist. The deferred floats which have not yet appeared in the starting page and thus will appear in the next or succeeding pages are considered as page-wise floats given in the environment.
- The environment can be enclosed in a list-like environment such as enumerate, itemize and description. If so, \items in each column are typeset using the parameters of the surrounding environment such as \leftmargin and \rightmargin. For example, the following short paracol environment is included in an itemize for this and other \items in this page.
- This is the first \item in the left column.
- This is the second \item in the left column followed by a \switchcolumn¹¹.
- This is the first \item in the right column.
- This is the second \item in the right column.
- This is the third and last \item in the right column.

You are now seeing the switching to/from multi-columned and itemized texts are naturally connected with the last and this single-columned sentences. You may feel the space between two columns above is too large but it simply results from the large total \leftmargins of the outer description and this itemize, which make the right column shifted right. A simple remedy for this large space is to make \columnsep narrower, for example 0 pt as shown below.

- This \item is wider than the last \item above because \columnsep is 0 pt.
- Therefore, this \item is shifted left a little bit to make inter-column spece narrower.
- All local counters in all columns are initialized to have the values at \begin{paracol} on its first occurrence. On the second and succeeding occurrences of \begin{paracol}, the local counters in each column have the value at the last \end{paracol}, unless they are modified after the \end {paracol}. If a counter is modified (or declared by \newcounter) after the \end{paracol}, the local versions of the counter in all columns commonly have the value at \begin{paracol}.
- The environment may end at any vertical position in a page, i.e., the post-environment stuff being the single-column texts and others following \end{paracol} in the last page of the environment may not start from the top of a page. If any columns don't have deferred column-wise floats and the most advanced leading column at \end{paracol} has neither of footnotes 12 nor bottom floats, its bottom is naturally connected to the post-environment stuff. If the leading column has these kinds of bottom stuff, they are put above the post-environment stuff, with a vertical skip of \textfloatsep

¹⁰With merged footnote layout shown in Section 7.6, the footnotes in the single-column contents are merged with those in paracol environment and are put at the bottom of the starting page together as shown in this page.

¹¹This footnote is to show the footnotes in this page are merged.

¹²With merged footnote layout shown in Section 7.6, the footnotes in the closing paracol environment are merged with those in post-environment stuff and are put at the bottom of the page together as shown in this page.

separating them if bottom floats exist. All deferred column-wise floats given in the environment are flushed before the post-environment stuff appears, possibly creating *float columns* only with floats. On the other hand, deferred page-wise floats given in the environment are considered as deferred (single-) column-wise floats given just after \end{paracol}.

- The values of all local counters in the leftmost column are used as the initial values of them in the post-environment stuff.
- The paracol environment cannot be nested, or you will have an error message of illegal nesting.
- The commands \switchcolumn, \synccounter, \syncallcounters and \flushpage, and environments column(*), nthcolumn(*), leftcolumn(*) and rightcolumn(*) are local to paracol environment and thus undefined outside the environment 13. The command \clearpage is of course usable outside and inside the environment but its function inside is a little bit different from outside.

If a $\ensuremath{\mbox{\mbox{$\setminus$}}}$ has the optional numleft argument to specify the number of leading columns n_l together with the total n given by num, columns in the environment are laid out across two adjacent pages. In this parallel-page typesetting, the first n_l columns are placed in the left page while remaining $n_r = n - n_l$ columns go to the next right page. The pair of left and right pages is considered as comprising a virtual paired page and thus shares a common page number, unless non-paired typesetting is specified by the optional '*' following the optional numleft argument. In the non-paired parallel-paging, when the leading n_l columns are put in a page p, the trailing n_r columns are in the page p+1.

- All page-wise stuff, i.e., pre-environment and post-environment stuff, page-wise floats, spanning text and (merged or non-merged) page-wise footnotes, are placed only in left parallel-pages leaving corresponding regions in right parallel-pages blank¹⁴.
- A non-paired left parallel-page is not necessary to be even-numbered, though the printing tradition requires so if you naturally want to have a parallel-page pair in a double spread. The page number given to the first left parallel-page is simply the number of the page p_1 in which \begin{paracol} reside, and that for the k-th left parallel-page is $p_1 + 2(k-1)^{15}$. Therefore, to make it sure p_1 is even, you might need to have an ordinary page of blank, a title, etc., or to let page counter have an even number by \setcounter, etc., before starting a paracol environment.
- Section 9 shows examples of parallel-paging together with related issues on two-sided typesetting.

7.2 Column-Switching Command and Environments

The command switches columns from i to j where i and j is the zero-origin ordinals of the columns from/to which we are leaving/visiting respectively. Without the optional col, $j = i + 1 \mod n$ where n is the number of columns given to β , while j = col with the optional argument. If the command (or [col] if specified) is followed by a *, the column-switching takes place after synchronization and, if specified, the optional spanning text is put.

• Using \switchcolumn in a list-like environment *included* in a paracol environment causes an ugly result without any error/warning messages. This caution is effectual for all column-switching environments too.

¹³Unless you dare to define them.

¹⁴Someday the author could devise an advanced mechanism to exploit the space in right parallel-pages.

 $^{^{15}\}mathrm{Unless}$ you make some change to page counter.

- If $col \notin [0, n)$, an error is reported and, if you dare to continue, you will switch to the leftmost column 0
- The synchronization point is set just below the last line of the leading column in a page p, partly taking deferred floats into account. That is, all deferred floats are put in the pages up to p-1 and at the top of p if possible. Then, if a non-leading column has footnotes and/or bottom floats and they cannot be pushed down below the synchronization point, the point is moved to the next page top¹⁶.
- In a page having one or more synchronization points, stretch and shrink factors of all vertical spaces, such as those surrounding sectionning commands, are ignored. Therefore, even if you specify \flushbottom, the page is typeset as if \raggedbottom were specified.
- After a synchronization point is set, no top floats will be inserted in the page having the point, thus they will be deferred to the next page or further one.

The environment column contains body for the column next to what we are in just before \begin{column}. The starred version column* does the same after synchronization and, if specified, the optional spanning text is put.

• The environments are almost equivalent to;

```
{\switchcolumn body \par} {\switchcolumn*[text] body \par}
```

except for their first occurrences which don't switch to the column 1 (i.e., right column if two-columned) but stay in the leftmost column 0. More precisely, \begin{column(*)} does not make column-switching if it is not preceded by \switchcolumn nor other column-switching environments.

- The *body* of the environments cannot have \switchcolumn nor column-switching environments including column(*) themselves, or you will have an error message of illegal use of command/environment.
- Column-switching does not take place at \end{column(*)}. Therefore, texts following the environments are put in the column in which body resides until a column-switching command/environment is given.

```
\label{local_local_local} $$ \end{nthcolumn} $$ \end{nthcolumn*} $$ \end{nthcolumn*}
```

The environment nthcolumn contains body for the column col. The starred version nthcolumn* does the same after synchronization and, if specified, the optional spanning text is put.

• The environments are equivalent to;

- The body of the environments cannot have \switchcolumn nor column-switching environments including nthcolumn(*) themselves, or you will have an error message of illegal use of command/environment.
- Column-switching does not take place at \end{nthcolumn(*)}. Therefore, texts following the environments are put in the column in which body resides until a column-switching command/environment is given.

 $^{^{16}\}mathrm{Or}$ below top floats deferred to the page.

```
\label{leftcolumn} body $$ \left\{ \operatorname{leftcolumn} \right\} $$ \left\{ \operatorname{leftcolumn} \right\} $$ body \left\{ \operatorname{l
```

The environment leftcolumn contains body for the leftmost column 0, while rightcolumn for the column 1 being the right column in two-column typesetting. The starred versions leftcolumn* and rightcolumn* do the same after synchronization and, if specified, the optional spanning text is put.

• The environments leftcolumn(*) are equivalent to;

\thecolumn

The command gives you the zero-origin ordinal of the column in which this command appears. Therefore, the following code snip;

gives us the followings.

Column-0. Column-1. Column-2.

• The command is neither a LATEX's counter nor \count register of native TEX, and thus the value it keeps cannot be modified. However, it can be used wherever an integer number is required or appropriate. Therefore for example, \setcounter{mycounter}{\thecolumn} works well to give the column ordinal to the counter mycounter.

$\definecolumn preamble \{col\}\{pream\}$

The command is to define the column preamble *pream* for the column *col*, which is inserted at every column-switching to the column. More specifically, the command let \switchcolumn to *col* act as if you sepcify;

```
\switchcolumn \langle pream for col \rangle
```

and column-switching environments such as nthcolumn act as if you specify;

```
\begin{nthcolumn} \{col\} \ \langle pream \ for \ col \rangle
```

- The optional spanning text of \switchcolumn, column-switching environments and \begin{paracol} is considered to be in a virtual column −1, and thus if you need a preamble for spanning texts do \definecolumnpreamble{-1}{pream}.
- The command may appear in a paracol environment and, if so, *pream* is effective from the succeeding column-switching to *col*.
- The definition of *pream* is made globally.

$\ensuremath{\mbox{\mbox{ensurevspace}}}\{len\}$

The command tells the first synchronizing column-switching command (i.e., \switchcolumn[col]*) or environment (i.e., column*, etc.) following this command that the page must be broken before synchronization unless the synchronization point has the space of len or more below it in the page. If a synchronization does not have the command after the previous synchronization, it is assumed that \ensurevspace{\baselineskip} is given.

- This command is to be used when a synchronization point would be placed near the bottom of a page p and the space below it is not sufficient for a column c to put anything in the page, while another column c' can have a few lines in the page. If this happens, the first line after the synchronization should start at the top of the page p+1 in the column c, while that of c' is still in the page p, giving you an impression that the synchronization fails to align the top of all columns below it. The fact is, however, the synchronization point is properly established near at the bottom of the page but the first line of c needs some large space due to, for example, the followings.
 - The line has unusually tall stuff including larger font letters.
 - The line has a footnote reference which is hardly apart from the footnote, and thus the line and the footnote go to the next page together.
 - The parameter \clubpenalty is too large (e.g., 10000) to break the first and second lines into separate pages.
 - The first line follows a vertical space.
- This manual itself has some instances of \ensurevspace command in the page 13 and 14 in which each German stanza is enclosed in verse and then leftcolumn* environments and has \ensurevspace{2\baselineskip} before the \begining of the outer leftcolumn* because the first line of the stanza is preceded by a vertical space inserted by \begin{verse}. In fact without \ensurevspace, the first two lines of the sixth English stanza would be in the page 13, while corresponding German stanza go to the next page 14 as a whole, due to the difference of the height of footnotes in each column, i.e., German ones are taller than English ones to narrow the space for the German column.
- As the author does in the "An die Freude/To Joy" example, it is a good tactics to have an \ensurevspace with some vertical space larger than the default \baselineskip if it is sure that a column has a feature shown above regardless of the position of the synchronization point in question, because the point goes up or down with revisions of your document and using an \ensurevspace for a synchronization far above the page bottom is perfectly harmless. Similarly, if you find a problem in a synchronization and add an \ensurevspace to solve it, keeping the command attached is recommended even when the synchronization point moves up or down to make the command unnecessary.

7.3 Commands for Column and Gap Width

\columnratio
$$\{r_0, r_1, \cdots, r_k\} [r'_0, r'_1, \cdots, r'_{k'}]$$

The command defines the width of each column by the fraction r_i to specify the portion which i-th (i = 0 for the leftmost) column occupies. More specifically, the width w_i of the i-th column is defined as follows, where W is \textwidth, S is \columnsep, and n is the number of columns given to \begin{paracol}}.

$$W' = W - (n-1)S$$

$$w_i = \begin{cases} r_i W' & i \le k \\ \frac{(1 - \sum_{j=0}^k r_j)W'}{n - (k+1)} & i > k \end{cases}$$

For a paracol environment with parallel-paging, n is replaced with n_l for the columns in left parallel-pages, while n and w_i are replaced with n_r and w_{n_r+i} for those in right parallel-pages. Moreover, if the optional argument having $r'_0, r'_1, \dots, r'_{k'}$ is provided, w_{n_r+i} for a column in right parallel-pages is determined by r'_i and k' instead of r_i and k.

- The equations above imply that k < n-1, $r_i > 0$ and $\sum_{j=0}^k r_j < 1$. If $k \ge n-1$, k is assumed to be n-2 and all r_i such that $i \ge n-1$ are ignored. If r_i or its sum does not satisfy the conditions, you will have an ugly result with "Overfull" messages.
- The argument r_0, r_1, \dots, r_k can be empty to mean k = -1 to let all column widths be W'/n as default.
- The setting of column width by the command takes effect in the paracol environments following the command¹⁷. Therefore, though placing the command in the preamble is the most natural way¹⁸, you may place this command between two paracol environments to change the column layout for the second one even when they appear in a page as shown in Section 6.
- In the *i*-th column, \columnwidth has w_i and, for outermost paragraphs in the column, \hsize has w_i as well. As for \linewidth, it has w_i (\textwidth l) where l is what \linewidth had at \begin{paracol}, i.e., the \linewidth for the list-like environment surrounding paracol if any, or \textwidth otherwise.
- You can specify width of each column and that of each *gap* between two columns more detailedly by \setcolumnwidth shown below. If your document has both of \columnratio and \setcolumnwidth prior to a paracol environment, the command given later is effective for the environment.

$\strut \{s_0, s_1, \cdots, s_k\} [s'_0, s'_1, \cdots, s'_{k'}]$

The command defines the width of each column and that of each gap between two columns by the column/gap specification s_i for the i-th column and the gap between it and the (i+1)-th column. More specifically, s_i has the form of \hat{w}_i or \hat{w}_i / \hat{g}_i where each of \hat{w}_i and \hat{g}_i is a proper glue including a proper dimension, or an empty string to mean $\hat{w}_i = \text{fill}$ and $\hat{g}_i = \text{columnsep}$, to determine the width of i-th column w_i and that of i-th gap g_i as follows, where nat(x) is the natural width of the glue x, str(x) is the infinite stretch factor of x, W is textwidth, and n is the number of columns given to $\text{legin}\{paracol}\}$.

$$\begin{split} W' &= \sum_{i=0}^{n-2} \left(nat(\hat{w}_i) + nat(\hat{g}_i) \right) + nat(\hat{w}_{n-1}) \\ F &= \sum_{i=0}^{n-2} \left(str(\hat{g}_i) + str(\hat{g}_i) \right) + str(\hat{w}_{n-1}) \\ x_i &= \begin{cases} (W/W')nat(\hat{x}_i) & W' \geq W \ \lor \ F \leq 0 \\ nat(\hat{x}_i) + (str(\hat{x}_i)/F)(W - W') & W' < W \ \land \ F > 0 \end{cases} & (x \in \{w, g\}) \end{split}$$

That is, if the total of natural widths W' is larger than $\texttt{textwidth}\ W$ or there are no infinite stretch factors in the specification, given widths are scaled down or up so that the scaled total is equal to W. Otherwise, each width with an infinite stretch factor is extended according to its ratio in the total stretch so that the stretched total is equal to W.

For a paracol environment with parallel-paging, n is replaced with n_l for the columns in left parallel-pages, while n, w_i and g_i are replaced with n_r , w_{n_r+i} and g_{n_r+i} for those in right parallel-pages. Moreover, if the optional argument having $s'_0, s'_1, \dots, s'_{k'}$ is provided, w_{n_r+i} and g_{n_r+i} for a column in right parallel-pages are determined by s'_i instead of s_i .

¹⁷If the command is in a paracol environment, the command does not affect the column widths of the environment but does the next ones, though such usage is very unusual.

¹⁸Or second most to not using it at all, of course.

- In paracol environments having n columns, s_i s.t. $i \ge n$ and \hat{g}_{n-1} are ignored. On the other hand if k < n-1, it is assumed s_i is an empty string for all i > k.
- Finite stretch factors and finite or infinite shrink factors in \hat{w}_i and \hat{g}_i are ignored.
- Unlike T_EX 's genuine glue addition, all infinite unit fil, fill and fill1 are not distinguished in the summation for F. Also unlike T_EX 's genuine scaling of a glue primitive, $f \in F$ means $f \in F$ fill for convenience $f \in F$.
- The division W/W' and $str(\hat{x}_i)/F$ can have some arithmetic errors and thus the total of w_i and g_i may not be equal to W exactly but can be a little bit less than W. This small error is, however, equally distributed to g_i in typesetting of a page to make the total width of columns and gaps is exactly W^{20} .
- All the specifications shown in the table below give us same results for a paracol environment having three columns, providing $\text{textwidth} = 360 \, \text{pt}$ and $\text{columnsep} = S = 20 \, \text{pt}$.

s_0,s_1,s_2	w_0	g_0	w_1	g_1	w_2 (in pt)
50pt/20pt,100pt/40pt,150pt	50	20	100	40	150
50pt,100pt/2\columnsep,150pt	50	S	100	2S	150
50pt/\fill,100pt/2\fill,150pt	50	$(1/3) \cdot 60$	100	$(2/3) \cdot 60$	150
,2\fil1/2\columnsep,3\fill	$(1/6) \cdot 300$	S	$(2/6) \cdot 300$	2S	$(3/6) \cdot 300$
50pt/20,50pt plus 1fil/40pt,50pt plus 2fil	50	20	$50 + (1/3) \cdot 150$	40	$50 + (2/3) \cdot 150$
5pt/2pt,10pt/4pt,15pt	$10 \cdot 5$	$10 \cdot 2$	$10 \cdot 10$	$10 \cdot 4$	$10 \cdot 15$
100pt/40pt,200pt/80pt,300pt	$0.5 \cdot 100$	$0.5 \cdot 40$	$0.5 \cdot 200$	$0.5 \cdot 80$	$0.5 \cdot 300$

• If your document has both of \columnratio and \setcolumnwidth prior to a paracol environment, the command given later is effective for the environment.

7.4 Commands for Two-Sided Typesetting and Marginal Note Placement

 $\t two sided [t_1t_2\cdots t_k]$

The command enables a set of two-sided typesetting features $\{t_i | t_i \in \{p, c, m, b\}, 1 \le i \le k\}$ explicitly by the optional argument, or all of the following four features as a whole without the argument, in even-numbered pages.

- p(age) for ordinary two-sided paging, letting the left side margin be \evensidemargin, page headers be different from those in odd-numbered pages with headings or myheadings page style, and \cleardoublepage leave an even-numbered page blank if it is used in an odd-numbered page.
- c(olumn) for column-swapping to print columns in even-numbered pages in reverse order. This feature is sometimes preferable in typesetting especially with unbalanced parallel columns to make, for example, a wider columns are always inside while narrower ones are outside.
- m(arginal text) to place marginal notes in the side margin opposite to that specified by the command \marginparthreshold discussed shortly.
- b(ackground painting) to make background painting, shown in Section 7.8, mirrored so that, for example, a color specified for the left margin is used to paint the right margin instead.
 - The feature p is also enabled by the twoside option of \documentclass with almost all classes including article, book, report, etc. Though it is strongly recommended to make both settings by \documentclass and this command consistent, they can be inconsistent resulting in lack of

¹⁹In T_EX's grammar, f\fill means a dimension rather than a glue and is 0 pt because the natural component of \fill is 0. ²⁰If we may ignore the arithmetic error inherent in T_EX.

some expected functions. For example, enabling p feature by \twosided without twoside option in \documentclass makes the format of headers and footers in all pages same even with \pagestyle{headings}.

- \bullet The column-swapping enabled by the feature c is ineffective in non-paired parallel-paging because it is meaningless²¹, and thus silently ignored.
- In ordinary single-column typesetting, marginal note swapping in even-numbered pages is enabled by the twoside option, while it never takes place in ordinary two-column typesetting. For marginal notes given in paracol environments, however, swapping of them in even-numbered pages is enabled by giving the feature m to \twosided.
- The command has to be outside of paracol environments to decide the action in the environments following them. If it appears in a paracol environment, you will have a warning message saying it is ignored.
- This narrower, outside and italicized column-1 is at first in right side but the page break has changed the position to the left.
- Here is an example of column swapping. Since this page 22 is odd, this wider column-0 with roman font is placed in left side and thus inside at the begining, but now we are in an even page in which this column is in right side.
- In old versions of paracol, namely 1.2 and its minor revisions 1.2x, column-swapping was controlled by lengthy commmands \swapcolumninevenpages and \noswapcolumninevenpages. Though they are still available and will be so forever for backward compatibility, it is recommended to use \twosided with or without the feature c. The old versions also have a problem that spanning stuff crossing a page boundary is placed incorrectly after the page break in it, but this problem is solved by a fix incorporated in version 1.3.
- It must be $t_i \in \{p, c, m, b\}$, or you will have an error message of illegal two-siding feature.
- Section 9 shows examples of two-sided typesetting together with related issues on parallel-paging.

$\verb|\marginparthreshold{|}\{k\}[k']$

The command specifies the minimum ordinal k of columns whose marginal notes are placed in right margin. That is, marginal notes given in a column-i go to left margin if i < k, while they go to right if $i \ge k$. The optional argument k', if given, is for columns in right parallel-pages to decide the margin where their marginal notes are placed. In default, k = 1 is assumed to let marginal notes from the leftmost column-0 go to left margin while those from other columns go to right.

- You may specify k = 0 to let all marginal notes go to right margin, or may give the command a large number, say 100, to place all of them in left margin.
- The setting k=0 or k=100 above makes a side margin shared by marginal notes from different columns, and sharing is inevitable when a (parallel-) page has three or more columns. When a margin is shared by marginal notes from two or more columns, it can happen that two marginal notes from different columns conflict over the space to be occupied by each of them. This conflict is solved by paracol to push down the note given later in your source .tex until an available space for it is found. Note that the marginal note to be pushed down is determined by the position in the source rather than that in the printed result. Also note that paracol exploits space between two marginal notes having been already placed in the placement of other note coming later to place it at the natural position if possible or to minimize the amount of pushing down otherwise.
- In the decision of the real margin in which a marginal note is placed, other two factors are involved; m feature of \twosided command and the parity of the page; and LATEX's genuine command \reversemarginpar. More specifically, after the first preliminary decision is made according to

²¹Unless somebody tells the author it is meaningful.

the threshold given to \marginparthreshold, we have the following two steps to modify the decision; if m feature has been specified in \twosided command and the marginal note belongs to an even-numbered page, the decision is reversed to have the second preliminary result; and then if \reversemarginpar has been specified, the second result is reversed (again) to have the final result.

- In old versions of paracol, namely older than 1.3, marginal note placement was not only uncontrollable but also gave ugly results when your document has three or more columns because the marginal notes from a column not being leftmost or rightmost were placed in the gap following the column rather than a margin. This miserable *gap note* placement does not happen any more, or in other words this is no more available because the author believes nobody loves it.
- Section 9 shows examples of marginal note placement together with related issues on parallel-paging and two-sided typesetting.

$\mbox{\mbox{\tt marginnote}} [left] \{right\} [voffset]$

You may use the package marginnote and its command \marginnote in paracol environments as a replacement of \marginpar. However, the command is *emulated* with \marginpar and paracol's own mechanism of marginal note placement. Therefore, some of marginnote's functionality are not effective in paracol environment except for the following features.

- Shifting up/down a marginal note by the optional voffset.
- Defining fonts (and others) for marginal notes by \marginfont.
- Controlling the holizontal paragraph alignment by \raggedleftmarginnote and \raggedright marginnote.

Note that you will see a warning message "\margninnote is emulated by \marginpar" at the first inparacol occurrence of the command to let you know the imperfection.

7.5 Commands for Counters

\globalcounter{ctr} \globalcounter*

The command $\globalcounter\{ctr\}\$ declares that the counter ctr is global to all columns, while $\globalcounter*$ does so for all counters. An update of a global counter in a column is seen by any other columns.

- All column-local values of a descendant local counter of a global counter are zero-cleared when the global counter is explicitly stepped by \stepcounter or \refstepcounter, or implicitly by a sectioning command and so on.
- The counter page is always global but an explicit update of it by e.g., \setcounter in a non-leftmost column is not seen by other columns and is canceled even for the column itself after a column-switching or a page break in the column. Therefore, if you want to make a jump of page, it must be done in the leftmost column 0. Note that a jump from a page p to q can be seen in other columns even if they have gone beyond p before the column 0 makes the jump, as far as page having q (or its successor) is referred to by \pageref or through contents files such as .toc²².
- All counters except for page are local by default. This feature may cause a problem with some packages including marginnote and (auto-)pst-pdf having their own counters which must be global. Since it is tough to find the name of such counters from package sources, if you have something wrong with these (or other) packages, try to put \globalcounter* in your preamble and use \localcounter shown below to localize specific counters which you need to be local.

 $^{^{22}\}mathrm{Direct}$ reference to page may give an inconsistent result, as you might have in ordinary IATEX documents.

• Globalizing a ctr being already global is just ignored without any complaints.

\localcounter{ctr}

The command declares that the counter ctr is local for each column.

• Though this command is intended for localizing a *ctr* which is once globalized, localizing a local counter does not causes any error but is just ignored. Localizing the permanently global page is also just ignored without any complaints.

$\define the counter \{ctr\}\{col\}\{rep\}$

The command defines the ctr being $\{rep\}$ for the local use in the column col. That is, the ctr in the column col acts as if it is defined by rep.

\synccounter{ctr}

The command broadcasts the value of the local counter ctr in the column in which the command appears to the values in all other columns.

\syncallcounters

The command broadcasts the values of all local counters in the column in which the command appears to the values in all other columns.

7.6 Page-Wise Footnotes

\footnotelayout{layout}

The command specifies the $layout \in \{c, p, m\}$ of footnotes in paracol environments as follows.

- c(olumn) makes footnotes column-wise (aka multi-columned) being default to place footnotes in each column at the bottom of the column and separating them from pre-environment and post-environment footnotes.
- p(age) makes footnotes page-wise (aka single-columned) so that footnotes in all columns are gathered, typeset spanning all columns, and placed at the bottom of the page in which they appear or at the end of the paracol environment they belong to, so that they are separated from pre-environment and post-environment footnotes.
- m(erge) makes page-wise footnotes merged with footnotes in outside of the environment but in the same page, i.e., those in pre-environment and post-environment stuff.
 - An example of merged footnote is found in p. 15 while you will see many of them in Section 8²³.
 - In any layouts, a footnote cannot have page breaks in it, i.e., a footnote is always put in a page as a whole. This makes it impossible to have a footnote taller than \textheight and thus you will see a warning message if you give a very long footnote which will be printed intruding into the area for page footer (or out of the paper bound).
 - Choosing the layout page-wise or merged makes footnote counter global and \fincounteradjustment shown below performed inside \footnotelayout. Choosing column-wise let the command do the operations oppositely, i.e., localizes footnote and does \nofncounteradjustment. Though these settings are usually appropriate for each footnote layout but you can override them by explicitly using commands like \localcounter{footnote}.

²³The left-column footnote 6 in p. 12 looks like a merged footnote because it is at the bottom of the page and the marked text is above the single-column text. However, it is an ordinary column-wise one produced by a trick with \footnotemark and \footnotetext in different paracol environments.

- The command has to be outside of paracol environments to decide the action in the environments following them. If it appears in a paracol environment, you will have a warning message saying it is ignored.
- In old versions of paracol, namely 1.2 and its minor revisions 1.2x, footnote layout was controlled by a set of lengthy commands \multicolumnfootnotes for c, \singlecolumnfootnotes for p, and \mergedfootnotes for m. Though they are still available and will be so forever for backward compatibility, it is recommended to use \footnotelayout²⁴.
- It must be $layout \in \{c, p, m\}$, or you will have an error message of illegal layout specifier.

\footnote*[num]{text} \footnotemark*[num] \footnotetext*[num]{text}

The starred version of \footnote, \footnotemark and \footnotetext are for the adjustment of the footnote numbering, the order of footnote marks in main texts, and the stacking order of footnotes at page bottom. Their usages with various examples are given in Section 8.

\fncounteradjustment \nofncounteradjustment

The maintenance of footnote with the starred footnote commands such as \footnote* shown above causes out-of-order progress of the counter to make it hard to have a consistent counter value at \end{paracol}. The command \fincounteradjustment is to let \end{paracol} adjust the value of the counter based on its value at \begin{paracol} and the number of footnote commands in the environment. The command \nofncounteradjustment is to tell \end{paracol} to do nothing as in default.

- Though \footnotelayout with p(age-wise) or m(erged) argument does \fracounteradjustment while that with c(olumn) does \nofncounteradjustment inside of it, you can override these settings by explicitly putting a counter adjustment command after \footnotelayout.
- The effect of \fincounteradjustment is shown in Section 8.

\belowfootnoteskip

The typesetting parameter specifies the amount of the space inserted below footnotes of single-column pre-environment stuff if it does not have bottom floats. The default amount is 0 pt, i.e., no space is added.

7.7 Commands for Coloring Texts and Column-Separating Rules

 $\label{local_color} $$ \columncolor[mode]{color}[col] $$ \normalcolumncolor[col] $$$

The command \columncolor declares that the default color of a column is color or what it specifies by the combination with the optional mode. The command \normalcolumncolor declares the default color is what \normalcolor specifies, i.e., black usually. The target column of these commands is that in which the commands reside, or col if it specified.

- The command may be outside of paracol environment. If so and *col* is not provided, the target column is the leftmost 0.
- The default color declaration is *global*. Therefore, even if the command appears in a paracol environment (and even in some grouping structure in it), the declaration will be kept effective after \end{paracol} to determine the default color of the specified column in succeeding paracol environments.

²⁴Not only for type saving but also for being familiar with this command which could have some advanced feature, for example to put gathered footnotes into a specific column, someday.

- To give a color to texts (and maybe other stuff) in a column correctly, you need to load color package or its relative (e.g., xcolor) which the implementation of coloring in paracol relies on.
- Coloring with \color[mode]{color} and other coloring commands in paracol environments is of course allowed. One caution is that the \color decides the color for following texts until other specification is given or the group surrounding the command is closed. Therefore, \switchcolumn does not affect the coloring but a color given to the texts in a column is also applied to the texts in the column to be switched to. This irrelativeness of coloring and column-switching is shown in the example below.

This column is colored blue because \columncolor{blue}

is specifed. Here we have a \switchcolumn.

The color of this paragraph is green because we are still in the environment of green coloring, which we are now closing.

Since the coloring environment has been closed, the color of this paragraph is the default blue. Now we have yet another and the last \switchcolumn to the right.

This column is colored red because \columncolor{red} is specified.

Now the color of the right column is changed to green because

\begin{color}{green}

is given prior to this paragraph. Now we have another \switchcolumn to go back to the left.

Since this paragraph is outside of the coloring environment, its color is the default red.

The default coloring of columns does not affect anything outside of paracol environment of course, and thus this sentence is not colored²⁵.

\coloredwordhyphenated \nocoloredwordhyphenated

The command \coloredwordhyphenated allows the first word following a coloring command such as \color to be hyphenated, but at the same time make it possible that a line is broken before the word. The command \nocoloredwordhyphenated acts oppositely and thus line breaking before the first word and hyphenating it are inhibited. By default, \coloredwordhyphenated is effective.

• The implementation of color package and its relatives makes it impossible that word is hyphenated when it appears like {\color{red}word ...} or \textcolor{word ...}. This inhibition of the hyphenation is sometimes annoying especially when the document is multi-columned and thus a line is narrow and a column is written in a language having long words such as German. Therefore in paracol package, a trick is used to allow the word is hyphenated. However this trick being insertion of a null horizontal space has a side effect that the word can have a line break before it. Though this line break is usually unharmful, in a special occasion the break is undesirable and inappropriate by making it possible that the half-colored word 'inappropriate' is broken between 'in' and 'appropriate' without hyphenation. Therefore, if you find such a inappropriate break, use \nocoloredwordhyphenated as follows, for example.

{\nocoloredwordhyphenated in\textcolor{red}{appropriate}}

 $\label{localization} $$ \colseprulecolor[mode] {color}[col] $$ \normalcolseprulecolor[col] $$$

The command \colseprulecolor declares the color for *column-separating rules*, being the vertical rules drawn at the center of gaps between columns, is *color* or what it specifies by the combination with the optional *mode*. The command \normalcolseprulecolor declares the color of rules is what \normalcolor specifies, i.e., black usually. If the optional argument *col* is given, these commands specifies the color of the rule in the gap following the column whose ordinal is *col*, rather than all rules.

²⁵Or colored black as \normalcolor specifies.

• The rules are drawn if IATEX's typesetting parameter \columnseprule for the rule width has non-zero value, e.g., 0.4pt to obey the standard rule thickness. The rules are not drawn on page-wise stuff, i.e., pre-environment and post-environment stuff, page-wise floats or (merged or non-merged) page-wise footnotes of course but also spanning texts. Therefore, if a page has spanning texts, the rules are broken by them as shown in the red rule example below.

This is a left column paragraph preceding a spanning text. Of cource the rule separating this and the next column starts from the top of this paragraph.

This is a right column paragraph preceding a spanning text given by the \switchcolumn* at its end.

An Example of Spanning Text Given by \subsubsection* Command

Since we have a spanning text above, the red rule separating this and the next column is broken by the text. It is also natural that the rule separating this and the previous column is terminated at the end of this paracol environment.

- To give a color to rules correctly, you need to load color package or its relative (e.g., xcolor) which the implementation of coloring in paracol relies on.
- Once you give a color to rules in a specific gap with the optional *col*, another \colseprulecolor or \normalcolseprulecolor without *col* does *not* change the color of the rule in the gap.

7.8 Commands for Background Painting

```
\label{lem:color} $$ \ \color{region}[mode]{color} $$ \ \color{region}(x_0,y_0)}[mode]{color} $$ \ \color{region}(x_0,y_0)(x_1,y_1)}[mode]{color} $$
```

The command declares that *background painting* of *region* is performed with *color* or what it specifies by the combination of the optional *mode*. The *region* whose background is painted is one of the following.

c(olumn) for all columns, or particular one if region is c[col] to specify its ordinal col.

g(ap) for all gaps between columns, or particular one if region is g[col] to specify the ordinal col of the column preceding the gap.

s(panning) for spanning texts.

f(loat) for page-wise floats.

n(ote) for (merged or non-merged) page-wise footnotes.

p(re/post) for pre-environment and post-environment stuff.

t(op) for top margin.

b(ottom) for bottom margin.

1(eft) for left margin.

 $\mathbf{r}(ight)$ for right margin.

In addition, capitals of the keys above, i.e., C, G, \ldots, L , are also legitimate for *under painting*. For example, you may specify to paint the background of a region, say top margin, by two **backgroundcolor** with t and T and with different color arranging the size of the region of either t or T (or both of them) by the *extension* option shown below.

The optional (x_0, y_0) is to enlarge the region to be painted shifting its left-top and right-bottom corner outside by the dimension x_0 horizontally and y_0 vertically, or to shrink it with negative dimensions. This extension can be asymmetric giving another optional (x_1, y_1) so that it acts on the right-bottom corner while let (x_0, y_0) shift only the left-top corner. Moreover, you may make each extension infinite by giving $10000\,\mathrm{pt}$ (about $3.5\,\mathrm{m}$) to x_0, y_0, x_1 and/or y_1 so that the corresponding region edge is shifted to the paper edge. Furthermore, this infinite extension can be terminated at the point α inside the corresponding paper edge by giving $10000\,\mathrm{pt} - \alpha$ ($\alpha \leq 1000\,\mathrm{pt}$) to an extension parameter x_0 , etc.

- A region whose color is not specified is not painted and thus left blank (or kept as painted by \pagecolor if you specify it).
- Under-painting of columns and gaps by C and G is made for regions different from those over-painting c and g. That is, under-painting is done ignoring all page-wise stuff and thus the height of the regions is always \textheight + \maxdepth. On the other hand, over-painting is only for chunks shrunk or separated by page-wise stuff.
- You may exploit the following painting order, where x_i is the *i*-th spanning text $(x \in \{s, S\})$ or *i*-th chunk followed by the *i*-th spanning text, m and n is the number of spanning texts and columns in a page respectively, to overlay a preceding region with a succeeding region, if your *printer* allows overlaid color painting.

$$\begin{split} \mathbf{T} &\to \mathbf{B} \to \mathbf{L} \to \mathbf{R} \to \mathbf{G} [0] \to \cdots \to \mathbf{G} [n-1] \to \mathbf{C} [0] \to \cdots \to \mathbf{C} [n-1] \\ &\to \mathbf{t} \to \mathbf{b} \to \mathbf{1} \to \mathbf{r} \to \mathbf{N} \to \mathbf{n} \to \{\mathbf{F}, \mathbf{P}\} \to \{\mathbf{f}, \mathbf{p}\} \to \mathbf{S}_1 \to \cdots \to \mathbf{S}_m \\ &\to \mathbf{g}_1 [0] \to \cdots \mathbf{g}_1 [n-2] \to \mathbf{c}_1 [0] \to \cdots \mathbf{c}_1 [n-1] \to \mathbf{s}_1 \\ &\to \cdots \\ &\to \mathbf{g}_m [0] \to \cdots \mathbf{g}_m [n-2] \to \mathbf{c}_m [0] \to \cdots \mathbf{c}_m [n-1] \to \mathbf{s}_m \\ &\to \mathbf{g}_{m+1} [0] \to \cdots \mathbf{g}_{m+1} [n-2] \to \mathbf{c}_{m+1} [0] \to \cdots \mathbf{c}_m [n-1] \end{split}$$

- If you specify b feature by \twosided, background painting is mirrored in even-numbered pages so that 1 and L mean right margin, r and R mean left margin, and asymmetric extensions are applied to right-top and left-bottom corners.
- To give a color for background painting correctly, you need to load color package or its relative (e.g., xcolor) which the implementation of coloring in paracol relies on.
- To paint margins and regions having infinite extension correctly, the parameters \paperwidth and \paperheight should be set properly by, for example, a paper selection option of \documentclass.
- Section 10 shows examples of background painting to give you more intutive explanations of \backgroundcolor and its region specifications.

\nobackgroundcolor{region} \resetbackgroundcolor

The command \nobackgroundcolor declares that the background of region is not painted, where region is one of legitimate region specifiers of \backgroundcolor. The command \resetbackgroundcolor declares no regions are painted and thus gives you the default state.

• If you specified the background painting of c[col] or g[col] by \backgroundcolor, the painting is not canceled by \nobackgroundcolor with c or g but without [col]. Similarly, once you made declarations of background painting of both c and c[col] (resp. g and g[col]), \nobackgroundcolor with c[col] (resp. g[col]) cancels the painting of c[col] (resp. g[col]) but the region will still be painted by the color you gave to c (resp. g).

\pagerim

This is a (kind of) $length\ command^{26}$ to have the width of the rim area placed at each paper edge to inhibit background painting in the area. That is, the inner edges of the area are considered as virtual paper edges to block painting of all margins and regions having infinite extension to the edges, for example in order to avoid printing troubles caused by painting the rim area too close to the real paper edges. The default value of $\partial paper edges$ in a paper.

7.9 Control of Contents Output

$\addcontentsonly{file}{col}$

The command inhibits the output of contents information to $file \in \{toc, lof, lot\}$ from columns other than col.

- For example, this manual has \addcontentsonly{toc}{0} to inhibit the contents information output from \subsection commands in the right column in Section 4 and 5, or the table should have duplicated entries of sub-sections.
- It must be $file \in \{toc, lof, lot\}$, or you will have an error message of illegal type of contents file.

7.10 Page Flushing Commands

\flushpage

The command flushes pages up to the *top page* in which the leading column resides. Deferred floats which can be put in the pages up to the top page are also flushed.

\clearpage

The command does what \flushpage does and then flushes all floats still deferred if any. The deferred float flushing beyond the top page takes place at first for column-wise ones creating float columns for them, and then for page-wise ones creating float pages only with page-wise floats, as LATEX's \clearpage does outside paracol environment.

\cleardoublepage

The command does what LATEX's \cleardoublepage does outside paracol. That is, it does \clearpage always and then leaves a blank page if it is even-numbered and two-sided p(age) feature is enabled by twoside option of \documentclass or paracol's own \twosided command shown in Section 7.4.

• This command is equivalent to \clearpage in paracol environments for non-paired parallel-paging because \clearpage flushes both left and right parallel-pages.

²⁶In reality, it is a \dimen register rather than a \skip register.

8 Numbering and Placement of Page-Wise Footnotes

Here we have a simple example of page-wise but not-merged footnotes²⁷.

First left-column paragraph in it.	First right-column paragraph in it
Second left-column paragraph in it.	Second right-column paragraphin it
²⁸ First left-column footnote. ²⁹ Second left-column footnote. ³⁰ First right-column footnote. ³¹ Second right-column footnote. This and all other footnotes at they are put above the post-environment stuff.	pove are page-wise and, since footnote typesetting is non-merged

As shown above, it is easy to have a reasonable result of footnote numbering and placement as far as your paracol environment is completely included in a page and you accept the numbering in left-column-first manner constructing the environment as follows exploiting the fact footnote is made global, where b is the value of footnote counter at ϵ , i.e., the number given to the footnote just preceding the environment, and thus b = 27 in the example above.

The real life is, however, tougher than that, because the assumptions above are too optimistic as described in the following subsections.

8.1 Multiple \switchcolumn in a Page

Here we have an example with three \switchcolumn commands in a page having six footnotes. Hereafter, footnotes are typeset with $footnotelayout\{m\}^{32}$.

First left-column paragraph in it.	First right-column paragraph with a footnote ³⁵ in it.
Second left-column paragraph in it.	It is followed by a \switchcolumn*.
It is followed by a \switchcolumn.	
Third and synchronized left-column paragraph in it.	Second and synchronized right-column paragraph with a footnote ³⁷ in it.
It is followed by a \switchcolumn.	Third right-column paragraph
	\dots with a footnote ³⁸ \dots in it.

²⁷Because of the non-merged typesetting, this footnote is put above the example.

 $^{^{32}\}mathrm{And}$ thus this footnote is merged with those in the paracol environment.

 $^{^{33}{}m First}$ left-column footnote.

 $^{^{34}{}m Second}$ left-column footnote.

 $^{^{35}}$ First right-column footnote but following the second left-column one.

 $^{^{36}}$ Third left-column footnote but following the first right-column one.

 $^{^{37}\}mathrm{Second}$ right-column footnote but following the third left-column one.

³⁸Third right-column footnote.

The example in the previous page should look weird because the order of the third footnote in the left column 36 and the first in the right 35 are reversed in their numbers and in the stack at the page bottom. However, the result is natural because they are numbered and stacked in the order of occurrence in the source .tex as always done in any documents without paracol and with it but column-wise footnote typesetting. Since the paracol cannot maintain the order automatically³⁹, you have to maintain it by yourself.

The problem is partly solved by using \footnote with its optional argument [num] to number the first right-column and the third left-column footnotes explicitly, i.e., to give num = 36 to the former and num = 35 to the latter. One caution is that you have to remember that \footnote with the optional num does not update footnote counter and thus you have to do \setcounter{footnote}{36} or \addtocounter{footnote}{2} after the third left-column footnote.

This remedy, however, cannot change the stacking order of these two footnotes of course. Therefore, you need another trick with \footnotemark and \footnotetext to stack the third left-column footnote above the first right-column one. More specifically, you can solve the problem inserting

\footnotetext[35]{\text for the third left footnote}

somewhere between \footnote commands for the second left-column and the first right-column ones, e.g., at the end of the second left-column paragraph, and attaching its mark to the appropriate word for the footnote by \footnotemark[35], to have the following.

First left-column paragraph	First right-column paragraph
Third and synchroized left-column paragraph	Second and synchronized right-column paragraph
with a footnote whose mark here ⁴²	with a footnote 44 in it.
is given by \footnotemark[42] in it.	Third right-column paragraph
It is followed by \addtocounter{footnote}{2} and	\dots with a footnote ⁴⁵ \dots in it.
a \switchcolumn.	

Though this solution gives a good result, however, it has the following two problems. First, you have to explicitly specify the footnote number through the optional arguments [num] of \footnote, \footnotetext and \footnotemark. This problem is quite severe because, for example, if you add a footnote somewhere preceding the paracol environment in question, you have to modify all [num] arguments of footnote-related commands in the environment. This means that when the footnote addition is done in the first page of a 100-page document having paracol environments with explicitly numbered footnotes in every page, you have to make the corrections for environments in 99 pages. The other a little bit less severe problem is that you have to keep footnote counter having correct value by \setcounter, \addtocounter or \stepcounter for footnotes following those with explicit numbering so that their numbers are given by the default action of \footnote.

To cope with these two problems, paracol provides you with the *starred* versions of \footnote and its relatives as introduced in Section 7.6 and detailedly explained in the next Section 8.2.

 $^{^{39}}$ So far, because the maintenance is extremely tough. But since it is not impossible, some day you could have an improved version of paracol with the automatic ordering.

⁴⁰First left-column footnote.

 $^{^{41}{}m Second}$ left-column footnote.

⁴²Third left-column footnote given by \footnotetext[42]{text} placed at the end of the second left-column paragraph.

⁴³First right-column footnote whose number 43 is explicitly given by \footnote[43]{text}.

⁴⁴Second right-column footnote correctly following the first right-column one.

⁴⁵Third right-column footnote.

8.2 Commands \footnote* and Relatives

\footnote*[+disp]{text} \footnote*[-disp]{text} \footnote*[disp]{text}

The command is similar to its non-starred counterpart but the explicit numbering with the optional argument is done in *self-relative* or *base-displacement* style. That is, if the optional argument has a leading '+' or '-', the number given to the footnote is f + disp or f - disp respectively where f is the value of footnote counter, or in other words the number given to the last footnote⁴⁶. Otherwise, i.e., the optional argument is a number without +/- sign, the number given to the footnote is b + disp where b is the base value of footnote counter at \begin{paracol} paracol} for the environment in which the command appears, or in other words the number given to the last pre-environment footnote⁴⁷.

In addition, unlike the non-starred version, this command updates footnote counter with the number given to the footnote, i.e., $f \leftarrow f + disp$, $f \leftarrow f - disp$ or $f \leftarrow b + disp$ is performed, so that following \footnote without explicit numbering option have numbers f + 1, f + 2 and so on with new f.

• If the optional argument is not provided, it is assumed that [+1] is given and thus \footnote*{text} acts as \footnote{text}.

$\footnotemark*[[+-]disp]$

This command is a mixture of its non-starred counterpart and \footnote*. That is the number for the footnote mark is calculated in the way of \footnote* and footnote counter is updated.

$\footnotetext*[[+-]disp]{text}$

Without the optional argument [+-]disp, this command does what $footnoteext{text}$ does but in addition increments footnote counter before that. With the optional argument, on the other hand, the number given to the footnote text is calculated as done in footnote, but the footnote counter is not updated.

With these starred commands, you can produce the following using the base-displacement mechanism without worrying about the absolute value of \footnote counter and its change.

First left-column paragraph	First right-column paragraph
\switchcolumn.	
Third and synchronized left-column paragraph with a footnote whose mark here 50	Second and synchronized right-column paragraph \dots with a footnote ⁵² \dots in it.
is given by \footnotemark*[3] because $50 = 47 + 3$.	Third right-column paragraph
It is followed by a \switchcolumn.	with a footnote $\overline{53}$ in it.

⁴⁶If it is put by the ordinary \footnote.

⁴⁷Or the last footnote in the previous paracol environment, etc.

⁴⁸First left-column footnote.

 $^{^{49}{\}rm Second}$ left-column footnote.

⁵⁰Third left-column footnote given by \footnotetext*[3]{text} placed at the end of the second left-column paragraph to have 50 = 47 + 3.

 $^{^{51}}$ First right-column footnote whose number 51 is given by \footnote*[4]{text} because 51 = 47 + 4.

 $^{^{52}}$ Second right-column footnote produced by \footnote*[5]{text} because 52 = 47 + 5.

⁵³Third right-column footnote produced by \footnote{text} because 53 = 52 + 1.

The other way to produce the same result except for the absolute footnote numbers is to use the self-relative mechanism and to exploit the progress of **footnote** counter as follows.

First left-column paragraph with a footnote 54 in it. Second left-column paragraph with a footnote 55 in it. It is followed by \footnotetext*{ $text$ } and a	First right-column paragraph in it. with a footnote ⁵⁷ in it. It is followed by a \switchcolumn*.
10 is followed by (100thotetext, [text] and a	
\switchcolumn.	
Third and synchronized left-column paragraph with a footnote whose mark here 56 is given by \footnotemark*[-1] because $56 = 57 - 1$. It is followed by a \switchcolumn.	Second and synchronized right-column paragraph with a footnote 58 in it. Third right-column paragraph with a footnote 59 in it.

It depends on the structure of your document which of the base-displacement and self-relative is better. If your document has frequent switching between single- and multi-column text typesetting and thus the contents of a paracol environment is relatively small, the base-displacement is a good choice because you may concentrate on one base value of footnote counter. Otherwise, especially when your document consists of one single and large paracol environment, the base-displacement is almost equivalent to maintaining absolute values and thus the self-relative should be preferred.

Note that if the last \footnote or \footnotemark in a paracol environment is starred, the command lets footnote counter have some value smaller than that for the last stacked footnote. For example, if the second and third right-column footnotes 58 and 59 are omitted from the example above, the last footnote-related command will be \footnotemark*[-1] which makes the counter at \end{paracol} 56 rather than 57. You may not worry about this problem, however, because \end{paracol} automatically maintains the counter letting it have b+n where n is the number of \footnote and \footnotemark in the environment, if the maintenance is ordered by the command \fncounteradjustment which is automatically executed by \footnotelayout with the argument p or m.

8.3 Page Break

When a paracol environment with footnotes lays across a page boundary, you could have some weird result even if the environment have just one \switchcolumn as shown below.

First left-column paragraphwith a footnote ⁶⁰	First right-column paragraph with a footnote 62
in it.	in it.

⁵⁴First left-column footnote.

 $^{^{55}}$ Second left-column footnote.

⁵⁶Third left-column footnote given by \footnotetext*{text} placed at the end of the second left-column paragraph because it follows the second footnote 55.

⁵⁷First right-column footnote whose number 57 is given by \footnote{text} because 57 = 56 + 1 and \footnotetext* for 56 lets footnote have the value.

⁵⁸Second right-column footnote produced by \footnote*[+2]{text} because 58 = 56 + 2.

⁵⁹Third right-column footnote produced by \footnote{text} because 59 = 58 + 1.

⁶⁰First left-column footnote.

Second left-column paragraph	Second right-column paragraph
\dots with a footnote ⁶¹ \dots in it.	\dots with a footnote ⁶³ \dots in it.

Since the part of the source .tex for this example above is fundamentally same as that in p. 30 at the beginning of this Section 8, footnotes are simply numbered in left-column-first manner without any tricks. However it results in giving an impression that two paragraphs in each of both columns at the bottom of the last page have footnote marks of inconsecutive numbers 60 and 62 due to the second left-column paragraph and the footnote 61 in it. More weirdly, the first right-column footnote 62 is not put in the last page where its mark is shown but is stacked below 61 in this page.

The reason why this happens is that a footnote is not immediately put to the bottom of the page where its mark resides but to the page constructing at the time when the footnote is processed at the end of the paragraph in which the corresponding \footnote (or \footnotetext) occurs⁶⁴. Therefore, it may happen even in an ordinary single-column document or a paracoled multi-column one with column-wise footnotes that a footnote is thrown to the page p+1 next to the page p in which its mark is left, when the mark is placed around the bottom of the page p.

This footnote placement mechanism becomes clearly visible in the example above in which the footnote 62 is processed after the second left-column paragraph is processed to complete the last page giving no chance to the footnote placed in the page⁶⁵. Therefore, the solution of this placement problem is to let the first right-column footnote processed before the page is broken by the progress of the left-column. That is, in the solution shown below the author inserted \switchcolumn after the first left-column paragraph to let the first right-column paragraph and its footnote are processed, and then did \switchcolumn again after the right-column paragraph to go back to the left-column.

First left-column paragraph with a footnote ⁶⁶	First right-column paragraph with a footnote ⁶⁷
	•••••

	in it.
in it.	It is followed by a \switchcolumn to go back to the
It is followed by a \switchcolumn.	left column.

 $^{^{61}}$ Second left-column footnote.

 $^{^{62}}$ First right-column footnote weirdly placed here while the footnoted main text is in the previous page.

⁶³Second right-column footnote whose mark in the main text gives impression that footnote numbering jumps from 61 to 63.

⁶⁴More accurately, the footnote is kept in a place in TEX together with other preceding but still unprocessed footnotes and then TEX examines them at the end of a paragraph in which a page break is found to decide whether each of them is included in the page just being completed.

⁶⁵In fact, even \footnote for the footnote is processed after the page break in this case.

⁶⁶First left-column footnote.

 $^{^{67}}$ First right-column footnote which is now placed in this page where its mark 67 resides.

Second left-column paragraph	Second right-column paragraph
\dots with a footnote ⁶⁸ \dots in it.	\dots with a footnote 69 \dots in it.
It is also followed by a \switchcolumn.	

Unfortunately, this tactics does not always solve the problem. If a left-column paragraph has a page break in it and a footnote before the break, doing \switchcolumn after the paragraph is too late to let right-column footnotes reside in the page just having been broken, while inserting \switchcolumn before the paragraph should cause incorrect stacking order.

The remedy for this problem is similar to that shown in Section 8.1 to cope with multiple \switchcolumn in a paracol environment. Here it is shown a little bit more formally. Suppose we have a page in a paracol environment in which a page break occurs in p_l -th and p_r -th paragraphs in the left and right columns respectively. Thus we have $p_l - 1$ and $p_r - 1$ completed paragraphs in each of both columns. Let n_l (resp. n_r) be the number of footnotes in the pre-break left-column (resp. right-column) paragraphs, and m_l (resp. m_r) be the number of pre-break footnotes in the p_l -th (resp. p_r -th) paragraph. Thus we have $n_l + m_l$ (resp. $n_r + m_r$) footnotes in the left (resp. right) column of the page before the break. The following construct assures that those footnotes are properly numbered and stacked at the bottom of the page.

```
First to (p_l-1)-th paragraphs with n_l footnotes in total given by \footnote{text}. \footnotetext*{1st footnote in p_l-th paragraph} .... \footnotetext*{m_l-th footnote in p_l-th paragraph} \switchcolumn First to (p_r-1)-th paragraphs with n_r footnotes in total given by \footnote{text}. \footnotetext*{1st footnote in p_r-th paragraph} .... \footnotetext*{m_r-th footnote in p_r-th paragraph} \switchcolumn p_l-th paragraph whose first footnote mark is given by \footnotemark*[-(m_l+n_r+n_r)).
```

 p_l -th paragraph whose first footnote mark is given by \footnotemark*[-($m_l+n_r+m_r-1$)], while second to m_l -th ones are given by \footnotemark without * nor optional [num]. The first subsequent footnotes beyond the page break, if any, is given by \footnote*[+(n_r+m_r+1)]{text} while further subsequent ones are given by \footnote{text}.

\switchcolumn

 p_r -th paragraph whose first footnote mark is given by \footnotemark* $[-(m_r+k_l-1)]$ where k_l is the number of left-column footnotes beyond the break, while second to m_r -th ones are given by \footnotemark. The first subsequent footnotes beyond the page break, if any, is given by \footnote* $[+(k_l+1)]$ {text}, while further subsequent ones are given by \footnote{text}.

The example shown in the next two pages is for the case of $p_l = p_r = n_l = n_r = m_l = m_r = k_l = 2$.

⁶⁸Second left-column footnote whose number 68 follows the right-column footnote 67 in the last page.

⁶⁹Second right-column footnote whose number 69 follows the left-column footnote 68.

First left-column paragraph with two footnoteshere ⁷⁰ by \footnote{text}	First right-column paragraph with two footnoteshere ⁷⁴ by \footnote{text}
followed by a series of \footnotetext*{text} and then a \switchcolumn.	followed by a series of \footnotetext*{text} and then a \switchcolumn.
Second left-column paragraph across two pages	Second right-column paragraph across two pages
with two pre-break footnotes	with two pre-break footnotes
70First left-column footnote given by \footnote{text}.	
THE TELL-COLUMN TOOLHOUS SIVEN BY TOOLHOUSE LEAD.	

⁷⁶ First left-column footnote given by \footnote{text}.
71 Second left-column footnote also given by \footnote{text}.
72 Third left-column footnote given by \footnotetext*{text}.
73 Fourth left-column footnote given by \footnotetext*{text}.
74 First right-column footnote given by \footnote{text}.
75 Second right-column footnote also given by \footnotetext*{text}.
76 Third right-column footnote given by \footnotetext*{text}.
77 Fourth right-column footnote given by \footnotetext*{text}.

and two post-break footnotes	and two post-break footnotes
here ⁷⁸ by \footnote*[+5]{\text}	$\dots \text{here}^{80} \text{ by } \text{ footnote*[+3]} \{text\} \dots$
and here 79 by \footnote{text}	and here 81 by \footnote{text}
followed by a \switchcolumn.	·

Note that though the remedy works well as shown above, it is not a good idea to do that when you are writing draft versions of your document because page break points go up and down by your modifications to the document. Therefore, it is recommended to put all footnotes by non-starred \footnote until your document becomes perfect except for footnote numbering and placement and then to adjust them by the techique described in this section.

⁷⁸Fifth left-column footnote given by \footnote*[+5] because $n_r + m_r + 1 = 2 + 2 + 1 = 5$ and thus 78 = 73 + 5.

⁷⁹Sixth left-column foootnote given by \footnote{text}.

⁸⁰Fifth right-column footnote given by \footnote*[+3] because $k_l + 1 = 3$ and thus 80 = 77 + 3.

⁸¹Sixth right-column foootnote given by \footnote{text}.

9 Two-Sided Typesetting and Parallel-Paging

This and the next section are typeset with \twosided enabling features p, c and m and also b for a part of the next section. The effect of p feature can be seen by the right, or in other word inside, margin of this even-numbered page is narrower than that of the previous pages because the author reduced the effective right side margin being calculated from \evesidemargin by 75 %⁸². This setting makes the left side or outside margin of this page enlarged by 125 %, as well as the right side and outside margin of the next odd-numbered page specified by \oddsidemargin.

Next, we see the effects of c and m features by the paracol environment below for which \columnratio{0.6} and \marginparthreshold{0} are declared to make the *inside* columns (right ones in even-numbered pages) are wider than the *outside* ones and all marginal notes go to outside (left in even-numbered pages) margins.

First marginal note from column-0.

First marginal note from column-1.

Second marginal note from column-0. Second marginal note from column-1. This is the first paragraph in the narrower, italicized and outside column-1. In this paragraph, we shortly have a marginal note, italicized too, which goes to the outside margin shared by all marginal notes from both columns. The marginal note given here is placed its natural position and its first line is aligned to the first line of the second sentence of this paragraph by exploitation of the space between two marginal notes from the column-0, though we already have had three notes from the column.

Now the author puts another marginal note whose first line would be aligned to that of this paragraph, but it is pushed down below the second marginal note from the column-0 because two notes conflict with each other over the space⁸³. Note that since the note from this column is given after that from the column-0 was given, the conflict is solved pushing the note from this column down rather than that from the column-0. Now the author puts a few dummy lines to go to the second last line of this page.

This is the third paragraph of the outside column-1, which becomes right shortly

This line of the first paragraph of the inside column-0 has a marginal note. Now the author puts a few dummy lines to keep a space below the marginal note.

.....

•			•							•		•		 						•	•	•	•	•	•	•	•	•		•	•							•	•		•	•						•	•		•				
•	•	•	•				•	•	•	•		•		 				•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•					•	•	•	•	•	•				•	•	•	•	•	•		•	•
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			1	7	h:	is		li	n	ıe	,	o	f	tl	h	е	5	se	96	c)	n	d		r) 8	u	٠٤	ı	21	:8	ı	ol	h	(0	f	t	h	e		iı	n	si	id	lε	,	c	О	ŀ	u	n	ır	1-	(

also has a marginal note. Now the author puts a few dummy lines again but this time to go down to the bottom of the page.

This is the third paragraph of the inside column-0 having a page break in it. Since shortly we will be in an odd-numbered

⁸²This document itself does not have twoside option in its \documentclass but the inconsistency between the option and \twosided is not visible because \pagestyle is plain.

⁸³Since the author is temporarily disabling the warning from marginal note placement mechanism of L^AT_EX, pushing down the second marginal note from column-1 is silently performed when you process this document.

page 39 (now), this wider column is now left one keeping it inside, while the marginal note given in the first line of this page goes to right and outside. Now we will have a \switchcolumn below this paragraph to go to the column-1 and back to the previous page 38.

by the page break. The third marginal note Third is given in the first line of this page, but marginal it is pushed down again due to the conflict note from with the note from the column-0.

column-0 Thirdmarginal

Note that the position of the last marginal note in the paracol environment which we just have closed note from affects the marginal note placement in post-environment stuff. For example, the marginal note given in the first column-1. line of this paragraph is pushed down.

We will see a few examples of parallel-paging shortly, but before that we will have an intentional black note given page to make the first page of the example odd-numbered to avoid you have an impression that its layout is after incorrect⁸⁴ because if it were in an even page you would see the *outside* third and fourth supplementary columns paracol at first.

Marginal environment is closed.

⁸⁴At least the author himself had such impression without the blank page.

(intentionally blanked page)

Example of Paired Parallel-Paging

Shortly we will start a paracol environment by \begin{paracol}[2]{4} having four columns but two for each of left and right paired parallel-pages. Since the author declares \columnratio{0.6}[0.5], the columns in left pages are made unbalanced while those in right pages are balanced.

This is the first paragraph of the leftmost column-0, whose first line has a marginal note placed in the right margin because the setting of \marginparthreshold being 0 is still effective and we are in the odd-numbered page 41. Now we have a \switchcolumn to the next column-1.

This is the first paragraph of the sec- Marginal ond and right column-1 in the left parallel- note from page. We shortly give an italicized mar- column-0. ginal note carefully, so that it does not conflict with the marginal note from the column-0. That is, now the author puts Marginal the note. Now we have a \switchcolumn note from to the next column-2.

column-1.

A Spanning Text: though this is wider than the page width, this text does not span the boundary between the left and right parallel-pages.

We have come back to this column-0. The space above the spanning text is due to the synchronization because two paragraphs in the column-2 are significantly taller in total than the	We have restarted this column-1. This paragraph has a footnote ⁸⁵ as shown be low.
paragraphs in other columns. As the spanning text itself says,	
it cannot extend to the right parallel-page. The author puts	
dummy lines to go to the page bottom.	
Now we will have a page break shortly. You could be surprised by seeing this column is not in the left parallel-page after	After the page break below, this column also goes to the right page together with the

⁸⁵This footnote is put in the left parallel-page together with another footnote below given in the column-2 in the right parallel-

page. 86 This footnote is not put in the right parallel-page though it is given in the column-2 in the right parallel-page and thus its reference is in the column, of course.

This is the first paragraph of the column-2 being the left column of the right parallel-page. Though we are in a page different from that column-0 and 1 reside in, this page is still numbered 41 because the left and right page is paired. Therefore, the left margin of this page is narrower than the right margin because the page number is odd.

You have to notice the first paragraph does not start from the page top but above it we have some space of exactly same size as the pre-environment stuff shown in the left parallel-page. Therefore, the top of the first paragraphs in all columns are aligned. The marginal note given in the first line of this paragraph goes to the right margin of this page because of the \marginparthreshold setting and the parity of this page. Now we have a \switchcolumn to the next column-3.

We have a few other materials not shown in right

This is the first paragraph in the last rightmost Marginal column-3 whose width is equal to that of the column- note from 2. The marginal note given in the first line goes column-3. to right and does not conflict with that from the column-2. We are now going back to the column-0 by a \switchcolumn* with a spanning text.

As expected, this line is aligned to the first line of

Marginal

note from

column-2.

parallel-pages. The space above this paragraph is for the spanning text placed in the left parallel-page. The page-wise footnote given here so also not in this page out in the left. Finally, the author has put a page-wise figure spanning columns just before \switchcolumn by which we left this column, but it will be in the right	the paragraph in the column-2 as well as those in column-0 and 1. It is also consistent the first lines including that of this paragraph are not indented because the spanning text is given by \subsection* which makes first paragraphs unindented.
page 42 together with column-0 and 1.	
Though the footnote numbered 86 goes to the left	After the page break we will have shortly, this col-

Another marginal note from column-3.

as you are seeing now, but still outermost as well as the marginal note in the outside left margin.

columns shorter in the previous page. Similarly, we have a space above for the page-wise figure shown in the right page.

page-wise figure given in column-2

Figure 11: A Page-Wise Figure

Another marginal note from column-1.

column-0 and is placed outside (left) in the page, as well as the marginal note in this right page but in the outside margin.

the break but in the right one. This is because the feature c is enabled to swap not only columns in a page but also the left and right paired parallel-pages when they are even-numbered. The other feature p makes the left outside margins of this right and the previous left pages wider than the right inside margins.

Now you are seeing yet another material placed only in the page in which the column-0 resides and thus being the right page now, i.e., this paragraph and the next one in the post-environment stuff. You might be disappointed by the fact the *outside* pages, i.e., left in this page 42 and right in the previous page 41, cannot have page-wise stuff but it is what the author can do now for the version 1.3 and thus you have to wait some future versions in which the author could devise a mechanism to exploit the corresponding space in the pages⁸⁷. In addition, you might think it is weird that the c feature of \twosided swaps columns and paired pages. However this swapping is a natural consequence of the combination of column-swapping and paired parallel-paging. Therefore, you can simply disable the c feature (maybe together with other features) to have more intuitive results.

In the next Section 9.2, you will see another kind of parallel-paging namely non-paired one. Before that, we need a blank page to let the non-paired parallel-paging start from an even-numbered page so that a left and right page pair comprises a double spread. A short remark on the blank next page is that it does not have a right counterpart parallel-page because the page is outside paracol environments and does not have any portion from the environments⁸⁸.

⁸⁷You might complain the immaturity of parallel-paging and might claim that it should be included in paracol after the author implements the mechanism. In fact the author himself is frustrated current features of parallel-paging but he dared to release the version 1.3 knowing that there are people who happily typeset their parallel-paged documents with the current limited features.

⁸⁸To illustrate this fact, the author dares to put a real blank page rather than stepping the page counter.

(intentionally blanked page)

9.2 Example of Non-Paired Parallel-Paging

This and following three pages are to show an example of non-paired parallel-paging, in which the author keeps the setting of <page-header> (columnratio and \marginparthreshold unchanged. The arguments of \begin {paracol} for column population are also unchanged to have 2+2 configuration, but the first argument is followed by * for non-paired typesetting. That is, the environment below starts by $\ensuremath{\mbox{begin}{paracol}[2]*{4}}$. The contents of the environment is also almost same as the previous Section 9.1, while bold-faced words show the difference from the paired typesetting.

Marginal note from column-0.

This is the first paragraph of the leftmost column-0, whose first line has a marginal note placed in the **left** margin because the setting of \marginparthreshold being 0 is still effective and we are in the **even**-numbered page **44**. Now we have a \switchcolumn to the next column-1.

Marginal note from column-1.

This is the first paragraph of the second and right column-1 in the left parallel-page. We shortly give an italicized marginal note carefully, so that it does not conflict with the marginal note from the column-0. That is, now the author puts the note. Now we have a \switchcolumn to the next column-2.

A Spanning Text: though this is wider than the page width, this text does not span the boundary between the left and right parallel-pages.

We have come back to this column-0. The space above the spanning text is due to the synchronization because two paragraphs in the column-2 are significantly taller in total than the	We have restarted this column-1. This paragraph has a footnote ⁸⁹ as shown below.
paragraphs in other columns. As the spanning text itself says,	
it cannot extend to the right parallel-page. The author puts	
dummy lines to go to the page bottom.	
Now we will have a page break shortly. You will not be surprised by seeing this column is still in the left parallel-	After the page break below, this column also staus in the left page together with

⁸⁹This footnote is put in the left parallel-page together with another footnote below given in the column-2 in the right parallel-page.

page. 90 This footnote is not put in the right parallel-page though it is given in the column-2 in the right parallel-page and thus its reference is in the column, of course.

This is the first paragraph of the column-2 being the left column of the right parallel-page. Since we are in the page next to that column-0 and 1 reside in, this page is numbered 45 because the left and right page is non-paired. Therefore, the left margin of this page is narrower than the right margin because the page number is odd.

You have to notice the first paragraph does not start from the page top but above it we have some space of exactly same size as the pre-environment stuff shown in the left parallel-page. Therefore, the top of the first paragraphs in all columns are aligned. The marginal note given in the first line of this paragraph goes to the right margin of this page because of the \marginparthreshold setting and the parity of this page. Now we have a \switchcolumn to the next column-3.

We have a few other materials not shown in right

page, its space and that of 89 make this and the next

This is the first paragraph in the last rightmost Marginal column-3 whose width is equal to that of the column- note from The marginal note given in the first line goes column-3. to right and does not conflict with that from the column-2. We are now going back to the column-0 by a \switchcolumn* with a spanning text.

As expected, this line is aligned to the first line of

umn is kept being the rightmost in the right

Marginal note from column-2.

parallel-pages. The space above this paragraph is for	the paragraph in the column-2 as well as those in
the spanning text placed in the left parallel-page. The	column-0 and 1. It is also consistent the first lines
page-wise footnote given here ⁹⁰ is also not in this page	including that of this paragraph are not indented be-
but in the left. Finally, the author has put a page-wise	cause the spanning text is given by \subsection*
figure spanning columns just before \switchcolumn by	which makes first paragraphs unindented.
which we left this column, but it will be in the left page	
46 together with column-0 and 1.	
Though the footnote numbered 90 goes to the left	After the page break we will have shortly, this col-

page-wise figure given in column-2

Figure 12: A Page-Wise Figure

Another marginal note from column-1.

page after the break. This is because the feature c is not effective in non-paired parallel-paging. The other feature p consistently makes the left outside margins of this and the previous page in which this column resides wider than the right inside margins.

the column-0 and is placed inside (right) in the page, as well as the marginal note in this left page still in the outside margin.

As the post-environment stuff in Section 9.1 is, this paragraph being the post-environment stuff of the non-paired parallel-pages appears only in the parallel-page in which the column-0 belongs to, and thus in the left parallel-page in this case.

columns shorter in the previous page. Similarly, we have a space above for the page-wise figure shown in the **left** page.

parallel-page, as you are seeing now, and still out- Another ermost as well as the marginal note in the outside marginal right margin.

note from column-3.

10 Examples of Background Painting

10.1 Fundamental Painting

As you undoubtedly notice, this page and a few pages following it are colorfully painted. For this and the next three pages, the author declared the background color of each region as follows.

```
\backgroundcolor{t}[rgb]{0.7,0,0}
                                        % dark red for top margin
\backgroundcolor{b}[rgb]{0.8,0.6,0}
                                        % dark orange for bottom margin
\backgroundcolor{1}[rgb]{0,0,0.7}
                                        % dark blue for left margin
\backgroundcolor{r}[rgb]{0,0.7,0}
                                        % dark green for right margin
\backgroundcolor{c[0]}[rgb]{1,0.8,1}
                                        % pink for column-0
\backgroundcolor{c[1]}[rgb]{1,1,0.8}
                                        % cream yellow for column-1
\backgroundcolor{g}[rgb]{0.8,1,1}
                                        % light blue for the gap
\backgroundcolor{f}[rgb]{0.8,0,1}
                                        % purple for page-wise floats
                                        % light purple for page-wise footnotes
\backgroundcolor{n}[rgb]{0.8,0.6,1}
\backgroundcolor{p}[rgb]{0.8,1,0.6}
                                        % pale green for pre/post-environment
\backgroundcolor{s}[rgb]{0.8,0.8,0.8}
                                        % light gray for spanning texts
```

Therefore, the background of this pre-environment paragraph and other stuff above is painted by pale green. Since the author set \pagerim to be 5 pt, you will see unpainted strips of 5 pt wide at all paper edges surrounding painted regions. For this and the next three pages, \twosided[pcm] is declared to enable p, c and m features but to disable the b feature. Therefore, though this page 48 is even and thus the left outside margin is wider than the right inside one, the backgrounds of 1(eft) and r(ight) margins are painted by dark blue and dark green respectively.

As explained in the right column-0, the background of this left and outside column-1 is painted by cream yellow as \backgroundcolor{c[1]} specifies. Now we have a \switchcolumn* with a spanning text to show the background painting for it⁹¹.

This column-0 is now right and inside because of the c feature of \twosided is enabled. On the other hand, the background is this column is painted by pink because \backgroundcolor for c[0] specifies so. That is, the column ordinals optionally given to c(olumn) (and g(ap)) regions are logical ones not always corresponding to their physical positions in a page.

The background of this s(panning text) region is painted by light gray

See the right column for the reason why this paragraph is here.

This paragraph is to show how the first line of a paragraph just below a spanning text is placed in the painted region.

See the right column for what we are now doing.

Now we have a \flushpage to see the background painting for a material not shown in the page, i.e., a page-wise float.

⁹¹Since the footnotes in this paracol environment are page-wise and merged, and \backgroundcolor{n} specifies light purple, the background of this (foot)n(ote) region is painted by the color.

f(loat) region for this page-wise figure is painted by purple

Figure 13: A Page-Wise Figure

Since we are now in an odd-numbered page 49, this column0 is now a left one and is still painted by pink of course.

As expected, the background of this column-1 is still painted by cream yellow.

This paragraph is to show how the last line of a page without page-wise footnotes is placed in the painted region.

See the comment in the left column.

See the right column for the reason why we have this almost blank page.	This page is to show how the page without any page-wise stuff looks like.
ac nace the annest man page.	ovan looks me.
See the right column for what will happen shortly.	Shortly we will close this paracol environment in the next page.

Now we are closing this paracol environment to show how its post-environment stuff is painted.

See the left column for the reason why we are now closing the environment.

The background of this paragraph in p(ost-environment) region is also painted by pale green, because post-environment stuff can be pre-environment stuff at the same time as we see shortly.

This short paracol environment illustrates how the preenvironment stuff of this environment, or the post-environment stuff of the last environment in other words, is painted. Therefore, the author does not have much to say in this column, except for giving a footnote here⁹².

Before moving to the next example, one caution is given for background painting of merged footnotes. As the footnote 92 itself says, merged footnotes given in the last page of a paracol environment are considered as belonging to post-environment stuff. Therefore, the footnote 92 is painted by pale green as well as another footnote given now⁹³.

⁹²Since this footnote is merged with that in the post-environment stuff, it is considered as a part of post-environment stuff and thus painted by pale green rather than light purple.

⁹³Since this footnote really belongs to post-environment stuff, its background is painted by pale green naturally.

10.2 Mirrored Painting and Enlarging/Shrinking/Shifting Regions

At a glance, this and the next three pages look painted similarly to previous four pages, but by a careful examination you should notice two important differences. The first one is found in the colors of left and right margins. As the author enabled all features of \twosided including b for mirroring and we are now in an even-numbered page 52, the left and outside margin is painted by dark green for the region r(ight margin), while the right and inside one is painted by dark blue for 1(eft margin).

The other is that regions are enlarged, shrunk or shifted by 4 pt by the following \backgroundcolor commands with extensions.

```
\backgroundcolor{t(0pt,0pt)(0pt,-4pt)}[rgb]{0.7,0,0}
                                                                                                                                                                                                  % B up
\begin{cal}{l} \beg
\backgroundcolor{1(0pt,4pt)(-4pt,4pt)}[rgb]{0,0,0.7}
                                                                                                                                                                                                  % R left T/B outside
\backgroundcolor{r(-4pt,4pt)(0pt,4pt)}[rgb]{0,0.7,0}
                                                                                                                                                                                                  % L right T/B outside
\backgroundcolor{c[0](4pt,4pt)}[rgb]{1,0.8,1}
                                                                                                                                                                                                  % all edges outside
\backgroundcolor{c[1](4pt,4pt)}[rgb]{1,1,0.8}
                                                                                                                                                                                                  % all edges outside
\backgroundcolor{g(-4pt,4pt)}[rgb]{0.8,1,1}
                                                                                                                                                                                                  % L/R inside & T/B outside
\backgroundcolor{f(4pt,4pt)(4pt,-4pt)}[rgb]{0.8,0,1}
                                                                                                                                                                                                 % L/R outside & T/B up
\backgroundcolor{p(4pt,4pt)}[rgb]{0.8,1,0.6}
                                                                                                                                                                                                 % all edges outside
\backgroundcolor{s(4pt,-4pt)}[rgb]{0.8,0.8,0.8}
                                                                                                                                                                                                 % L/R outside & T/B inside
```

In the comments above, L(eft), R(ight), T(op) and B(ottom) mean edges moved by a given extension. Therefore, for example, "L/R outside & T/B up" for f(loat) region means it is enlarged horizontally and shifted up vertically by the asymmetric extension (4pt,4pt)(4pt,-4pt). These a little bit complicated setting of extensions are to solve the problems in the fundamental example shown in previous four pages, namely too strict definition of the regions to be painted. That is, both vertical edges of regions having texts, e.g., c(olumn) regions, should look too close to the first and last letters. Similarly both horizontal edges of those regions seem too close especially when the first line is tall (e.g., the section title in p. 48 and the page-wise figure in p. 49) and the last line of a column is followed by spanning text or post-environment stuff. Therefore, the author made fine tuning moving inside edges of margins outside, and so on. We will come back this issue after exemplifying the effect of the tuning.

This paragraph is surrounded by spaces of a small but comfortable amount as $well.^{94}$.

By the tuning to enlarge this c(olumn) region, this paragraph has comfortable spaces above and below it, as well as at the both side edges.

The background of this s(panning text) region is painted by light gray and enlarged horizontally but shrunk vertically

See the right column for the reason why this paragraph is here.

This paragraph is to show how well the first line of a paragraph just below a spanning text is separated from the boundary of two painted regions.

See the right column for what we are now doing.

By enlarging this c(olumn) region and shift the (foot)n(ote) region down, this paragraph has a comfortable amount of space below it.

⁹⁴Shifting this (foot)n(ote) region down a little bit, the space below this footnote and above the top edge of the b(ottom margin) region is enlarged.

shifting up this f(loat) region gives us a small space above the top edge of the rectangle

Figure 14: A Page-Wise Figure

Similarly to other paragraphs below page-wise stuff, this paragraph is well separated from the bottom edge of the f(loat) region above.

See the comment in the left column for the intention of placing this paragraph here.

As in the case of the line above page-wise footnotes, the last line of this paragraph has a sufficient space separating it from the top edge of the b(ottom margin) region.

 $See \ the \ comment \ in \ the \ left \ column, \\ too.$

 $See \ the \ right \ column \ for \ the \ reason \ why$ This page is to show how the page without any page-wise we have this almost blank page. stuff looks like. As you are seeing, the space above this paragraph is sufficient and comfortable. See the right column for what will hap-Shortly we will close this paracol environment in the next pen shortly. page.

Now we are closing this paracol environment to show how this paragraph is separated from the boundary of c(olumn) and p(ost-environment) regions.

See the left column for the reason why we are now closing the environment.

The background of this paragraph in p(ost-environment) region is painted by pale green as done in p. 51, but its top and bottom edges *look* shifted down and up to give spaces below and above the last and first paragraphs in paracol environments, respectively.

This short paracol environment illustrates how the preenvironment stuff of this environment, or the post-environment stuff of the last environment in other words, is painted. Therefore, the author does not have much to say in this column, except for giving a footnote here⁹⁵.

In the setting with $\begin{tabular}{l} backgroundcolor commands in p. 52, the author carefully moved contacting edges of regions. For example, to enlarge <math>c(\text{olumn})$ regions, the inside edges of l(eft margin) and r(ight margin) regions are moved outside, and both vertical edges of the g(ap) region shifted toward its inside. As for the horizontal edges, the bottom edges of t(op margin) and f(loat) regions are moved up, the top edges of b(ottom margin) and f(oot)n(ote) regions are moved down, and both top and bottom edges of the s(panning text) region are shifted toward its inside.

These edge shifting could make a region too narrow or too much shifted resulting in a material in it over-reaching its boundary, especially in vertical shifting of horizontal edges. However we can exploit some large space automatically or manually inserted above and/or below the material to avoid overreaching. That is the author exploited the following spaces; \headsep below the page head (though it is empty in this document); \dbltextfloatsep below the bottom-most page-wise float; spaces that \subsection* inserts above and below it together with manually inserted \medskip below it; \skip\footins⁹⁶ above the first footnote which the author enlarged by 4pt temporarily for this and the next subsections; and \footskip from the bottom edge of text area to that of the page number.

Now you might notice that the explanation above does not mention the p region for pre-environment and post-environment stuff. As you should find in the settings, this region is enlarged horizontally and vertically so that its top and bottom edges are moved up and down when the region is at the top or bottom of a page, as you are seeing now and find in p. 52. However, this enlargement of course has a side effect that the region collides against c(olumn) and g(ap) regions also enlarged vertically making them overlapped. This overlap will be invisible with most of printers because, as shown in Section 7.8, p region is painted before c and g regions are painted. In addition, since relatively large spaces of \bigskip are manually inserted before each \begin{paracol} and after each \end{paracol}, texts in pre-environment and post-environment stuff are well separated from region boundaries.

This overlay painting c and g over p, however, might produce an unexpected result with some printer with which, for example, two colors are *blended* in the thin overlapped strip⁹⁷. Unfortunately, this overlay painting is inevitable in the current version 1.3, but in a future version, hopefully 1.4, more sophisticated *position-dependent* region definition, for example, to shift the top edge of p region only when the region is at the top of page, could be introduced.

Another remark is that the mirroring specified by the b feature of \twosided works not only on the colors of side margins but also on their asymmetric shrinkage. That is, the asymmetric shifts of vertical edges of 1 and r regions correctly performed irrespective of their physical positions, i.e., even when the 1 (resp. r) region is at the right (resp. left) margin and the edge to be shift is the left (resp. right) one rather than right (resp. left).

⁹⁵As the footnote 92 in p. 51, this merged footnote is a part of post-environment stuff and thus painted by pale green rather than light purple.

⁹⁶This is a kind of "length command" maybe not widely known.

 $^{^{97}}$ For example, a dvi previewer **dviout** produces such a blended result with the default setting of coloring.

10.3 Regions with Infinite Extensions

You are now seeing another background painting much different from previous two examples. That is, after disabling painting of t, b, 1, r and g regions by \nobackgroundcolor, the author gave the followings for painting this and the next pages.

```
\backgroundcolor{c[0](4pt,4pt)(0.5\columnsep,4pt)}[rgb]{1,0.8,1}
\backgroundcolor{c[1](0.5\columnsep,4pt)(4pt,4pt)}[rgb]{1,1,0.8}
\backgroundcolor{C[0](10000pt,10000pt)(0.5\columnsep,10000pt)}[rgb]{1,0.8,1}
\backgroundcolor{C[1](0.5\columnsep,10000pt)(10000pt,10000pt)}[rgb]{1,1,0.8}
```

The first two lines above is different from the previous declaration because inside edges of c[0] and c[1] regions are shifted toward outside of them and thus inside of unpainted g region so that the edges are contacted. On the other hand, the last two lines are for *under-painting* of columns and has *infinite extension* to make top, bottom and outside edges of C regions reaching to the corresponding paper edges. Since this under-painting is done with colors same as those of over-painting of c regions, you will have an impression that the paper is two-toned and page-wise stuff are pasted on the paper⁹⁸.

As explained in the right column, this c[1] region also has an invisible left edge shifted left by 4 pt⁹⁹.

Though you cannot see, the right edge of this over-painted c[0] region is shifted right by 4pt to hide the small patch at the right bottom corner of the p region above by overlaying.

This s(panning text) region could be extended to both side edges of the paper if its extension were (10000pt,-4pt).

Little to say as well.

The author does not have much to say now for this column chunk.

Nothing to say as well.

Still nothing to say particular to the page break we will have shortly.

⁹⁸This footnote is given outside paracol environment but its background is painted by light purple because it is merged with the footnote 99.

 $^{^{99}}$ This (foot)n(ote) region could be extended to both side edges and the bottom edge of the paper if its extension were (10000pt,-4pt)(10000pt,10000pt).

This f(loat) region could be extended to both side edges and the top edge of the paper if its extension were (10000pt,10000pt)(10000pt,-4pt).

Figure 15: A Page-Wise Figure Imported from Pre-Environment

This paragraph is just for keeping the paracol environment alive in this page.

This paragraph is not necessary for keeping alive the environment but is given for consistent view.

Note that overlay painting is inevitable for two-toned page painting, as far as you want to paint background of page-wise stuff.

The last issue of background painting is about painting materials given outside paracol. As you have seen, pre-environment and post-environment stuff are painted but it is done only when they reside in a page having a portion of a paracol environment (maybe) of course. Therefore, the next page is *not* painted because the page does not have any parallel-columned stuff. Therefore, even if you wish to paint the whole of your document including pages without paracol stuff, you cannot do it just with paracol package, at least so far.

On the other hand, some materials given outside paracol environments are painted as if they are given in the environment when they are *imported* into the environment. One category has footnotes given in preenvironment stuff when $footnotelayout{m}$ is specified for merging, as exemplified by the footnote 98 in the previous page. Note that such a footnote is painted by the color for n region rather than p region even when there are no footnotes in the paracol environment. The other category has ordinary floats given by figure and/or table (i.e., neither figure* nor table*) environments outside paracol and then *deferred* to a page having (a portion of) stuff produced by paracol. Since such a float, e.g., Figure 15 in this page, is considered as a page-wise float given in the paracol environment in this section, its background is painted by the color for the f region, rather than that for the p region which would be used if the float were is placed in the previous page. Note that such a deferred float import could occur not only from the page having \begin{paracol} but also from pages preceding it. For example, if you have three figure environments in a page p-1 just preceding the page p in which you start a paracol environment, it could happen that first one is placed in p-1 without painting, the second is placed in p and painted by the color for p, and the third is placed in p and painted by the color for p.

Finally some materials *exported* from a paracol environment are painted as if they are in post-environment stuff. In previous two subsections, we saw merged footnotes (e.g., 92 in p. 51 and 95 in p. 55) are painted by the color of p rather than n. The other kind of exportation is of page-wise floats given in a paracol environment but deferred to the page next to the page having \end{paracol}, or further. For example, Figure 16 is given in the paracol environment above in this page, but its background is not painted because the next page in which the figure is placed does not have any parallel-columned stuff¹⁰⁰.

 $^{^{100}\}mathrm{If}$ it has, the background is painted by the color for p.

This figure is given in the paracol environment closed in the previous page but its background is not painted.

Figure 16: A Page-Wise Figure Exported to Post-Environment

(intentionally blanked page to show this page is not painted)

11 Known and Unknown Problems

Here a few problems you could face in the use of paracol are summarized.

- If your (e.g.,) left column goes ahead too much farther than the right column, LATEX could stop with the following error message.
 - ! Package paracol Error: Too many unprocessed columns/floats.

This usually means that the internal space to keep materials in the left column is exhausted. More specifically, suppose at some point in your .tex the left column is in the page p while the right is in q < p. We need (p-q) boxes to keep the left column contents in the pages q, q+1, ..., p-1 because these pages cannot be printed yet until the right column fills them. In addition, we also need two boxes for the left column in p and the right column in q so that you make column-switching between them keeping unprinted contents in them. Therefore, at least we need to have (p-q)+2 boxes, while the number of them provided by LATEX is only 18^{101} . Therefore, paracol cannot continue its work if (p-q) reaches 17. Furthermore, other stuff also consumes the boxes as follows.

- If there are n pages in q, q + 1, ..., p having pre-environment stuff or page-wise floats, n boxes are consumed by them. Similarly, if m pages in them have page-wise footnotes, m boxes are given to them
- If the left (resp. right) column has column-wise footnotes in p (resp. q), a box is used for them.
- If the left (resp. right) column has k floats to be placed in p (resp. q) or to be deferred to p+1 (resp. q+1) or a succeeding page, k boxes are reserved for them.

Therefore, it should be safe to keep (p-q) from exceeding 10 or so placing \switchcolumn in both columns fairly frequently.

- As discussed in Section 7.2, setting a synchronization point in a page brings the following side effects.
 - Stretch and shrink factors of all vertical skips in the page are nullified. The nullification of stretch factors could make a sparse column in the page have a vertical space at its bottom as if \raggedbottom setting is in effect even with \flushbottom one, rather than distributing the amount of the space to the skips so that the bottom line is aligned at the page bottom. As for the nullification of shrink factors, it makes the page have lines a little bit less than that it would have without synchronization because lines above the (last) synchronization point cannot be compressed. The other effect is a little bit subtle because the shrink factors below the last synchronization point are taken care of by TEX's page builder when it examine the appropriateness of each breakable point, but they are nullified when the page is printed. That is, if TEX finds a good break point which needs that the stuff between the synchronization and break points is compressed a little bit, the stuff is printed without compression making its bottom edge a little bit below the page bottom.
 - After a synchronization point is set, columns in the page cannot have top floats any more even if a column has space above the synchronization point and large enough to place the float. Therefore, if you like to exploit the space, you have to place the figure or table environment in question prior to the column-switching command or environment for the synchronization.

¹⁰¹ Readers who are acquainted with LATEX implementation will understand that 18 is the cardinality of the set {\bx@A,...,\bx@R} for floats acquired by \newinsert. Those who are more familiar with that might know that most LATEX, based on e-TEX or others having similar extensions, now have 52 \inserts {\bx@A,...,\bx@Z,\bx@AA,...,\bx@ZZ} for floats and materials of paracol, since 2015

• As the author did for Section 1 to 5, sometimes you will make a section header spanning all columns by giving a sectioning command such as \section, \subsection and \subsubsection to the optional argument of \switchcolumn* or \begin of a synchronizing column-switching environment. These three commands work well and you will have what you intend to have, but you have to be careful with lower-level commands \paragraph and \subparagraph. Unlike higher-level relatives, these lower-level commands does not put the header immediately but keep it somewhere 102 so that when the paragraph following the command starts it is put as the leading part of the paragraph. Therefore if the spanning text has (e.g.) \paragraph only, the header is not put as a spanning text but at the head of the first paragraph of the column to which you switch, leaving an empty spanning text with some large space as follows.

This left-column paragraph precedes a synchronized column-switching.

This right-column paragraph precedes a synchronized column-switching.

A Spanning Text Given by \paragraph This left-column paragraph follows the synchronization but is led by \paragraph given to the optional argument of \switchcolumn* for spanning text.

This right-column paragraph follows the synchronization with an empty spanning text.

Therefore, unless this is what you intend to do, you have to give some paragraph together with \paragraph to the optional argument for spanning text. For example, \mbox{} is a good candidate as the paragraph following \paragraph because it produces (almost) nothing. By using this technique the example above becomes the followings.

This left-column paragraph precedes a synchronized column-switching.

This right-column paragraph precedes a synchronized column-switching.

A Spanning Text Given by \paragraph Followed by \mbox{}

This left-column paragraph follows the spanning text above.

This right-column paragraph follows the spanning text above.

- As shown in Section 8, it is not easy to have good numbering and stacking order of page-wise footnotes even with the supports from \footnote* and its relatives. In addition, a footnote in a paracol environment cannot be broken into two (or more) pages.
- As the author confessed in Section 9.1, right parallel-pages cannot have page-wise stuff but have blank spaces in the corresponding region for them. The author will try to remove this limitation from a future version of paracol, in the version 1.4 hopefully.
- As discussed in Section 10.2, it is desirable that background painting region definition in \backgroundcolor has position dependent extensions. The author is fairly optimistic about the incorporation of this advanced feature in the version 1.4.
- In the release dated 2015/01/10, LATEX changed its mechanism of the placement of double-column floats (or in our terminology, page-wise floats) to avoid out-of-order appearance of them. That is, until the release on 2014/05/01 a double-column float (e.g., figure*) can be overtaken by a single-column float of the same category (e.g., figure) when they cannot be put into the page in which texts around them are put. In order to cope with the problem, the new version merged two lists to keep deferred double- and single-column floats into one so that the appearance order of them is determined by their order in the

 $^{^{102}}$ For people familiar to TEX's dangerous bends, the header is kept in \everypar.

single list. Though this change should have made people happy when they typeset *ordinary* two-column (or multiple-column) documents, the new feature might not be welcomed by paracol users because your parallel-columns have their own *streams* of floats to be put in the corresponding columns. Therefore, and for the sake of simplicity of paracol's implementation, the author decided to nullify this new feature in paracol environments. That is, even with new releases of IATEX, your page-wise floats given in a paracol environment can be overtaken by column-wise floats.

In addition to the problems above known to the author, there may be (or should be, honestly speaking) other unknown problems in paracol because it cannot be perfect though the author has made his best effort for testing and debugging it. Particularly, sometimes it is very tough, if not impossible, to make paracol compatible with other packages, especially with those having dark magic as paracol has in it¹⁰³. Therefore, though reporting incompatibleness with a package you use is very welcome¹⁰⁴, you should kindly understand the toughness of the compatibility issue.

Furthermore, even without such problematic packages, paracol might produce weird results due to its bug. If your document has something to make unknown bugs visible, you might have one (or more) of the followings which the author encountered in his debugging work.

- A page, a column, a footnote and/or a float disappears ¹⁰⁵.
- A page, a column, a footnote and/or a float is duplicated.
- A message like "Overfull \vbox (1.23456pt too high) has occurred while \ouptut is active" is shown.
- A message "Underfull \vbox (badness 10000) has occurred while \ouptut is active" is shown. This message, however, does not always mean a bug but may just be a complaint that a column or a page is too sparse to meet your request to align the bottom of all columns and pages by \flushbottom setting. Therefore, if you have this message and you cannot be sure whether it means a bug or not, try \raggedbottom setting to see if you still have the message, before sending a bug report to the author.

If you encounter anything like them (or whatever you cannot solve by yourself), don't hesitate to report it to the author with minimum source file to produce the problem ¹⁰⁶.

 $^{^{103}}$ For example, the author knows it is almost impossible to make paracol compatible with one of the author's own package available in CTAN.

¹⁰⁴For example, paracol is now compatible with color package thanks to a report from a user.

¹⁰⁵In fact, a bug fixed in version 1.2 caused page losing though it happens very very rarely but an unlucky user encountered it. ¹⁰⁶And with patience because your problem might not be solved quickly.

Implementation

1 Overview

1.1 Column-Pages

In our parallel multi-column typesetting, a column may grow independently of other columns and may cross its page boundary asynchronously with others. Therefore, we cannot throw away the contents of a column in a page, or a *column-page* in short, when a page break occurs in the column. Instead, we have to keep column-pages until all columns are *synchronized* implicitly or explicitly.

An implicit synchronization takes place when all columns in a page see page-breaks to let the page is shipped out. In general, all columns but the last one which arrives the page-break have completed column-pages in the page in question and some of them may have succeeding column-pages. Therefore, we maintain the list of completed column-pages $S_c = \pcol@shipped\cdot c$ for each column $c \in [0, C)$, where $C = \pcol@ncol$ is the number of columns given through the argument of paracol environment, and the set of them $S = \{S_c \mid c \in [0, C)\}$.

Each element $s_c(p)$ of a list S_c is an \insert whose \vbox contains the p-th completed column-page 107 , where p=0 for the first column-page produced in paracol environment or that following a page flushing macro \flushpage, \clearpage or \cleardoublepage. That is, S_c is defined as follows, where $p_b = \pcol@basepage$ is the zero-origin ordinal of the base page being the oldest page not shipped out yet.

$$\begin{split} S_c &= (s_c(p_b), s_c(p_b+1), \dots, s_c(p_b+k-1)) \\ &= \texttt{Qelt}\, s_c(p_b) \, \texttt{Qelt}\, s_c(p_b+1) \, \cdots \, \texttt{Qelt}\, s_c(p_b+k-1) \end{split}$$

Note that a list S_c can be empty and all members in S may be empty.

The other type of synchronization, explicit synchronization, takes place by \switchcolumn* or the beginning of starred column-switching environments, by \end{paracol}, or by one of page flushing macros \flushpage, \clearpage and \cleardoublepage. A flushing explicit synchronization ships out the pages from p_b to $p_t = \polenoise \pole$

1.2 Current Column-Pages and Their Contexts

We also have to maintain another type of column-pages which are currently built, or *current column-pages* in short, to switch from a column to another. Since each column may have its own *context* for the typsetting of it, or *column-context* in short, it were perfect to save the context when we leave from a column and to restore that when we revisit the column if we could. However, TEX and LATEX has a tremendously large number of context variables and the number becomes virtually boundless when we take variables defined in various styles and by users themselves into account. Therefore, we had to abandon to keep the whole context of the column but carefully chose a small subset comprising variables automatically modified outside

 $^{^{107}\}mathrm{Other}$ registers such as **\count** are not used.

of users' control. That is, the column-context $\kappa_c = \text{\color} c$ of a column c consists of the following elements, each of which named e is referred to as $\kappa_c(e)$ hereafter.

- β represents \insert β containing the followings.
 - $-\beta^b = \text{box} \cdot \beta = \text{Qholdpg}$ is the \vbox containing the main vertical list which has already contributed to the current column-page.
 - $-\beta^p = \text{count} \cdot \beta = \text{pcolopage}$ means the current column-page belongs to the page β^p .
 - $-\beta^r = \dim \beta = \operatorname{Qcolroom}$ is the room of the column.
- $\tau = \pcol@currfoot$ is the \insert containing the footnotes added in the current column-page, if column-wise footnote typesetting is in effect. Its constituent \box, \count, \dimen and \skip are denoted as τ^b , τ^c , τ^d and τ^s respectively. On the other hand, if page-wise footnote typesetting is in effect, τ is always empty¹⁰⁸.
- $\delta = \prolepreve = b$ obtained by \prevdepth.
- $\lambda_t = \emptyset$ toplist is the list of top floats inserted in the current column-page.
- $\lambda_m = \emptyset$ is the list of mid floats inserted in the current column-page.
- $\lambda_b = \emptyset$ the list of bottom floats inserted in the current column-page.
- $\lambda_d = \texttt{Qdeferlist}$ is the list of column-wise floats deferred to the next column-page.
- $\xi = \$ is the vertical skip used instead of \textfloatsep for top floats in the current column-page if it has synchronization points, or ∞ otherwise.
- $\eta = \text{Qtextfloatsheight}$ is the total height of mid floats and their separators in the current column-page.
- $\nu_t = \mathbb{Q}$ topnum is the maximum number of top floats which the current column-page can accommodate further.
- $\rho_t = \text{Qtoproom}$ is the room for top floats in the current column-page.
- $\nu_b = \emptyset$ thum is the maximum number of bottom floats which the current column-page can accommodate further.
- $\rho_b = \emptyset$ to troom is the room for bottom floats in the current column-page.
- $\nu_c = \$ colnum is the maximum total number of floats which the current column-page can accommodate further.
- σ is the following encoding of \if@nobreak and \if@afterindent at the time we left from the column c.

$$\sigma = \begin{cases} 0 & \texttt{\ \ } \texttt{\ \ \ } \texttt{\ \ \ } \texttt{\ \$$

Note that we have only three states because $\ifloar[Cafter]$ is meaningful only when $\ifloar[Cafter]$ if $\ifloar[Cafter]$ in the states because $\ifloar[Cafter]$ is meaningful only when $\ifloar[Cafter]$ is meaningful only when $\ifloar[Cafter]$ is the states because $\ifloar[Cafter]$ is meaningful only when $\ifloar[Cafter]$ is the states because $\ifloar[Cafter]$ is meaningful only when $\ifloar[Cafter]$ is the states because $\ifloar[Cafter]$ is meaningful only when $\ifloar[Cafter]$ is the states because $\ifloar[Cafter]$ is the states because $\ifloar[Cafter]$ is the states because $\ifloar[Cafter]$ is the states $\ifloar[Cafter]$ is the states $\ifloar[Cafter]$ is the state $\ifloar[Cafter]$ is

 $^{^{108}}$ But the macro \pcol@currfoot is used to keep page-wise footnotes temporarily.

¹⁰⁹If only with the standard IATEX and so far.

• $\varepsilon = \text{verypar}$ is the tokens stored in \everypar at the time we left from the column c.

In addition, we have special context variables $w_c = \colonormal{localumnwidth} \cdot c$ in which we keep \columnwidth for the column c.

Note that we could add other variables to the saved context and/or provide some API macro to define them by users, but abandon them because it should be too complicated for users¹¹⁰. Also note that we provide a save/restore mechanism for local counters as discussed in §1.4.

1.3 Pages and Their Contexts

Besides the column-pages, we have to keep track each whole page not yet shipped out but has some complete or incomplete (i.e., current) column-pages. We maintain the list;

$$\begin{split} \varPi &= \texttt{\pcol@pages} = (\pi(p_b), \pi(p_b+1), \dots \pi(p_t-1)) \\ &= \texttt{\pcol} \pi(p_b) \texttt{\pcol} \pi(p_b+1) \cdots \texttt{\pcol} \pi(p_t-1) \\ \pi(p) &= \{\pi^p(p)\}\pi^i(p)\pi^f(p)\{\pi^s(p)\}\{\pi^m(p)\} \end{split}$$

where $\pi(p)$ is the page context of p and its elements $\pi^p(p)$, $\pi^i(p)$, $\pi^f(p)$, $\pi^s(p)$ and $\pi^m(p)$ have the followings.

- $\pi^p(p) = page(p)$ is the value of the counter page (i.e. \congregor) for the page p.
- Iff $\pi^i(p) \neq \bot$, the page p has page-wise floats or the single-column pre-environment stuff preceding ϵ in the tarting page where it resides and spanning all columns. In this case $\pi^i(p) = i$ represents tarting often tarting often tarting in the macro tarting spanning, for such tarting whose registers have the followings.
 - $-\pi^b(p) = \text{box} \cdot i$ contains the spanning stuff.
 - $-\pi^h(p) = \dim i = \mathbb{C}$ colht if positive for the height of columns shrunk by the spanning stuff. If negative, the page is only for the spanning stuff, i.e. a *float page*. We use the notation $\pi^h(p)$ for the pages $\pi^i(p) = \bot$ to mean \textheight.
 - $-\pi^t(p) = \sin \{i = \pcol@topskip\ being the value of \topskip at \begin{paracol} to be inserted at the top of each column in each non-first page. Otherwise, i.e., for the columns in the starting page following the pre-environment stuff, it has 0 to prevent the \topskip insertion. We use the notation <math>\pi^t(p)$ for the pages $\pi^i(p) = \bot$ to mean \pcol@topskip.
- Iff $\pi^f(p) \neq \bot$, page-wise footnote typesetting, discussed in §1.5, is in effect and the page p has some footnotes in $\mathtt{box} \cdot \pi^f(p)$. This element is often *cached* in the macro $\mathtt{pcol@footins}$.
- $\pi^s(p) = (span(H_1, h_1), \ldots, span(H_n, h_n)) = \{elt\{H_1, h_1\} \ldots \{elt\{H_n, h_n\}\}$ is the list of spanning texts in the page p, where i-th one's top edge is at H_i from the top of the page (excluding spanning stuff) and its height-plus-depth is h_i , where H_i and h_i are represented in the form of integers. Therefore, it is emptied by \cline{close} and then the elements are added by \cline{close} (only for the last one) and \cline{close} output@switch whenever they find a spanning text completes. The element is often \cline{close} and it macro \cline{close} find a spanning text completes. The element is often \cline{close} and \cline{close} for spanning rule and to paint columns and column-separating gap leaving spaces for spanning texts. The usage of this element is discussed in §1.7 a little bit more detailedly.

¹¹⁰ And for the author if we include save/restore of macros, though it could be done with a \toks containing the \definitions of macros.

• $\pi^m(p) = \{M_L^l\}\{M_L^r\}\{M_R^l\}\{M_R^r\}$ is the set of lists of marginal notes in the left (l) and right (r) margins and in the left (L) and right (R) parallel-pages. The words left and right of margins mean physical left and right, while left and right of parallel-pages mean the logical ones, i.e., the page where the column-0 resides is left. Each element $M_{\{L,R\}}^{\{l,r\}}$ has a list $(mpar(t_1, b_1), \dots, mpar(t_n, b_n)) = \{b_1\} \dots \{b_n\}$ of marginal notes whose top and bottom are at t_i and b_i from the top of the column area, where t_i and b_i are represented in the form of integers. Each element can be empty of course, and $\pi^m(p)$ itself can be so as well to mean all elements are empty¹¹¹. Therefore, $\pi^m(p)$ is emptied by \pcol@startpage, and then examined and modified by \pcol@addmarginpar when it adds a marginal note through macros \pcol@getmparbottom and \pcol@setmpbelt. Another modifier \pcol@output@start initializes one of the element $M_L^{\{l,r\}}$ with the value representing the last marginal note in pre-environment stuff, while another examiner \pcol@output@end lets the outside \@mparbottom have a value based on b_n of one of the element, according to LATEX's setting of marginal note placement. The whole elemnt $\pi^m(p)$ is often cached in the macro \pcol@mparbottom. The usage of this element is discussed in §1.7 a little bit more detailedly.

Note that even in parallel-paging and in non-paired one in particular, a page p consists of all columns $c \in [0, C)$. Therefore, the term left/right parallel-page p always mean the left and right component of a parallel-page (pair) p.

The reason why we keep track of page(p) is that page numbering is not necessrary to be consecutive. If such a jump occurs randomly in any columns explicitly updating page, it is very tough to give a consistent view of the page number of a specific page to all columns. Therefore we suppose jumps occur only in the leftmost column 0^{112} which controls the page numbering, while non-leftmost columns are expected to refer the page passively.

This page numbering is implemented as follows. Each time a column-page at p of the leftmost column is completed to start a new column-page, page(p) is fixed to be the value of page and $page(q) = \pi^p(q)$ for all $q \in [p, p_t]$ are let be page(p) + (q - p) in usual cases but page(p) + 2(q - p) in non-paired parallel-paging. This update also takes place on column-switching from the leftmost column-page at p to another column so that a jump happning before the switching is notified to other columns. On the other hand, starting or column-switching to a non-leftmost column-page at p lets page have page(p) referring to $\pi(p)$, unless the column starts the most advanced top page. In this new top page case, $\pi(p_t+1)$ is added to $\pi(p)$ with the temporary setting $\pi(p) = page(p) + 1 = page(p) + 2 = page(p) + 2$

Note that this management is imperfect because direct references of page in non-leftmost columns can give inconsistent results if page is modified in a non-leftmost column or the reference occurs in a page p after that the leftmost column modifies page in a page q such that $q \leq p$. In addition to them, this mechanism in non-paired parallel-paging always gives incorrect page number to the columns in a right parallel-page because $\pi^p(p)$ always has page(p) for the left parallel-page. However, it is expected that the progress of the leftmost column usually preceeds other columns to give consistent page reference even with jumps, unless the reference is made by a column in a right non-paired parallel-page. More importantly, it is assured that indirect refereces through .aux records and page numbers recorded in .toc, .idx, and so on are always consistent because of the lazy evaluation of page = page(p) at ship-out of an ordinary page p or a left parallel-page p, while the counter is let have page(p)+1 when a right non-paired

¹¹¹¹ To minimize the possibility of miscoding for emptying and save a small amount of memory for pages having no marginal notes.

¹¹²But we neither inhibit nor nullify a jump in non-leftmost column and thus the update can be seen referring to page counter explicitly.

parallel-page p is shipped out.

Also note that we also keep $\pi(p_t)$ in \pcol@currpage which is initialized by \pcol@output@ start to let $\pi^i(p_t)$ have the pre-environment stuff. Then the macro is redefined to have the value representing the new page possibly with $\pi^i(p_t)$ for page-wise floats in \pcol@startpage by the macro \pcol@defcurrpage. Another \definition is done in \pcol@output@switch also with \pcol@defcurrpage to let $\pi^f(p_t)$ have page-wise footnotes built in \footins if page-wise typsetting is in effect and the column-switching leaves the column in p_t^{113} . We denote the concatenation of Π and $\pi(p_t)$ as Π^+ to represent all pages on-the-fly.

1.4 Counters

Besides the context variables discussed in §1.2, we need to make counters local to each column except for those declared to be global by \globalcounter. Let Θ be the set (list) of all counters declared before \begin{paracol}, i.e., $\Theta = \cl@ckpt$, and

$$\Theta^g = \text{pcol@gcounters} = \{\theta_1^g, \ldots\} = \text{Qelt}\{\theta_1^g\} \cdots$$

be the set of global counters which have declared so by \globalcounter{ θ_i^g }. Then the set of local counters Θ^l is defined as follows.

$$\Theta^l = \Theta - \Theta^g = \text{pcol@counters} = \{\theta^l_1, \ldots\} = \text{Qelt}\{\theta^l_1\} \cdots$$

Since each column has its own values in local counters, we have to keep the set of counter/value pairs

$$\Theta_c = \text{pcol@counters} \cdot c = \{\langle \theta_1^l, val_c(\theta_1^l) \rangle, \ldots\} = \text{Qelt}\{\theta_1^l\}\{val_c(\theta_1^l)\} \cdots$$

for each column c, where $val_c(\theta_i^l)$ is the value of a counter θ_i^l local to c. That is, whenever we switch from a column c to d, we save $\langle \theta_i^l, val_c(\theta_i^l) \rangle$ in Θ_c and restore θ_i^l for d by letting it have $val_d(\theta_i^l)$ in Θ_d , for all $\theta_i^l \in \Theta^l$.

A global counter is free from these save/restore operations but needs another special operation when it is incremented by \stepcounter. That is, the invocation of \stepcounter for a global counter θ_i^g may clear local counters in its set of descendant counters $\zeta(\theta_i^g) = \text{pcol@cl@}\theta_i^g$ and this clearing must be performed on the all instances of $\theta_j^l \in \zeta(\theta_i^g)$ saved in Θ_c for all $c \in [0, C)$. Therefore, on the \stepcounter, we do the followings for all $c \in [0, C)$; temporarily restore all $\theta_k^l \in \Theta^l$ from Θ_c ; clear all $\theta_j^l \in \zeta(\theta_i^g)$; and then save $\langle \theta_k^l, val_c(\theta_k^l) \rangle$ back to Θ_c .

The other item we maintain for a local counter θ^l is its local representation $\langle rep \rangle$ in a column c defined by $\langle efinethecounter \langle \theta^l \rangle \langle c \rangle \langle rep \rangle$. The local representation $\langle rep \rangle$ is kept in $\langle efinethecounter \cdot efinethecounter \cdot$

1.5 Page-Wise and Merged Footnotes

Page-wise footnote typesetting is completely different from ordinary column-wise footnote typesetting.

When a column-page in the top page is built, \footins keeps all footnotes \inserted by \footnote or \footnotetext in any columns in the page. Therefore, \footnote and \footnotetext in the top page act as usual to add the footnote to \footins. Then if a column-switching takes place to leave the column, \footins is saved into $\pi^f(p_t)$ by \pcol@

¹¹³The \definition of \pcol@currpage in \pcol@setpnoelt, and emptying it in \pcol@output@start and \pcol@freshpage are for coding trick and thus not for giving a really new \definitions.

output@switch, so that $\pi^f(p_t)$ is \inserted to \footins again by \pcol@restartcolumn when it visits a column in p_t , or by \pcol@startcolumn when it finds a column proceeds to p_t .

Then, when a column-page in the top page completes advancing p_t , \footins is kept in $\pi^f(p_t-1)$ by \pcol@startpage, rather than being combined with the column-page. This saving into $\pi^f(p_t-1)$ fixes the footnotes in p_t-1 so that $\pi^f(p_t-1)$ is combined with other materials in the page by \pcol@outputelt or \pcol@makeflushedpage through \pcol@putfootins when the page is shipped out.

Fixing $\pi^f(p)$ for $p < p_t$ makes it impossible to add footnotes in a column in the page p not only to $\pi^f(p)$ but also to \footins for the page p because we have at least one fixed column-page $s_c(p)$ unable to shrink to have such additional footnotes in p^{114} . Therefore, such a footnote addition is deferred and is thrown into $\pi^f(p_t)$ through a list;

$$\Phi = \text{pcol@topfnotes} = (f_1, f_2, \dots, f_n) = \text{vbox}\{f_1 \ f_2 \ \cdots \ f_n\}$$

where f_i is a \vbox containing the deferred footnote preceded by \penalty\interlinepenalty to allow TeX to break footnotes to place them in two (or more) pages. That is, \footnote or \footnotetext in $p < p_t$ adds an element for the footnote to Φ , then all the elements¹¹⁵ are \inserted to \footnotets by \pcol@deferredfootins invoked in \pcol@restartcolumn when it visits a column in p_t , or in \pcol@startcolumn when it starts a column-page in p_t . The macro \pcol@output@end also do the \insertion by itself with merged footnote typesetting to let deferred footnotes be a part of post-environment stuff.

The reference to $\pi^f(p)$ for $p < p_t$ is also made in \pcol@restartcolumn and \pcol@flushcolumn. The former \inserts $\pi^f(p)$ to \footins so that the column-page which the macro restarts is built as if it has the footnotes in $\pi^f(p)$ to make the column-page broken leaving the space for the footnotes. However, \footins is never grown because it has been fixed and thus additional footnotes will go to Φ as discussed above. Then \footins is discarded by \pcol@makecol when the column-page completes, or by \pcol@output@switch when it leaves the column.

The reference to $\pi^f(p)$ by the latter macro \pcol@flushcolumn is to build the ship-out image of the column-page to be flushed. When this macro and other macros, namely \pcol@makecol and \pcol@makeflushedpage, build the ship-out image in a page p having $\pi^f(p)$ using \@makecol, we have to be careful of the fact that the column-page has been build as if it has footnotes in $\pi^f(p)$ but the footnotes are not included in its ship-out image but that of the page. Therefore, \@colht referred in \@makecol should be shrunk by the sum of height and depth of $\pi^f(p)$ and \skip \partial \pi^f(p) by \pcol@shrinkcolbyfn. Other and more subtle adjustment is to add the stretch and shrink factors of \skip \partial \pi^f(p) at the tail of the column-page by \pcol@ unvbox@cclv. This is necessary because TeX has broken the column-page taking account of the stretch and, more essentially, shrink factors, and thus without the factors the main vertical list in the column-page could be a little bit taller than \@colht causing overfull.

The feature gathering footnotes in all columns in a page brings a problem to explicit synchronization, because a column whose contents fit the top page at the last visit may be too tall on the synchronization because other columns have put some footnotes after the last visit. That is, we cannot simply build the top page combining $s_c(p_t)$ for all $c \in [0, C)$ and $\pi^f(p_t)$ because there could be $s_c(p_t)$ too tall to reside in p_t with $\pi^f(p_t)$.

To solve this problem, we perform the following operations prior to fix the contents of p_t having an explicit synchronization point in it. First one is column-scan to visit all columns by column-switching prior to the synchronization so that TEX's page builder has opportunities

 $^{^{114}}$ The column-page $s_c(p)$ could have some space at its bottom produced by, for example, \newpage, but exploitation of such space is extremely hard.

 $^{^{115}}$ More accurately, some trailing elements may be left in Φ if its total height is too large, as discussed in §11.5.

to break too tall column-pages. Since this scan could merely break footnotes rather than the main vertical lists in the column-pages and the broken footnotes will be reconnected when the **\output-routine** is invoked for the synchronization, we then examine if all $s_c(p_t)$ are accommodated in p_t with $\pi^f(p)$.

This examination for a synchronization by \switchcolumn* or its relatives is done as a part of the inherent synchronizing procedure to see if the combination of the tallest top items, i.e., top floats and the main vertical list, and the tallest bottom items, i.e., bottom floats and columnwise footnotes, is too large causing page flushing. As for page flushing and environment closing, this pre-flushing column height check requires a special kind of synchronized column-switching by which we flush pages up to $p_t - 1$ and examine if there is a too tall column.

Then if too tall columns are found, in either cases, we move to the *tallest* column to force a page break in the column so that we have a new page with shorter columns and shorter pagewise footnotes as well. In the synchronization by \switchcolumn* or its relatives, this forced page break is then applied to all other columns so that new column-pages have top floats, if any, below which we should place the synchronization point. This examination and forced page break is repeated until we have a page without any too tall columns, because a page break may bring deferred floats and footnotes which may result in a too tall column.

1.6 Text Coloring

1.6.1 Fundamental Mechanism

Text coloring done by color package and its relatives using \special stands on the fact that the main vertical list is printed in the order of occurrence in the source .tex. That is, a command such as \color{red} puts \special{color push [1 0 0]}^{116} into .dvi to make all stuff in the main vertical list colored red until other coloring \special inserted by other coloring macro appears in .dvi. This simple mechanism works well even when the pair of coloring \specials are in different pages and/or columns because, with respect to the main vertical list, everything between them in .tex is also surrounded by the \special pair in .dvi. As for other stuff such as header, footer, floats and footnotes, IATEX surrounds them by \color@begingroup and \color@endgroup or other similar constructs so that they are colored without interference with the coloring of the main vertical list.

In paracol environment, however, the orders of the main vertical list in .tex and .dvi are not always same. When a column encounters a page break, in .dvi the other column should intervene between the stuff in the broken pair of column-pages possibly changing the color of the second column-page. A column-switching from c_1 to c_2 also makes the main vertical list out-of-order to cause another unexpected coloring because a coloring command in c_2 will have no effect when c_1 is revisited after that following its pre-switching stuff in .dvi which was put before the coloring. Therefore, we have to make *color contexts* in both .tex and .dvi coherent inserting appropriate \specials into .dvi whenever an out-of-order *jump* occurs in .dvi by a page break or in .tex by a column-switching.

The color package and its relatives¹¹⁷ assume that *printers* have a stack for coloring and thus a coloring \special pushes the new color into the stack while it is popped by another \special which will be inserted by \aftergroup mechanism when a group surrounding the coloring \special is closed. Therefore we have to keep track of the color context with *color stack*

$$\varGamma = (\gamma_1, \gamma_1, \dots, \gamma_n) = \texttt{\t vbox} \{ \gamma_1 \ \gamma_2 \ \dots \ \gamma_n \}$$

¹¹⁶If .dvi is processed by dvips, or other printer-dependent command corresponding to it.

 $^{^{117}}$ And all other coloring mechanism compliant with IATEX 2_{ε} , hopefully and believingly.

where γ_i is a \vbox of 1 sp tall, 0 deep and 0 wide containing a coloring \special which \set@color puts into the main vertical list. That is, when \set@color is invoked we push γ to the tail of Γ , while when the corresponding \reset@color appears we pop it from Γ . Then when we encounter an out-of-order jump, at first we rewind the color stack in .dvi by putting \specials which \reset@color would put, and then reestablish the color stack by putting \specials in γ_i as if \set@color for it is invoked for all $\gamma_i \in \Gamma$. Therefore from the viewpoint of a printer, it will see stack-rewinding at the end of each column-page and the leaving points of column-switching, while the beginning of each column-page and the entry points of column-switching should have the sequence of coloring \specials to regain the color stack which the printer must have at each of the points.

In addition, for each column c we keep $\gamma_0^c = \pcol@columncolor@box \cdot c$ as the default color of the column c, optionally given by the API macro \columncolor or \normalcolumncolor. If given for c, it is assumed to be at the bottom of the color stack denoted by $\Gamma^c = (\gamma_0^c, \gamma_1, \dots, \gamma_n)$ which we rewind/reestablish at each out-of-order jump in the column c.

1.6.2 Coloring in Horizontal Mode

We have to pay attention to the fact a coloring command can appear in horizontal mode of course, and thus push/pop operations in a column-page would be done before the column-page starts when \set@color or \reset@color is in the second half of a page-crossing paragraph and if we immediately performed push/pop of the color stack in these macros. In addition, even in vertical mode these macros can appear before TeX finds a page break after which they must be in effect, if they are preceded by a sequece of non-breakable vertical items by which TeX's examination of the page break is delayed as well as the invocation of \output at the break.

In order to solve the problem of push/pop timing, we perform push/pop operations through \insert to our own register set \pcol@colorins. That is, we \insert γ to \pcol@colorins when we encounter a \set@color for γ , while its corresponding \reset@color also \inserts another \vbox γ^- of null-height/depth/width having a \special which the \reset@color puts into the main vertical list. Since we let \count\pcol@colorins = 0 and \skip\pcol@colorins = 0 to keep the \insertiion from affecting the growth of \pagetotal, it is guaranteed that an inserted γ or γ^- is given to \output through \pcol@colorins together with \box255 containing the corresponding \special.

When \output is invoked, \pcol@colorins has Γ_r containing γ_i and possibly its corresponding γ_i^- . Therefore, if \output is for a page break or a column-switching, we remove all pairs of γ_i and γ_i^- from \pcol@colorins to let it have Γ only with γ_j whose corresponding γ_j^- is not in Γ_r . For this removal, we scan Γ_r from its tail incrementing/decrementing a counter n_{pop} which we initialize to 0 before scanning. In the scan, we remove all γ^- unconditionally incrementing n_{pop} , and γ such that $n_{\text{pop}} > 0$ on the encounter with it decrementing n_{pop} . This scan is done by \pcol@clearcolorstack, invoked from \pcol@opcol for a page break and \pcol@coutput@switch for a column-switching through \pcol@clearcst@unvbox, and is for rewinding the color stack $(\gamma_0^c, \Gamma_r) = \Gamma_r^c$. Therefore, for each γ to be kept because of $n_{\text{pop}} = 0$ on the encounter with it we put \special for \reset@color. Note that on another scan for stack reestablishment, \pcol@colorins has Γ and is kept unchanged. Also note that other \output invocations such as that for floats do not touch Γ_r to allow it grows with γ and γ^- corresponding to \set@color and \reset@color in the column-page in which the invocation happens 118.

The mechanism above especially for horizontal mode has subtle issues as follows.

 $^{^{118}}$ Unlike \footins which becomes void by putting its contents back to the main vertical list to reexamine the footnote placement possibly with splitting.

- If \set@color appears in a \vbox, the \insertion for pushing is not effective but corresponding \reset@color can be outside of the \vbox to make pushes and pops unbalanced because \aftergroup for it inserts it just after the closing of the \vbox if \set@color is not surrounded by an inner group.
- If we are in vertical mode, we can know if we are in a \vbox by \ifinner. However, in horizontal or math mode, \ifinner cannot help us because it is true iff we are in a \hbox or in an in-text math. In short, TeX does not provide us with any convenient means to know if we are in a \vbox.

To solve the problem above, we introduced a trick with \everyvbox to turn a switch \ifpcol@inner = true at the beginning of every \vbox in a paracol environment, by which we supress the \insertion for \set@color because a \vbox cannot cross a page boundary. As for that of \reset@color, we suppress it by not reserving our own macro \pcol@reset@color@pop for the \insertion by \aftergroup. That is, we reserve both \reset@color and \pcol@reset@color@pop with \aftergroup if we are outside of any \vboxes, while does the former only otherwise. By the same reason, we supress the \insertion if we are in restricted horizontal mode, i.e., if both \ifhmode and \ifinner are true. On the other hand, we cannot supress the \insertion when we are in an in-text math because it can cross a page boundary 119. Note that the detailed implementation shown in §12 does not interfere the use of \everyvbox inside/outside of paracol environments or is not affected by the use.

Another attention we should pay is that color will leave $\operatorname{aftergroup}$ tokens of color and thus they are invoked just after end . However, since we have completed all column-pages in the last page, the color stack in .dvi should be empty. Therefore to avoid stack underflow, we should reestablish Γ (not Γ^c) so that elements in the stack are popped by color invoked with the $\operatorname{aftergroup}$ mechanism. We also take care of our own color stack popper $\operatorname{pcol@reset@color@pop}$ which must do nothing, i.e., must not make an $\operatorname{aftergroup}$ after we completed the last page, i.e., if $\operatorname{aftergroup}$ to $\operatorname{aftergroup}$ is false .

1.6.3 Changing Default Column Color

The implementation of \columncolor and \normalcolumncolor is relatively easy for the cases that they appear outside paracol environment or they define the default color of a column different from the current column. That is, for the default color of a column c we simply \define $\hat{\gamma}_0{}^c = \text{pcol@columncolor} \cdot c$ to let it have what \current@color has for the color. Then, in \begin{paracol} in the former case or immediately in the latter, we let $\gamma_0^c = \text{pcol@coloumncolor@box} \cdot c$ have the coloring \special for the color acquiring an \insert from \@freelist if the box is \bot .

On the other hand, when the API commands are to define the default color of the current column c, we need to place the coloring at the bottom of color stacks in terms of .tex and .dvi. That is, for the former we have to rewind and reestablish the stack which can be different from Γ^c because the API command can follow a page break which TEX does not yet find. Therefore, we maintain a shadow of Γ namely;

$$\hat{\varGamma} = \texttt{\pcol@colorstack@shadow} = (\hat{\gamma}_1, \hat{\gamma}_2, \dots, \hat{\gamma}_n) = \texttt{\qcol@colorstack@shadow} = (\hat{\gamma}_1, \hat{\gamma}_2, \dots, \hat{\gamma}_n) = (\hat{\gamma}_1, \hat{\gamma}_1, \dots, \hat{\gamma}_n) = (\hat{\gamma}_1, \hat{\gamma}_1, \dots, \hat{\gamma}_n) = (\hat{\gamma}_1, \hat{\gamma}_1, \dots, \hat{\gamma}_n) = (\hat{\gamma}_1, \dots, \hat{\gamma}_$$

to which our version of \set@color pushes $\hat{\gamma}_i$ being \current@color which the original one defines, while popping is done automatically by TEX's grouping mechanism because pushes are

¹¹⁹If an in-text math is in a \hbox, \insertion is not necessary because the math cannot cross a page boundary. Though we can detect it by a trick with \everyhbox, we abandon this idea because the request is not harmful. Another and more serious issue of coloring in math mode will be discussed shortly.

done by \edef rather than \xdef. Then before we \define $\hat{\gamma}_0^c$ we rewind $\hat{\Gamma}^c = (\hat{\gamma}_0^c, \hat{\gamma}_1, \dots, \hat{\gamma}_n)$ putting \special for pop to the main vertical list for each elements, and then after the \definition of $\hat{\gamma}_0^c$ we reestablish $\hat{\Gamma}^c$ putting coloring \special for each element.

As for placing γ_0^c at the bottom of Γ^c , we must ensure that the placement is done for the column-page in which the API command belongs to, as we did in ordinary push/pop of the color stack. Therefore the API command \inserts γ_0^c to Γ_r in the form of a \vbox, whose height and depth are 1 sp and width is 0, containing the coloring \special for γ_0^c . Then when Γ_r is scanned for rewinding in \output, this \vbox is found to let γ_0^c have the \special acquiring an \insert from \@freelist it was \bot . Note that Γ_r may have multiple \vboxes to update γ_0^c and if so the last one is effective.

1.6.4 Coloring in Math Mode

Unfortunately the solution above is imperfect because T_{EX} builds an implicit \hbox for a {math stuff} construct in math mode and an \insert in the construct does not contribute to the main vertical list at all¹²⁰. Since the implicit \hbox does not care about \everyhbox, we cannot use the trick similar to that with \everyvbox. Another bad news is that built-in \ifs for mode checking cannot help us because we always have \ifvmode = \ifmmode = false and \ifmmode = true while \ifinner is true or false when we are in in-text or displayed math mode respectively. Therefore, we have to take care of the potential loss of \insertion for pushes and thus unmatched pops in Γ_r .

For example, we have to remember that, in the cases like ${\color{c}text}$ or ${c}{text}$ expanded to the former, the \insertion for push is lost while its counterpart for pop survives making it necessary to check the existance of pushing counterpart for each pop in Γ_r^{121} . Note that the fact that the pop in the examples is in the in-text math does not help us, because the pop in ${\color{c}text}$ endgroup\$ is also in the in-text math while its pushing counterpart performs an effective \insertion, and two \insertions must be presented in Γ_r because we can have a page-break in text. Therefore, we have to find a means to examine whether a pop γ_i^- has its counterpart γ_i in Γ_r to remove γ_i from Γ_r if exists or to igonore γ_i^- otherwise. That is, we have to attach an identifier m to γ_i and γ_i^- , i.e., to make them $\gamma_{i,m}$ and $\gamma_{i,m}^-$.

Since the only means we have for the communication with \output routine is what we \insert to Γ_r , the \inserted \vbox must carry an identifier m for a push/pop in math mode. To do that, we make \vbox m sp wide (m > 0) if our version of \set@color is in math mode to represent $\gamma_{i,m}$ and $\gamma_{i,m}^-$, while the width is 0 otherwise as described in §1.6.2. Then in the scan of Γ_r for rewinding in \output, we supress incrementing/decrementing n_{pop} for $\gamma_{i,m}$ and $\gamma_{i,m}^-$, but remove $\gamma_{i,m}$ if $\gamma_{i,m}^-$ is in Γ_r as a successor while we keep it in Γ_r otherwise putting a \special of pop for it to the main vertical list.

To ensure that $\gamma_{i,m}$ has its counterpart $\gamma_{i,m}^-$ in Γ_r iff the push and pop are in a column-page, we maintain the counter \pcol@mcid incremented before (the attempt of) the \insertion of $\gamma_{i,m}$ with $m = \pcol@mcid$ and the \aftergroup reservaion for that of $\gamma_{i,m}^-$. Then the counter is zero-cleared by \output routine in order to keep it less than \pcol@mcpushlimit = 1000 unless, roughly speaking, a column-page has a unexpectedly large number of math constructs having coloring commands in them. Note that this zero-clearing does not ensure that an identifier m is unique in Γ_r . That is, it can happen that Γ_r has $\gamma_{i,m}$, $\gamma_{i,m}^-$, $\gamma_{j,m}$ and/or $\gamma_{j,m}^-$ in this order for i < j, when two math constructs with coloring for i and j are in different

 $^{^{120}}$ The contents is not thrown away but \insertion itself is added to the list rather than given to \output. 121 Since a pop is always in a group one level outer from its push counterpart, the pop request should be

presented if the push does.

paragraphs and \setminus output is invoked at or after the end of the paragraph with the math for i. This potential duplication is, however, unharmful because of the following.

- Since a math construct cannot have immediate \output invocations in it, the order of the elements in Γ_r must be $\gamma_{i,m}$, $\gamma_{i,m}^-$, $\gamma_{j,m}$ and $\gamma_{j,m}^-$ from its bottom to top, though some of them could be missing. Therefore, if $\gamma_{i,m}^-$ is in Γ_r , $\gamma_{j,m}$ must follow it if exsits not causing accidental matching with $\gamma_{i,m}^-$.
- If $\gamma_{i,m}$ is in Γ_r but $\gamma_{i,m}^-$ is not, it means we have a page break between vertical items corresponding to $\gamma_{i,m}$ and $\gamma_{i,m}^-$ to keep the \insertion of $\gamma_{i,m}^-$ and anything following it from appended into Γ_r . Therefore, Γ_r cannot have $\gamma_{j,m}^-$ not causing accidental matching with $\gamma_{i,m}$.

1.6.5 Emptiness of a Column-Page

The mechanism above works well with respect to coloring, but it has a problem that a column-page created by, for example, a forced page break may not be perfectly empty but can have some coloring \specials for color stack reestablishing and rewinding. They are of course invisible but affect the examination of column-page emptiness for explicit synchronization. That is, we examine if a column-page does not have anything by a tricky way by \pcol@ifempty but the existence of coloring \specials makes the examination failed even if no other ordinary stuff such as boxes and skips are in the column-page.

Therefore we need to put coloring \specials for color stack establishing and rewinding a little bit more carefully to avoid empty column-pages just having such \specials as follows. When we start a new column-page, we don't put \specials for establishing immediately but save the color stack Γ^c into $\Gamma_s = \poolecolorstack@saved$. Then when we leave the column-page by switching or page breaking, we examine the emptiness of the column-page and if so we do nothing, while otherwise we put the \specials for reestablishing Γ_s at the top of the column-page and those for rewinding Γ_r at the bottom. Similarly, when we revisit a column-page, we examine its emptiness and if so we save Γ^c into Γ_s , while otherwise we put \specials for reestablishing Γ^c and nullify Γ_s so that nothing will be put at the top of the column-page when we leave it. By these mechanisms, an empty column-page should not have coloring \specials, while non-empty ones should have a sequence of triples; reestablishing \specials; ordinary main vertical list items including coloring \specials inserted by \color etc.; and then rewinding \specials.

1.7 Parallel-Paging, Column-Swapping, Column-Separating Rule Drawing and Background Painting

We have the following four extensions, which are correlated to each other, from the basic parallel-columning.

Parallel-paging to extend the concept of parallel-columning in a page to a pair of adjacent pages. A *left* parallel-page starts from column-0, has C_L columns where C_L is given by the first optional argument of \begin{paracol}, while a *right* parallel-page starts from column- C_L and has $C - C_L$ columns. Since we let $C_L = C$ when parallel-paging is not in effect, we may ship out columns $c \in [0, C_L)$ always and then, if $C_L < C$, ship out columns $c \in [C_L, C)$ as a right parallel-page.

The pair of parallel-pages can be paired to comprise a virtual page p and thus has common page number page(p), while non-paired parallel-paging produces two individual pages from a

internal page p (i.e., set of all columns $\{c \mid c \in [0,C)\}$) whose left and right components have page numbers page(p) and page(p)+1 respectively. Since a page p is internally considered as the set of all columns $c \in [0,C)$ always, regardless of paired or non-paired parallel-paging, the difference between them arises only in two-sided ship-out process in which the header, footer and left-margin are common for left/right paired parallel-pags while they have to depend on the parity of the number of each non-paired parallel-page. Note that paracol does not specify the parity of a left non-paired parallel-page number, but the number is decided by the page from which a parallel-paged paracol environment starts.

In ship-out process, we build the ship-out image of a right parallel-page in our own \box register \pcol@rightpage instead of the usual \@outputbox. The register, however, must survive after \end{paracol} to keep the columns in the last right parallel-page, so that it is shipped out when the whole of last page including post-environment stuff is shipped out, or, more complicatedly, to be passed to the next paracol environment as a part of its pre-environment stuff.

Page-wise stuff spanning all columns, i.e., spanning stuff being pre-environment stuff or page-wise floats, spanning texts, page-wise footnotes and post-environment stuff are always placed in a left parallel-page, while the corresponding regions for them in a right parallel-page are always blank¹²² unless pre-environment stuff has the last page of the previous paracol environment.

Column-swapping to reverse the order of columns in even numbered pages from left-to-right to right-to-left. It is enabled by the specifier 'c' of \twosided^{123}. Though it is fundamentally simple because we just need to reverse the scanning order of columns from left-to-right (i.e., 0 to C-1) to right-to-left (i.e., C-1 to 0) in the ship-out process of an even numbered page, there are a few complications in the implementation of related functionalities.

First, a paired parallel-page should also be swapped so that a *physical* left (resp. right) parallel-page has columns C-1 to C_L (resp. C_L-1 to 0) in this order. Note that this parallel-page swapping also swaps the page in which page-wise stuff are placed. That is, if both paired parallel-paging and column-swapping are in effect, page-wise stuff are placed in the physical right parallel-page, or in other words they always placed in the page in which column-0 resides. Note that since column-swapping with non-paired parallel-paging is meaningless and thus column-swapping is disabled.

Second, the side margin to which a marginal note goes can be swapped but enabling this swap is independent of column-swapping and done by the specifier 'm' of \twosided, though almost all users will specify both swapping consistently. Since the side margin for a marginal note is decided in \output routine by \pcol@addmarginpar being our own version of LATEX's macro for maginal notes \@addmarginpar, the page in which the margial note resides has been fixed. However, the number of the page and thus its parity may not have been fixed yet due to the possible jump in column-0 taking place afterward, unlike column-swapping for which the page number has been fixed because it is performed in ship-out process. Since it is too costly to avoid this possibly wrong placement, we have to accept the possibility as LATEX itself does. Also unlike column-swapping, the swapping of marginal notes is not disabled in non-paired parallel-paging because it is meaningful.

Another remark for marginal notes is that two ore more columns may *share* a margin, inevitably if a (parallel) page has three or more columns or intentionally with a setting of \marginparthreshold. Therefore, the context of marginal notes cannot be in column-context

¹²²So far. In some future, we could implement a special setting to let pre-environment stuff, post-environment stuff and page-wise footnotes are split into both parallel-pages, and to make it possible that a page-wise float or a spanning text has its counterpart placed in the corresponding right parallel-page.

¹²³ Or the backward compatible macro \swapcolumninevenpages.

but should be in page context, or cannot simply give the bottom of the last marginal note (i.e., LATEX's \@mparbottom) but should show all marginal notes in margins in a page 124 . Therefore, each page context has all marginal notes in the form of lists of their top and bottom positions in all margins as $\pi^m(p)$, so that we find a space for a marginal note in a column to add it to not only to the bottom but also into a space between two marginal notes having already been put by other columns.

Third and finally, we have to take care the placement of spanning texts. In version 1.2 to which column-swapping is introduced, we let a spanning text belong to column-(C-1) instead usual column-0 so that its left edge is aligned to the left edge of the leftmost column, i.e., that of the text area. However this simple solution has a severe problem that, if a spanning text is broken into two pages, its second half should be put in the rightmost column. In addition, even when a spanning text does not have page break in it, such wrong placement may happen if the text is followed by \nobreak and thus a page break is made above the text but after the text is processed.

In version 1.3, this problem is solved by capturing the first half of a spanning text in \output routine for the page break in the text, and the second half or the whole of it in that for synchronized column-switching to close the text. Since an invocation of \output routine means that it has been fixed which page the spanning text or its part resides in, we can place the text much more reliably expecting the parity of the page number has also been fixed. In addition, this decision making in \output routine allows (or forces) us to let spanning texts always belong to column-0 preserving the consistency of, for example, local counter values referred to in them, while we need to shift a text to the left edge of the text area if it resides in an even numbered page. Furthermore, this spanning text capturing enables to measure the vertical size of the captured text together with the vertical position of its top edge to record them in the list $\pi^s(p)$, so that we draw column-separating rules skipping the text and painting its background with a specific color different from colors of columns and column-separating gaps, as discussed shortly.

Column-separating rule drawing to draw a vertical rule in column-separating gap is correlated with a part of background painting to paint each region in a page with a color specific to the region. Thanks to the list of spanning texts $\pi^s(p) = (span(H_i, h_i))_i^n$, we can draw column-separating rules skipping spanning texts in the page p as the sequence of;

$$rule(H'_1), gap(h_1), \dots, rule(H'_n), gap(H'_n), rule(H'_{n+1})$$

 $H'_i = H_i - (H_{i-1} + h_{i-1})$ $H_0 = h_0 = 0$ $H_{n+1} = \pi^h(p)$

where rule(H') is a vertical rule of H' high and gap(h) is a vertical space of h. A rule may be colored with the color specified by \colseprulecolor for each column-separating gap or all of them. Note that if column-swapping is in effect, a column c is preceded by c-th column-separating gap which may have its own width and color for its rule, rather than being followed by it.

Background painting also uses the list $\pi^s(p)$ to paint the background of each column-c with the color B_c^c , each column-separating gap following the column-c with B_g^c , and spanning texts with B_s and B_s , where $B_a^{[c]}$ is specified by the second argument of a[c] (color) ($a \in \{c, g, s, s\}$) and kept in the macro a[c] (or). The region to be painted for each item is as follows where a[c] means the region a[c] (x, y) a[c]

 $^{^{124}}$ Before version 1.3, we have $\mbox{\em Qmparbottom}$ in column-context because a column has its own area for marginal notes, which can be the gap between columns rather than a margin of a page.

 $[x_0, x_1), y \in [y_0, y_1)$ of the top-down xy-coordinate whose origin is at the left-top corner of the leftmost column.

$$\begin{split} R_c^c(i) &= \left[(W_c, \ H_{i-1} + h_{i-1}) \ (W_c + w_c, \ H_i + d_{c/g}) \right] \\ R_g^c(i) &= \left[(W_c + w_c, \ H_{i-1} + h_{i-1}) \ (W_{c+1}, \ H_i + d_{c/g}) \right] \\ R_{\{s,S\}}(i) &= \left[(0, \ H_i) \ (W_T, \ H_i + h_i + d_s) \right] \\ W_c &= \sum_{d=c_0}^{c-1} (w_c + g_c) \qquad c_0 = \begin{cases} 0 & c < C_L \\ C_L & c \ge C_L \end{cases} \quad W_T = \texttt{\textwidth} \\ d_{c/g} &= \begin{cases} \texttt{\text{maxdepth}} & i = n+1 \ \land \ H'_{n+1} > 0 \ \land \ \texttt{non-last page} \\ 0 & \texttt{otherwise} \end{cases} \\ d_s &= \begin{cases} H_{n+1} - (H_n + h_n) + \texttt{\text{\text{maxdepth}}} & i = n \ \land \ H'_{n+1} = 0 \ \land \ \texttt{non-last page} \\ 0 & \texttt{otherwise} \end{cases} \end{split}$$

In the specifications above, w_c and g_c is the width of the column c and that of the column-separating gap following it, defined by \columnratio or \setcolumnwidth and stored in \pcol@columnwidth c and \pcol@columnsep c respectively. The additions of $d_{c/g}$ and d_s are to extend the bottom edge of each region down to the bottom of text area. In addition, for each $R_a^{[c]} = [(x_0, y_0)(x_1, y_1)]$, extensions $e_a^{[c]}(\{x, y\}^{\pm})$ can be specified to shift the base points x_0, y_0, x_1 and y_1 left (x^-) , right (x^+) , upward (y^-) and downward (y^+) respectively. That is, a region is defined as;

$$R_a^{[c]} = [(x_0 - e_a^{[c]}(x^-), y_0 - e_a^{[c]}(y^-)) (x_1 + e_a^{[c]}(x^+), y_1 + e_a^{[c]}(y^+))]$$

with the optional shifts specified by the first argument of \backgroundcolor as $\{a[c](x^{\pm},y^{\pm})\}$ (for both x^-/y^- and x^+/y^+) or $\{a[c](x^-,y^-)(x^+,y^+)\}$ and kept in macros \pcol@bg@ext@ $d\cdot @\cdot a[\cdot @\cdot c]$ where $d\in \{1,\mathbf{r},\mathbf{t},\mathbf{b}\}$ for x^- (1), x^+ (r), y^- (t) and y^+ (b). Note that $e_a^{[c]}(\{x,y\}^{\pm})$ can be extremely large, namely greater than or equal to 9000pt, to mean the region is extended to a border near by the corresponding paper edge. More specifically, by this infinite extension, each xy coordinate in $[(x_0,y_0)(x_1,y_1)]$ is defined as follows to represent a coordinate being $10000\,\mathrm{pt}-e_a^{[c]}(\{x,y\}^{\pm})+\mathrm{pagerim}$ inside from the page edge;

$$\begin{split} x_0 &= -W_M + (10000\,\mathrm{pt} - e_a^{[c]}(x^-) + W_R) \\ y_0 &= -(H_S + H_M) + (10000\,\mathrm{pt} - e_a^{[c]}(y^-) + H_R) \\ x_1 &= (W_P - W_M) - (10000\,\mathrm{pt} - e_a^{[c]}(x^+) + W_R) \\ y_1 &= (H_P - H_S - H_M) - (10000\,\mathrm{pt} - e_a^{[c]}(y^+) + H_R) \\ W_P &= \mathrm{\paperwidth} \\ W_M &= \mathrm{\paperwidth} \\ W_M &= \mathrm{\paperwidth} \\ W_R &= H_R = \mathrm{\paperim} \\ H_P &= \mathrm{\paperheight} \\ H_M &= \mathrm{\paperheight} \\ H_M &= \mathrm{\paperheight} \\ H_M &= \mathrm{\paperheight} \\ H_S &= height(\pi^b(p)) + depth(\pi^b(p)) \end{split}$$

where f_{even} is true iff we are in an even numbered page and two-sided typesetting is specified by the optional argument of \documentclass or by the specifier 'p' of \twosided explicitly or implicitly.

Another remark is that column-swapping affects $R_c^c(i)$ and $R_s^c(i)$ to mirror the region making a reflection-symmetric transformation on it using a vertical edge of a page as the axis. That is, $[(x_0, y_0)(x_1, y_1)]$ for a region is transformed to $[(W_T - x_1, y_0)(W_T - x_0, y_1)]$ if $x_{\{0,1\}}$ is not extended infinitely. With infinite extension on the other hand, before this transformation x_0 and/or x_1 are calculated by the rule above replacing W_M with $W_P - (W_M + W_T)$ to represent the width of the right margin rather than the left.

On the other hand, the mirroring of $R_{\{s,S\}}$ is enabled by the specifier 'b' of \twosided, together with other regions being top margin (t,T), bottom margin (b,B), left margin (l,L), right margin (r,R), page-wise floats (f,F) and page-wise footnotes (n,N). The geometrical specifications R_a for those regions are given as follows, but the coordinate origin is at the top-left corner of text area (rather than the leftmost column).

$$\begin{split} R_{\{t,T\}} &= [(-W_M + W_R, \, -H_M + H_R), \, (W_P - W_M - W_R, \, 0)] \\ R_{\{b,B\}} &= [(-W_M + W_R, \, H_T - H_M), \, (W_P - W_M - W_R, \, H_P - H_M - H_R)] \\ R_{\{l,L\}} &= [(-W_M + W_R, \, 0), \, (0, H_T)] \\ R_{\{r,R\}} &= [(W_T, \, 0), \, (W_P - W_M - W_R, \, H_T)] \\ R_{\{f,F\}} &= [(0, \, 0), \, (W_T, \, H_S)] \\ R_{\{n,N\}} &= [(0, \, H_T - H_N) \, (W_T, \, H_T)] \\ H_T &= \text{\textheight} + \text{\tmaxdepth} \\ H_N &= \text{\textheight} + \text{\tmaxdepth} \end{split}$$

Note that, since we use text area coordinates, in the calculation of infinite extension H_S is let be 0.

We have other regions for columns and column-separating gaps, namely R_C^c and R_G^c , which vertically span all over text area regardless exsistance of any page-wise stuff. Therefore, their geometrical specifications are as follows with text area coordinates.

$$R_C^c = [(W_{c-1}, 0), (W_{c-1} + w_c, H_T)]$$

$$R_G^c = [(W_{c-1} + w_c, 0), (W_c, H_T)]$$

In addition, we have to paint pre-environment stuff and post-environment stuff with color $B_{\{p,P\}}$. The region $R_{\{p,P\}}$ for them is defined as follows with text area coordinates where H_B is the y-coordinate of the bottom of previous paracol environment if any, or 0 otherwise.

$$R_{\{p,P\}} = \begin{cases} [(0, H_B) (W_T, H_S)] & \text{pre-environment stuff} \\ [(0, H_B) (W_T, H_T)] & \text{post-environment stuff} \end{cases}$$

Note that paiting of post-environment stuff is done *outside* paracol environment when the post-environment stuff encounters a page break, unless another paracol environment starts in the page and thus the post-environment stuff becomes pre-environment stuff of the second (or subsequent) environment.

Finally, we define the order of background painting as follows, where a, a(i), a^c and $a^c(i)$ mean R_a , $R_a(i)$, R_a^c and $R_a^c(i)$ respectively, so that a succeding region is *overlaid* on preceding regions.

$$T \to B \to L \to R$$

$$\to G^0 \to \cdots \to G^{C-2} \to C^0 \to \cdots \to C^{C-1}$$

$$\to t \to b \to l \to r \to N \to n \to \{F, P\} \to \{f, p\}^{125}$$

$$\to S(1) \to \cdots \to S(n)$$

1.8 Page-wise Float Placement

In the release on 2015/01/10, LATEX's float placement mechanism was drastically changed to avoid out-of-order appearance of page-wise floats as follows. Since the cause of overtaking of a page-wise float by a column-wise float is that they are in two separated lists \@dbldeferlist for the former and \@deferlist for the latter, in the new implemenation the two lists are merged to let all floats go to \@deferlist. To distinguish page-wise and column-wise floats in the list, \end@dblfloat lets the page-wise float processed by the macro have a special depth of 1sp, while depth of column-wise floats are 0 since \@endfloatbox add a \vskip of 0 at the end of the box of floats.

Then all float placement macros invoked in \output-routine examine the depth of floats in the list they are working on against a newly introduced macro \f@depth by also newly introduced \@testwrongwidth, so that they process only floats of a page/column category specified by \f@depth, while those not matching to \f@depth are let go to \@deferlist to inhibit succeeding floats of the same type from overtaking them. The \definition of \f@depth is done only by modified \@dblfloatplacement, always invoked in a group, to let it have 1sp so that float placement macros usually work on column-wise ones with the default setting of \f@depth = \z@ except for special occasions in which the placement of page-wise floats is tried.

Though the mechanism should work well with ordinary multi-columned documents, it is incompatible with paracol almost inherently. That is, in the first place we have to separate float-related lists into the sets of them corresponding to columns as we do¹²⁶. Therefore, it is obviously nonsense to merge the list for page-wise floats, i.e., \@dbldeferlist, to \@deferlist of a particular column, and thus we have to stick with the conventional implementation to process page-wise and column-wise floats separately as follows.

- (1) We \define our own \end@dblfloat namely \pcol@end@dblfloat whose definition is exactly same as the old version of \end@dblfloat, and replace the new version with it by \letting them equivalent in \pcol@zparacol by which start paracol environments. Therefore, page-wise floats composed in a paracol environment is processed in the traditional way, i.e., being included in \@dbldeferlist rather than \@deferlist and having ordinary depth 0.
- (2) Each invocation of \@dblfloatplacement in our own \output-routine is followed by a \let to nullify the setting of \f@depth = 1sp done by \@dblfloatplacement by doing \f@depth=\z@. By this setting, \@tryfcolumn in \pcol@startpage and \@makefcolumn in \pcol@output@clear work on their argument \@dbldeferlist in the way exactly same as in 2014 or before.

¹²⁵In column flushing, the order is $\{F, P\} \to \{f, p\} \to N \to n$ but this reversion should have no effect (almost always).

¹²⁶ If counters figure and table are global and we have to avoid inter-column overtaking with respect to, for example, the partial ordering rooted by the top-left corner, merging column-wise lists together with the merge of \@deferlist and \@dbldeferlist might be a solution to let the depth of a column-wise float be c sp while that of page-wise is C sp. However such implementation is not only tough but also doubtful to be worthwhile.

- (3) Among LaTeX's macros in its \output-routine which we use in our own one as well, only \@addtodblcol changed its target from \@dbldeferlist to \@deferlist. That is, if the macro fails to put a page-wise float to the page we just have started by \pcol@startpage, the float is added to \@deferlist rather than \@dbldeferlist. Therefore, when we apply \@sdblcolelt to the copy of \@dbldeferlist to invoke \@addtodblcol for each of its element float, we have to save \@deferlist somewhere, to \reserved@c in reality, and clear it prior to the application. Then after all elements are processed, we have to let \@dbldeferlist have what \@deferlist have, while \@deferlist should regain its origial contents from the saved place. A subtle issue is that we might work with LaTeX of 2014 or older in which the floats are returned to \@dbldeferlist. Therefore to make paracol compatible with both of new and old versions, we have to add \@deferlist to \@dbldeferlist rather than replacing \@dbldeferlist with \@deferlist. This addition should work well, because we clear both lists before the application of \@sdblcolelt and then one of them will have the still-deferred floats after the application while the other remains empty.
- (4) We convert \@deferlist to \@dbldeferlist in \pcol@output@start to start a paracol environment, and perform the reverse operation in \pcol@output@end to close the environment. Though it is very unlikely (or maybe impossible) that the \@deferlist imported in the former operation has LATEX's (i.e., not paracol's) double-column floats of 1sp deep, we make such floats old-fashioned making their depth 0 so that they can be put in a page built in the paracol environment. On the other hand, the latter cannot export a list having floats of 1sp deep because they have been produced in the closing paracol environment or have passed our custom \pcol@output@start when they were imported 127.

Note that the operations (1), (2) and (4) are fully compatible with 2014 or older version of LATEX, because with the old version; (1) \pcol@end@dblfloat is equivalent to \end@dblfloat; (2) modification of \f@depth cannot be seen because it does not exist; and (4) we virtually do nothing in the importation. As for (3), we explicitly take care of the compatibility as shown above.

2 Interaction with TEX and LATEX

The macros of paracol interacts with TEX and LATEX through various registers and macros as discussed in this section.

2.1 Registers

2.1.1 Insertion Registers

\footins is used to \insert footnotes through it by \footnote and \footnotetext, and then in \output routine the footnotes \inserted in a page is presented in the register. The register is referred to by the following macros.

• \pcol@makecol examines if the register has page-wise footnotes and, if so, saves it into $\pi^f(p)$ if $p = p_t$ or discards it otherwise.

¹²⁷Therefore, if one try to *smuggle* a double-column float of the new scheme into a **paracol** and to pass it through the environment to another double-column world, the float will become a single-column one. Even if such guy a really exists and complains abount this transformation, however, we have good right to say "don't do that".

- \pcol@startcolumn \inserts $\pi^f(p)$ into the column-page to be created through the register.
- \pcol@specialoutput logs the contents of the register for debugging.
- \pcol@output@start examines if the register has footnotes to be merged with those in paracol environment, refers to its height plus depth to calculate effective \@colht, and/or \inserts its contents through itself to the main vertical list as the first part of merged footnotes.
- \pcol@makenormalcol combines footnotes in the register to other pre-environment stuff to make a spanning stuff, or makes save/restore of the register to/from \@tempboxa to exclude footnotes from spanning stuff when merged-footnote type-setting is specified.
- \pcol@output@switch saves the register into $\pi^f(p)$ or $\kappa_c(\tau)$, or discards its contents, when we leave from the column c with footnotes.
- \pcol@restartcolumn restores $\kappa_d(\tau)$ or $\pi^f(p)$ to the register and then \inserts the contents of \box\footins into itself so that it contributes to the main vertical list to be rebuilt for the column d.
- \pcol@getcurrfoot for column d lets the register have $\kappa_d(\tau)$.
- \pcol@savefootins saves the register into an \insert for $\pi^f(p)$ or $\kappa_c(\tau)$.
- \pcol@deferredfootins refers the \skip component of the register to have the vertical skip above page-wise footnotes and \inserts deferred footnotes through the register.
- \pcol@output@end \inserts $\pi^f(p)$ into the last page through the register.
- \pcol@fntexttop{text} \inserts the footnote $\langle text \rangle$ and a penalty through the register.
- \pcol@fntextbody{text} refers to the \skip component of the register to cap the height of the footnote $\langle text \rangle$.

\bx@A, ..., \bx@R have floats created by \@xfloat in the ordinary usage of fundamental LATEX of 2014 or earlier or that without the extension of e-TEX or its relatives. On the other hand, in LATEX of 2015 or later and with e-TEX or its relatives, the set is \bx@A, ..., \bx@Z, \bx@AA, ..., \bx@ZZ. In addtion to the use in LATEX, we use these registers for completed column-pages $s_c(p)$ (\pcol@opcol, \pcol@flushcolumn), main vertical list $\kappa_c(\beta)$ (\pcol@output@switch, \pcol@flushcolumn) and column-wise footnotes $\kappa_c(\tau)$ (\pcol@output@switch) in current column-pages, spanning stuff including pre-environment stuff $\pi^i(p)$ (\pcol@startpage, \pcol@output@switch) in pages, MVL-floats for main vertical lists in synchronized pages (\pcol@synccolumn), and page-wise floats deferred from paracol to post-environment stuff (\pcol@output@end).

2.1.2 Integer Registers

\deadcycles is TEX's primitive register to count the number of \output requests made between two \shipout operatios. It is zero-cleared by \pcol@invokeoutput because it can have a large number in a paracol environment.

\outputpenalty is TeX's primitive register to have the page-break penalty with which \output routine is invoked. It is referred to by \pcol@output to know whether it has special code

less than -10000, and by \pcol@specialoutput in detail for the dispatch according to the code. The register is also used for the communication from the latter, which lets it be -10000 for our own special \output routines, to the former to determine \vsize according to if the register has a value greater than -10004 or not.

\interlinepenalty is TeX's primitive register to have the page-break penalty inserted between two lines. The register is referred to in the following macros.

- \pcol@output@start to make pre-environment merged footnotes followed by this \penalty on the \insertion, and to insert it to start the first column-page allowing page-break before the start unless it is inhibited by \if@nobreak = true.
- \pcol@restartcolumn to insert this \penalty to resume a column-page allowing page-break if $\footnote{\mathsf{lf@nobreak}} = false$.
- \pcol@deferredfootins to let the second half of split Φ have this \penalty as the very first element.
- \pcol@fntexttop{text} to make the footnote $\langle text \rangle$ followed by this \penalty on the \insertion.
- \pcol@fntextother{text} to make the footnote $\langle text \rangle$ preceded by this \penalty in Φ .
- \pcol@fntextbody to let the register have \interfootnotelinepenalty.
- \floatingpenalty is TEX's primitive register to have the page-break penalty added to \insertpenalties if an \insert is moved to the page next to the page in which the line having the \insert resides. It is let have 20000 in \pcol@fntextbody for footnote typesetting.
- \vbadness is TEX's primitive register to have the threshold of the badness of \vbox construction with underfull messages. That is, if the badness exceeds the threshold on a \vbox construction, TEX will complain showing an underfull message. In \pcol@makenormalcol and \pcol@deferredfootins, the register is temporarily let have 10000 to avoid that \@makecol invoked in the former and \vsplit done in the latter causes the message with inevitable underfull.
- \showboxdepth is TeX's primitive register to determine the maximum depth of box structure to be shown in logging etc. The register is let have 10000 in \pcol@ShowBox for full logging.
- \showboxbreadth is TeX's primitive register to determine the maximum breadth of box structure to be shown in logging etc. The register is let have 10000 in \pcol@ShowBox for full logging.
- \interfootnotelinepenalty is an API \count register to have \interlinepenalty for footnotes. It is used in \pcol@fntextbody to let \interlinepenalty have it.
- **\@ne** is a **\chardef** register to have 1. The register is referred to by the following macros mainly for incrementing another register.

\pcol@F@count, \pcol@output, \pcol@opcol, \pcol@setpnoelt,
\pcol@nextpage, \pcol@nextpelt, \pcol@startpage, \pcol@checkshipped,
\pcol@outputelt, \pcol@ioutputelt, \@outputpage, \pcol@bg@paint@ii,
\pcol@output@start, \pcol@makenormalcol, \pcol@output@switch,

```
\pcol@setcurrcol, \pcol@iscancst, \pcol@addmarginpar,
\pcol@do@mpbout@i, \pcol@sync, \pcol@flushcolumn,
\pcol@measurecolumn, \pcol@synccolumn, \pcol@makeflushedpage,
\pcol@imakeflushedpage, \pcol@iflushfloats, \pcol@freshpage,
\pcol@output@end, \pcol@invokeoutput, \pcol@zparacol,
\pcol@setcolwidth@r, \pcol@setcolwidth@s, \pcol@setcw@scan,
\pcol@setcw@calcf, \pcol@synccounter, \pcol@com@syncallcounters,
\pcol@stepcounter, \pcol@com@switchcolumn, \pcol@sptext,
\pcol@visitallcols, \pcol@ifootnote, \pcol@ifootnotemark.
\pcol@swapcolumn, \pcol@set@color@push,
```

\two is a \chardef register to have 2. It is used in \pcol@setcurrcol to let $\kappa_c(\sigma) = 2$ when \if@nobreak = true but \if@afterindent = false, in \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to calculate $x \cdot 2^k$, $y/2^k$ and $(x/y) \cdot 2^k$ with various k, and in \pcol@swapcolumn to calculate $C^1 - (c' - C^0) - 2 = c - 1 = c^g$ for the column-separating gap ordinal c^g physically following the column c at the position c'.

\model{model} model is a \count register to have -1. It is used in the following macros.

- \pcol@setpnoelt, \pcol@nextpelt, \pcol@getpelt and \pcol@setmpbelt to decrement \@tempcnta which initially has $p p_b$ for a page p.
- \pcol@bg@paint@i to decrement C_b^1 by one locally to have the column scanning range $[C_b^0,C_b^1-1)$.
- \pcol@iscancst to decrement n_{pop} by one.
- \pcol@do@mpbout@i to let \@tempcnta have it to indicate left margin.
- \pcol@setcolwidth@r to calculate $C^1 C^0 1$.
- \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ in \@whilenum loops to calculate $z'/2^k$ and z'/2k-16 where $z'/2^k \approx x/y$.
- \pcol@iadjustfnctr to decrement \c@footnote.

\sixt@On is a \chardef register to have 16. It is used in \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to calculate $Z=z \times 1$ pt $=z' \cdot 2^{16-k}$ where $z'/2^k \approx x/y$.

\@m is a \mathchardef register to have 1000. It is used in \pcol@synccolumn and \pcol@ output@end to let \prevdepth = 1000pt on a synchronization or the closing paracol environment with an empty main vertical list, and in \pcol@setcw@getspec@i to add 1000pt to strech and shrink components of \@tempskipa having a column/gap sepcification to make it sure the skip register has those components.

\@M is a \mathchardef register to have 10000. It is used in the following macros

- \pcol@ShowBox to let \showboxdepth and \showboxbreadth have 10000 for full logging of a box.
- \bullet \pcol@output to examine if \outputpenalty <-10000 to mean a special \output request.
- \pcol@specialoutput to let \outputpenalty = -10000 to tell \pcol@output that the special \output request is our own.
- \pcol@makenormalcol and \pcol@deferredfootins to let \vbadness have 10000 temporarily to avoid underfull messages.

- \pcol@synccolumn to bias \pcol@textfloatsep by 10000 pt to indicate a column-page has an MVL-float and in \pcol@cflt and \pcol@addflhd to remove the bias.
- \pcol@switchcol and \pcol@flushclear to put \penalty-10000 for forced page break.
- \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to let $Z = z \times 1$ pt = 10000 pt if x/y is too large.
- \@Mii is a \mathchardef register to have 10002. It is used in \pcol@end@dblfloat to examine if \@floatpenalty = -10002 to mean the float environment to be closed is given in horizontal mode.
- \QMiv is a \mathchardef register to have 10004. It is used in \pcol@output to examine if \outputpenalty = -10004 for a dummy \output request made by IATEX's float-related macros and our \pcol@invokeoutput to ensure the real request is not eliminated when it is made at the very beginning of a page or a column-page. It is also used in \pcol@ specialoutput for footnote logging when \outputpenalty = -10004.
- \@MM is a \mathchardef register to have 20000. It is used in \pcol@fntextbody to let \floatingpenalty have it for footnote typesetting.
- \@beginparpenalty is a \count register to have the page-break penalty inserted before the first \item of each list-like environment. The penalty is determined in class files and is, for example, −\@lowpenalty = −51 with article.cls. It is referred to and inserted by \pcol@zparacol when it finds the paracol environment to start is at the very beginning of a list-like environment.
- \@floatpenalty is a \count register to have the penalty code -10002 or -10003 given by \@xfloat at the beginning of a float environment according to the environment is in horizontal or vertical mode respectively, or by \marginpar for a marginal note in the same meaning. It is referred to by \pcol@end@dblfloat to insert the penalty, and by \pcol@xympar to confirm \marginpar is error free.
- \@topnum is a \count register to have the maximum number of top floats which the current column-page can accept further. It is used in \pcol@setcurrcol and \pcol@igetcurrcol to save/restore it into/from $\kappa_c(\nu_t)$. The macro \pcol@synccolumn also lets \@topnum = 0 to inhibit top-float insertions in the current column-page any more after a synchronization.
- \@botnum is a \count register to have the maximum number of bottom floats which the current column-page can accept further. It is used in \pcol@setcurrcol and \pcol@ijgetcurrcol to save/restore it into/from $\kappa_c(\nu_b)$.
- \@colnum is a \count register to have the maximum total number of floats which the current column-page can accept further. It is used in \pcol@setcurrcol and \pcol@ijgetcurrcol to save/restore it into/from $\kappa_c(\nu_c)$.
- \col@number is a \count register to have the number of columns. It is let have 1 by \pcol@ zparacol and \pcol@sptext regardless the real number of columns C in order to keep \maketitle from putting the title by \twocolumn.
- \c@page is LaTeX's counter page being a \count register to have the page number. It is referred to by \pcol@setpnoelt, and \pcol@output@start to let $\pi^p(p) = page(p)$. The macro \pcol@startpage reload the register from $\pi^p(p_t-1)$ and then increment it by one

usually but two in non-paired parallel-paging, and repeat $\pi^p(p_t) = page(p_t)$ and incrementing page(p) for each float pages of page-wise floats. Reloading page(p) to the register from $\pi^p(p)$ is also done by \pcol@getpelt for macros using \pcol@getcurrpage, and by \pcol@outputelt, \pcol@sync and \pcol@makeflushedpage by \pcol@getcurrpinfo. Then the register is referred to by the following macros to exmine its parity.

- Our own \@outputpage to give page(p) or page(p) + 1 to \pcol@outputpage@1 and \pcol@outputpage@r which finally let the register have the value to be referred to by \pcol@outputpage being LATEX's \@outputpage.
- \pcol@bg@swappage to determine the values of \pcol@bg@leftmargin and \ifpcol@bg@@swap with other factors.
- \pcol@shiftspanning to decide the necessity of shifting spanning text left with column-swapping, examining raw \c@page at the \output request to close the spanning text rather than $\pi^p(p_t)$ which will have the correct value with respect to possible jump after the macro completes its work.
- \pcol@addmarginpar to determine the margin to which a marginal note goes.
- \pcol@do@mpbout@i to determine which of M_L^l or M_L^r is the target of the operation specified by \pcol@do@mpbout@elem.
- \pcol@swapcolumn $\langle c_1 \rangle \langle c_2 \rangle \langle C^0 \rangle \langle C^1 \rangle$ to determine c_2 for c_1 if column-swapping is in effect.

In addition, to do the parity examination in \pcol@bg@swappage above correctly, the macros \pcol@ioutputelt, \pcol@makeflushedpage, \pcol@imakeflushedpage, \pcol@iflushfloats and \pcol@output@end temporarily increment the register by one when they are working on a right non-paired parallel-page.

The other users are \ctr{ctr} to check $\langle ctr \rangle \neq page$, \ctr{ctr} to let $\ctr{cl} \cdot \theta = \ctr{cl} \cdot \theta = page$, and $\ctr{cl} \cdot \theta = page$, and \ctr{ctr} to write it to a log file as a part the logging information of memory leak debugging.

- \control is LaTeX's counter footnote being a \count register to have the footnote number. It is referred to by \pcolozparacol to let $b_f = \pcoloroval{Q} = \$
- $\colonormal{CO}.\theta$ is a \count register being LATEX's counter θ . It is referred to by \pcol@savectrelt to let $val_c(\theta) = val(\theta)$ for saving it in Θ_c , by \pcol@cmpctrelt to examine if $val_0(\theta) = val(\theta)$ to detect a modification outside paracol environment, and by \pcol@syncctrelt to let $val_c(\theta) = val(\theta)$ for all c for counter synchronization. It is also referred to by \pcol@ remctrelt and \localcounter to examine if $\theta = \text{page}$. The macros \pcol@setctrelt and \pcol@stpldelt restore the value of the counter from $val_c(\theta)$, while \pcol@stpclelt lets $val(\theta) = 0$ for zero-clearing of descendent counters.
- \count@ is a \count register for temporary use. It is used in \pcol@iscancst to have m of $\gamma_{i,m}$, \pcol@addmarginpar to have the physical column position of the current column c in which \marginpar is given, and in \pcol@extract@fil@i $\langle s \rangle$ \@nil to exact the unit of the stretch component s of a glue.

\@tempcnta is a \count register for temporary use. The usages of this register are as follows.

 \bullet In \pcol@F@count, it is used to measure the cardinality of \@freelist.

- In \pcol@makecol, it is used to keep $page(p_t)$ gotten by \pcol@getcurrpinfo until we store it back by \pcol@defcurrpage.
- In \pcol@setpageno, \pcol@setpnoelt, \pcol@nextpage, \pcol@nextpelt, \pcol@getcurrpage, \pcol@getpelt, \pcol@addmarginpar and \pcol@setmpbelt, it has p-q when we scan $\pi(q)$ for all $q \in [p_b, p_t]$ and the current column-page is at p.
- In \pcol@checkshipped, it has c when we scan S_c for all $c \in [0, C)$ to examine if all of them are not empty and thus we have pages to be shipped out.
- In \pcol@ioutputelt, it has c' when we scan $s_c(q)$ for all $c \in [0, C_L)$ or $c \in [C_L, C)$ to build the shipping out image of a page q, where c = c' or $c = C^1 1 (c' C^0)$ where $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$.
- In $\colon page(p)$ or page(p) + 1 to be given to $\colon page(0) + 1$ or $\colon page(0) + 1$ to be given to $\colon page(0) + 1$ or $\colon page(0) + 1$ to be given to $\colon page(0) + 1$ to $\colon page(0) + 1$ to be given to $\colon page(0) + 1$ to
- In \pcol@bg@columnleft, it has a value in $[C_b^0, c)$ to sum up the width of columns and column-separating gaps in the range.
- In \pcol@output@switch, it is used to have page(p) obtained by \pcol@getcurrp info and simply to store the value in $\pi^p(p)$ by \pcol@defcurrpage when we use these macros to add an element to $\pi^s(p)$ and/or let $\pi^f(p) = \text{footins}$.
- In \pcol@setcurrcol, it has the code calculated from \if@nobreak and \if@after indent to be saved in $\kappa_c(\sigma)$.
- In \pcol@scancst $\langle box \rangle$, it is let have $\langle box \rangle \in \{\pcol@colorins, \pcol@color stack@saved\} and then is referred to in \pcol@iscancst.$
- In $\pcol@addmarginpar$ besides the page scan shown above, it is used to scan all columns whose physical position is left from the current colum c to measure the distance between the left edges of the leftmost column and c.
- In $\protect{\protect}$ it has ± 1 according to the margin (left = -1) which marginal notes outside paracol environments goes to.
- In \pcol@flushcolumn, it is used to throw $page(p_t)$ away when we get it by \pcol@ getcurrpinfo because we don't need it.
- In \pcol@setcolwidth@r, it has c to scan fractions r_d where $d = c C^0$ in its argument $\langle ratio \rangle$ specified by \columnratio, and then to distribute the unspecified portion of \textwidth evenly to w_c for all $c \in [C^0+k+1,C^1)$, where k is the number of fractions and $(C^0,C^1) \in \{(0,C_L),(C_L,C)\}$.
- In \pcol@setcw@scan $\langle C^0 \rangle \langle C^1 \rangle \{spec\}$, it has c for two loops for $c \in [C^0, C^1)$ to add ',' to the tail of $\langle spec \rangle$ as many as $k = C^1 C^0$ and then to process first k elements in $\langle spec \rangle$, and is referred to by \pcol@setcw@set invoked in the second loop.
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, it used to calculate and to have k such that $z'/2^k \approx x/y$.
- In \pcol@cmpctrelt, it has $val(\theta)$ of a counter θ to be compared with $val_0(\theta)$.
- In $\pcol@com@switchcolumn$, it has $(c+1) \mod C$ being the target of column-switching.
- In \pcol@sptext, it temporarily has d being the target of column-switching during we let \pcol@nextcol have 0 to visit the leftmost column to put a spanning text.

- In \pcol@visitallcols, it has $d \in [0, C) \{c\}$ being the columns to be visited for column-scanning.
- In $\definecolumnpreamble{c}{pream}$, c is assigned to the register to ensure c is a number.
- In \pcol@calcfnctr, it has the footnote ordinal calculated by the macro to be referred to by the invokers \pcol@iadjustfnctr and \pcol@iifootnotetext.
- In \marginparthreshold{ t_l }[t_r] it is let have t_l , while in the related macro \pcol@marginparthreshold[t_r] it is let have t_r .

\Otempcntb is a **\count** register for temporary use. It is used in the following macros.

- In \pcol@ioutputelt it has c, while in \pcol@imakeflushedpage and \pcol@iflushfloats it has c', to have c = c' or $c = C^1 1 (c' C^0)$ according to column-swapping for c'-th iteration of column scanning loop for $c' \in [C^0, C^1)$, where $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$.
- In \pcol@scancst and \pcol@iscancst, it has n_{pop} .
- In \pcol@addmarginpar, it is let have the column number d whose phisical position is left from the current colum c to measure the distance between the left edges of the leftmost column and c.
- In $\protect\protec$
- In \pcol@setcolwidth@r, it has $C^1 C^0 1$ then $C^1 1$ and finally $C^1 \min(C^0 + k, C^1 1)$, where k is the number of fractions given in the argument of \columnratio and $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$.
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, at first it is used to calculate $z'/2^k \approx x/y$ and then to calculate $Z = z \times 1$ pt $= z' \cdot 2^{16-k}$.
- In \pcol@visitallcols, it has $c = \pcol@currcol$ to exclude it from the column-scan targets.

2.1.3 Dimension Registers

\vsize is TEX's primitive register to have the height of a page or a column-page being built.

It is let be \@colroom or \maxdimen by \pcol@output.

\hsize is TeX's primitive register to have the width of a page or a column-page being built. It is let be w_c by \pcol@invokeoutput to restart (or stay in) the column c, be \textwidth by \pcol@sptext for spanning text, and be either of \textwidth or w_c by \pcol@fntextbody according to the footnote typesetting being page-wise or column-wise respectively.

\maxdepth is TeX's primitive register to have the maximum depth of the page being built. In IFTeX, it is assumed that its value is fixed at \begin{document}, in which the value is saved into \@maxdepth, for the typesetting throughout the document, unless a bottom float is added to a page in which the register is let have 0 until it is shipped out. This temporary setting for a page with bottom floats has some reasonability but its implementation for paracol environments having column-switching from/to a column-page with bottom floats to/from another one without them is too costly¹²⁸. Therefore, we

¹²⁸ That is, we would need to incorporate \maxdepth as a member of column-context, but we don't because the idea of temporary setting itself is too vague to pay the effort and a precious membership in column-context.

let the register have $\mbox{\mbox{$\mathbb{Q}$}}$ in $\mbox{\mbox{$\mathbb{Q}$}}$ and $\mbox{\mbox{$\mathbb{Q}$}}$ builder and $\mbox{\mbox{$\mathbb{Q}$}}$ builder and $\mbox{\mbox{$\mathbb{Q}$}}$

\boxmaxdepth is T_EX 's primitive register to have the maximum depth of \vboxes. The macros \pcol@cflt, \pcol@opcol, \pcol@ioutputelt, \pcol@combinefloats, \pcol@output@flush and \pcol@output@clear let it be \@maxdepth for the boxes having a completed column-page or page to cap the depth of the box. The macro \pcol@@makecol\langle d\rangle also do that when $d = \ensuremath{\maxdepth}$ but it can be d = 0 when it is invoked to build last page.

\splitmaxdepth is T_EX 's primitive register to have the maximum depth of the \vbox being the first half of a box being split. It is used in \pcol@deferredfootins to cap the depth of the first half of deferred footnotes split from Φ , and in \pcol@fntextbody to let it have the depth of \strutbox.

\prevdepth is TEX's primitive register to have the depth of the box which just has been added to a vertical list, or to be given to TEX's vertical list builder for the calculation of the vertical skip inserted below the last box. The macro \pcol@invokeoutput refers to it to save its value in \pcol@prevdepth before putting a dummy \vbox and making a \output request, and then let it have \pcol@prevdepth which is given by \output routine for the column that we resume. The macro \pcol@zparacol also refers to it to save it in \pcol@ firstprevdepth for the pre-environment stuff.

\vfuzz is TeX's primitive register to have the threshold height of overfull messaging. It is set to 0 in \pcol@ShowBox $\langle b \rangle$ to ensure overfull for any \box b of non-null height.

\maxdimen is a \dimen register to have 16383.99999 pt being the largest legal dimensional value. The usages of this register are as follows.

- For the \insert register set \pcol@colorins = Γ_r , \dimen\pcol@colorins is let be \maxdimen for the consistency with our intention that a column-page can have virtually infinite number of \insertions for text coloring.
- In \pcol@output, it is set into \vsize when \outputpenalty = -10004 for the dummy \output request so that no page break should occur between the dummy and real requests.
- Our own \dimen register \pcol@textfloatsep has \maxdimen if a column-page does not have synchronization points to let top floats are inserted in usual way. Therefore, \pcol@floatplacement and \pcol@zparacol let the register have \maxdimen as the initial value. Then the macros \pcol@makecol and \pcol@combinefloats examine if \pcol@textfloatsep = \maxdimen to determine the operation type of top float insertion, while \pcol@synccolumn does that to know if it is flushing a column-page with a synchronization point or is setting the first synchronization point in the column-page. The macro \pcol@addflhd also examines it for the measurement of the combined height of top and bottom floats, while \pcol@measurecolumn gives it \maxdimen as its third argument for bottom floats.
- The page context $\pi^h(p)$ has $-\mbox{maxdimen}$ if the page is a float page. The macro $\mbox{pcol@startpage}$ makes that when it creates such a page.
- Our own \pcol@prevdepth and that saved in $\kappa_c(\delta)$ have \maxdimen if the main vertical list is empty at a synchronization. The macro \pcol@measurecolumn makes that when it finds an empty list.

- The column-context $\kappa_c(\rho_t)$ may have \maxdimen if the column c has a float column in the last page of a paracol environment and the floats in it can be put as top floats. The macro \pcol@makefcolumn makes this special assignment, and \pcol@flushcolumn and \pcol@imakeflushedpage examine it.
- The macro \pcol@makefcolelt let the room for floats in a float page be -\maxdimen if it finds no futher floats can be added to the page.
- At a synchronization, we measure the maximum combined size of top floats and the main vertical list V_T , that of footnotes and bottom floats V_B , that of four items V_P , and V_P' being V_P or $V_P + \text{textfloatsep}$ according to the existence of bottom floats. We also let D_T and D_P be the minimum depth of the column-pages which gives V_T and V_P' respectively. For the measurement, the macro pcol@sync lets $V_T = V_B = V_P = V_P' = -\text{maxdimen}$ and $D_T = D_P = \text{maxdimen}$ as their initial values. Then the macro pcol@synccolumn examines if $D_T = \text{maxdimen}$ to mean the synchronization point is set just below the top floats of a column whose main vertical list is empty. On the other hand, pcol@makeflushedpage and pcol@output@end examine if $V_P' = -\text{maxdimen}$ to mean the last column-pages are empty.
- \linewidth is a \dimen register for an API parameter of IATEX to have the width of a line possibly shorter than \columnwidth in list-like environments. It is let have $w_c \mu$ by \pcol@invokeoutput for the outermost paragraphs in paracol environment, where $\mu = \pcol@Irmargin = \textwidth l$ which \pcol@zparacol lets have to represent the left-plus-right margin of the list-like environment, whose \linewidth is l, enclosing paracol if any. The macro \pcol@sptext also sets the register temporarily for spanning texts but letting it have \textwidth μ .
- \footnotesep is a \dimen register for an API parameter of LATEX to have the vertical space inserted in a footnote when it is split into two or more pages. It is uesed in \pcol@ fntextbody to \splittopskip have it, and to make the first line of the footnote is at least as tall as the amount in the register.
- \topmargin is a \dimen register for an API parameter of IATEX to have the width (height) of the top margin minus 1 inch. The register is used as an element of \pcol@bg@pagetop to calculate the distance from the origin at the left-top corner of text area to the top edge of a page. The other users are \pcol@ioutputelt and \pcol@makeflushedpage temporarily add the height-plus-depth of $\pi^b(p)$ to the register to make the calculation biased shifting the origin to the left-top corner of column area, i.e., below $\pi^b(p)$. The macro \@outputpage also refers to the register together with \headheight and \headsep to calculate the distance from the page top (ingoring 1 inch shift) to the text area top.
- \oddsidemargin is a \dimen register for an API parameter of LATEX to have the width of the left margin minus 1 inch for two-sided odd-numbered pages and all single-sided pages. The register is used together with \evensidemargin in \pcol@outputpage@1, \pcol@outputpage@1, \pcol@outputpage@r and \pcol@bg@swappage to decide the left margin of the page they are working on.
- \evensidemargin is a \dimen register for an API parameter of LATEX to have the width of the left margin minus 1 inch for two-sided even-numbered pages. The register is used together with \oddsidemargin in \pcol@outputpage@1, \pcol@outputpage@r and \pcol@bg@ swappage to decide the left margin of the page they are working on.
- \headheight is a \dimen register for an API parameter of IATEX to have the height of page headers. The register is used together with \topmargin and \headsep as an element

- of \pcol@bg@pagetop and in \@outputpage to calculate the distance from the real and imaginary page top to the text area top respectively.
- \headsep is a \dimen register for an API parameter of LATEX to have the vertical distance from the bottom of a page header to the text area top. The register is used together with \topmargin and \headheight as an element of \pcol@bg@pagetop and in \@outputpage to calculate the distance from the real and imaginary page top to the text area top respectively.
- \textheight is a \dimen register for an API parameter of IATEX to have the height of text area in a page. The register is referred to by \pcol@output to examine if a page is very short, by \pcol@getpinfo, \pcol@startpage, \pcol@flushfloats and \pcol@output@ end to let \@colht be it for a page without spanning stuff (so far), by \pcol@outputelt, \@outputpage, \pcol@output@flush and \pcol@output@clear to build a page to be shipped out, by \pcol@be@textheight to calculate H_T , and by \pcol@fntextbody to cap the height of a footnote.
- \textwidth is a \dimen register for an API parameter of LATEX to have the width of a page, which we occasionally refer to as W_T . The register is referred to by \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to build a \hbox of \textwidth wide to have all columns (in a left or right parallel-page). It also referred to by following macros; \pcol@bg@swappage to calculate the right margin for mirrored background painting; \pcol@bg@@r, \pcol@bg@@r, \pcol@bg@@n, \pcol@bg@@p and \pcol@bg@@s to specify the width of background of page-wise stuff to be painted; \pcol@shiftspanning to calculate the left-shift amount of a spanning text in column-swapping; \pcol@addmarginpar to measure the distance between the right edges of the rightmost and current columns; \pcol@zparacol for the calculation of $\mu = \text{pcol@lrmargin}$; \pcol@setcolwidth@r for the calculation of w_c for all $c \in [0, C_L)$ or $c \in [C_L, C)$; \pcol@setcw@calcfactors for the calculation of W_T/W and $(W_T W)/F$; \pcol@sptext, \footnoterule of paracol's local and \endparacol to set it in \columnwidth; and \pcol@fntextbody to set it in \hsize if page-wise footnote typesetting is in effect.
- \columnwidth is a \dimen register for an API parameter of LaTeX to have the width of a column. The register is let have w_c by \pcol@getcurrcol for the column c, then is referred to by the following macros; \pcol@shiftspanning to calculate the left-shift amount of a spanning text in column-swapping; \pcol@addmarginpar to measure the distance between the right edges of the rightmost and current columns; \pcol@imakeflushedpage and \pcol@iflushfloats to put each column-page into a \hbox of w_c wide for shipping a page out; \pcol@invokeoutput to let \linewidth and \hsize have the value of or based on it; and \pcol@fntextbody to let \hsize have it for column-wise footnote typesetting. The register is also let have \textwidth by \footnoterule of paracol's local defined in \pcol@zparacol if page-wise footnote typesetting is in effect, by \pcol@sptext for spanning texts, and by \endparacol for post-environment stuff.
- \columnsep is a \dimen register for an API parameter of IATEX to have the width of column-separating gaps. It is referred to by \pcol@setcolwidth@r to calculate w_c for all $c \in [0, C_L)$ or $c \in [C_L, C)$, and by \pcol@setcw@getspec as the default width of column-separating gaps.
- \columnseprule is a \dimen register for an API parameter of LATEX to have the width of the rules to be drawn in column-separating gaps. It is referred to by \pcol@buildcolseprule and \pcol@buildcselt to draw the rule, and by \pcol@hfil to examine if it is positive

- to mean the rule is really drawn and if so to add skips of $-\columnseprule/2$ to surround the rule to nullify the width of the rule.
- \marginparwidth is a \dimen register for an API parameter of LATEX to have the width of a marginal note. It is temporarily modified by \pcol@addmarginpar so that a left marginal note is placed appropriately.
- \marginparsep is a \dimen register for an API parameter of LATEX to have the distance between a marginal note and text area. It is temporarily modified by \pcol@addmarginpar so that a right marginal note is placed appropriately.
- \marginparpush is a \dimen register for an API parameter of LaTeX to have the minimum vertical distance between two marginal notes. It is referred to by \pcol@addmarginpar to find a place for a marginal note and remember the place in $\pi^m(p)$.
- \paperheight is a \dimen register for an API parameter of LATEX to have the height of physical pages H_P . It is referred to by \pcol@bg@paperheight to calculate $H_P 2W_R$.
- \paperwidth is a \dimen register for an API parameter of LATEX to have the width of physical pages W_P . It is referred to by \pcol@bg@swappage to calculate the right margin for mirrored background painting, and by \pcol@bg@paperwidth to calculate $W_P 2W_R$.
- \z@ is a \dimen register to have 0pt to initialize \pagerim, \belowfootnoteskip and \skip\pcol@colorins at their declarations, and is used in the following macros.

\pcol@ShowBox, \pcol@makecol, \pcol@combinefloats, \pcol@nextpelt, \pcol@floatplacement, \pcol@startpage, \pcol@restartcolumn, \pcol@outputelt, \pcol@buildcolseprule, \pcol@buildcselt@S, \pcol@buildcselt, \@outputpage, \pcol@startcolumn, \pcol@bg@paint@i, \pcol@bg@paintregion, \pcol@output@start, \pcol@putbackmvl, \pcol@iscancst, \pcol@deferredfootins, \pcol@combinefootins, \pcol@addmarginpar, \pcol@getmparbottom, \pcol@sync, \pcol@measurecolumn, \pcol@synccolumn, \pcol@sync, \pcol@measurecolumn, \pcol@synccolumn, \pcol@invokeoutput, \pcol@setcolwidth@s, \pcol@output@end, \pcol@invokeoutput, \pcol@setcolwidth@s, \pcol@setcw@calcfactors, \pcol@setcw@calcf, \pcol@extract@fil@ii, \pcol@sptext, \pcol@fntextbody. \pcol@marginpar, \pcol@icolumncolor, \pcol@set@color@push, \pcol@reset@color@pop, \pcol@reset@color@ii.

It is also used to give the number 0 for the initializations of \pcol@currcol, \pcol@ncol, \pcol@ncolleft and \count\pcol@colorins at their declarations, and in the following macros.

\pcol@ShowBox, \pcol@F@count, \pcol@makecol, \pcol@opcol,
\pcol@setpnoelt, \pcol@nextpelt, \pcol@checkshipped, \pcol@getpelt,
\pcol@outputelt, \pcol@ioutputelt, \@outputpage, \pcol@startcolumn,
\pcol@output@start, \pcol@output@switch, \pcol@setcurrcol,
\pcol@iscancst, \pcol@addmarginpar, \pcol@setmpbelt,
\pcol@do@mpbout@i, \pcol@sync, \pcol@synccolumn,
\pcol@makeflushedpage, \pcol@imakeflushedpage, \pcol@flushfloats,
\pcol@iflushfloats, \pcol@freshpage, \pcol@output@end,
\pcol@zparacol, \pcol@setcolwidth@r, \pcol@setcw@calcf,

\pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter, \pcol@stpclelt, \pcol@com@switchcolumn, \pcol@switchcolumn, \pcol@switchcolumn, \pcol@syncallcols, \pcol@xympar, \endparacol.

- \p@ is a \dimen register to have 1 pt. It is used in \pcol@ShowBox, \pcol@cflt, \pcol@addflhd, \pcol@synccolumn, \pcol@output@end, \pcol@setcolwidth@s, \pcol@setcw@getspec@i, \pcol@setcw@fill and \pcol@setcw@calcf, and the top level assignment to \@tempskipa for the invocation of \pcol@defkw, as the shorthand of pt.
- \@totalleftmargin is a \dimen register to have the total size of the left margins of a list-like environment and those surrounding it. It is given to \parshape by \pcol@invokeoutput and \pcol@sptext if paracol is enclosed in a list-like environment.
- \@themargin is a control sequence \let-equal to \evensidemargin for two-sided even numbered pages or \oddsidemargin for others. In \pcol@outputpage@l and \pcol@outputpage@r it is bound to one of \dimen registers for the references in \pcol@outputpage@ev¹²⁹.
- \@maxdepth is a \dimen register to have \maxdepth at \begin{document} to recover the temporary update of \maxdepth with 0 by \@addtobot for bottom float incorporation in a page. As discussed in the explanation of \maxdepth, in paracol environments \maxdepth is let have \Omaxdepth always by the assignments in \pcol0 output and \pcol@combinefloats. Other users, \pcol@cflt, \pcol@opcol, \pcol@ ioutputelt, \pcol@combinefootins, \pcol@output@flush and \pcol@output@clear, let \boxmaxdepth have \@maxdepth so as to limit the depth of boxes for a completed column-page or page to the value for page typesetting, while \pcol@flushcolumn and \pcol@imakeflushedpage do that by \pcol@makecol giving the register to it. The other usage of the register is to calculate background painting parameter H_T by **\pcol0** bg@textheight, and to determine the bottom edge of the backgrounds of columns and column-separating gaps through the argument of \pcol@buildcolseprule given by \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats. The register is also referred to by \pcol@unvbox@cclv to go back the last baseline of the main vertical list in \box255, and by \pcol@deferredfootins to let \splitmaxdepth have its value to cap the depth of the first half of footnotes split from Φ .

\@colht is a \dimen register to have the height of columns in a page possibly shrunk from \textheight by spanning stuff. The usages of the register are as follows.

- In \pcol@startpage, \pcol@output@start, \pcol@flushfloats and \pcol@output@end, it is initialized to \textheight. In first two, the value of the register is reduced to reflect spanning stuff if exists and then set into $\pi^h(p)$, while the setting by the third is referred to by its callee \pcol@iflushfloats.
- In \pcol@getpelt, \pcol@sync, \pcol@flushcolumn, \pcol@makeflushedpage and \pcol@imakeflushedpage, it is let have $\pi^h(p)$. In addition \pcol@sync examines if \@colht $< V_T + V_B + v(f)$, and \pcol@makefcolumn uses it to initialize the room of a float column as well as the height of $\kappa_c(\beta)$ for it.
- In \pcol@opcol, it is used to add \pcol@clearcolorstack to the bottom of $\kappa_c(\beta)$ whose height is \@colht.

¹²⁹The reference in \pcol@outputpage being IATEX's \@outputpage is done after the macro itself makes the assignment, which is of course consistent with those in our macros.

- In \pcol@startcolumn(*), \pcol@flushcolumn(*) and \pcol@freshpage, it is used to let \@colroom have it.
- In \pcol@restartcolumn(*), it is saved and restored for the use as the height cap of deferred footnote \insertion in \pcol@deferredfootins because it can be shrunk by the non-deferred page-wise footnotes.
- In \pcol@output@flush and \pcol@output@clear, it is given to \pcol@make flushedpage as its argument. The macro \pcol@makeflushedpage(*) lets \@colht be the argument if it is less than \@colht and thus is given by \pcol@output@end.

In addition, in the macros with '(*)' above and \pcol@makecol, the register is passed to \pcol@shrinkcolbyfn to shrink the height in it temporarily to keep the space required to put page-wise footnotes in the page they are working on, for the reference by starred macros themselves or \@makecol invoked in \pcol@makecol.

\@colroom is a \dimen register to have the height of a column possibly shrunk from \@colht by top and bottom floats. The register is initialized to have \@colht by \pcol@ startcolumn, \pcol@output@start, \pcol@flushcolumn and \pcol@freshpage, the last three of which also save it into $\kappa_c(\beta^r)$. This save operation is also done by \pcol@ output@switch while restoring from it done by \pcol@restartcolumn, but the latter macro may shrink the amount in its callee \pcol@putbackmvl to capture a spanning text while the former cancel this shrinkage. The macros \pcol@output and \pcol@output@ start also refer to this register to let \vsize have it in the former and to calculate the room for each column-page in the starting page in the latter. The macro \pcol@ output@end lets the register have \textheight for the post-environment stuff because the column-pages above it simply precedes the stuff in the main vertical list. The other users \pcol@makefcolumn and \pcol@makefcolelt use this register to accumulate the total size of floats to be put in a float column temporarily.

\@pageht is a \dimen register to be used in IATEX's \@specialoutput to have the height of \@holdpg. It is referred to by \pcol@addmarginpar to deteremine the position at which a marginal note is placed. We also use it as a scratchpad to have V_P in \pcol@sync and \pcol@measurecolumn, and to save $\pi^h(p_t)$ in \pcol@flushcolumn for the reference in itself, and to do so in \pcol@makeflushedpage for \pcol@imakeflushedpage.

\@pagedp is a \dimen register to be used in LATEX's \@specialoutput to have the depth of \@holdpg. However, we use it as a scratchpad in \pcol@sync and \pcol@measurecolumn to have D_P , and in \pcol@output@end to have the value to be set in \pcol@prevdepth.

\Quantum top floats. The register is saved in $\kappa_c(\rho_t)$ by \pcol@setcurrcol and restored from it by \pcol@iigetcurrcol. The macro \pcol@makefcolumn uses this register as a flag to indicate that $\kappa_c(\lambda_t)$ of the column c having $\kappa_c(\rho_t) = \infty$ contains floats to be put in its last float column possibly as top floats so that it is examined by \pcol@flushcolumn and \pcol@imakeflushedpage, the former of which then lets $\kappa_c(\rho_t) = 0$ to mean the floats are put in a float column in a non-last page by the macro.

\@botroom is a \dimen register to have the room for bottom floats. The register is saved in $\kappa_c(\rho_b)$ by \pcol@setcurrcol and restored from it by \pcol@ijgetcurrcol.

\@fpmin is a \dimen register to have \floatpagefraction \ \@colht being the minimum total size of floats for which an ordinary (not flushed) float column can be build. It is referred

to by \pcol@makefcolumn as the threshhold below which floats in the last float column can be put as top floats.

\@mparbottom is a \dimen register to have the bottom position of the last \marginpar stuff. Its value at \begin{paracol} is referred to by \pcol@output@start to let M_L^l or M_L^r of $\pi^m(0)$ has an element based on it, while the tail of one of the lists in $\pi^m(p_t)$ defines the value at \end{paracol} which \pcol@output@end lets the register have. The register is also updated by \pcol@getmparbottom and \pcol@getmpbelt to let \pcol@@addmarginpar being IATeX's original \@addmarginpar know the uppermost available position for the marginal note to be added. This update is, however, just for communication betwee these macros and thus is ineffective for typesetting posterior to that, as well as the update in \pcol@addmarginpar, because whole information for marginal note placement is kept in $\pi^m(p)$ in Π^+ .

\@textfloatsheight is a \dimen register to have the combined height of mid floats and their separators. It is initialize to be 0 by \pcol@floatplacement, saved in $\kappa_c(\eta)$ by \pcol@ setcurrcol, and restored from it by \pcol@ijgetcurrcol.

\dimen@ is a \dimen register for temporary use. It is used in the following macros.

- \pcol@buildcolseprule, \pcol@buildcselt@S and \pcol@buildcselt to have the argument $d \in \{\mbox{\colored} buildcselt, 0\}$ of the first macro.
- \pcol@bg@paintregion@i to have y_1 of $R_a^{[c]}$.
- \pcol@bias@mpbout@i $\{y\}\{t\}\{b\}$ to have t and then t+y.
- \pcol@output@switch to have the height of pre-spanning-text stuff in \pcol@ prespan, or 0 if it is \bot .
- \pcol@sync to have V or $V D_T + V_E$.
- \pcol@addflhd and \pcol@hdflelt to measure the height of top and bottom floats, \pcol@makecol and \pcol@output@switch to measure the height of pre-spanning-text stuff including the top floats, and \pcol@measurecolumn for top and bottom floats and V_T , V_B and V_P .
- \pcol@setcolwidth@s and \pcol@setcw@accumwd to accumulate W being the sum of natural widths of column/gap specifications, and then used by \pcol@setcw@calcfactors to calculate W/W_T and $W-W_T$.

\dimen@ii is a \dimen register for temporary use. It is used in the following macros.

- \pcol@makecol to measure the total height of top floats by \pcol@addflhd.
- \pcol@bg@addext to have $e = \text{pcol@bg@ext@} \cdot d \cdot @ \cdot \{a \cdot @ \cdot c, a\}$ and then $10000 \, \text{pt} e$ to calculate an extension of background painting.
- \pcol@bias@mpbout@i $\{y\}\{t\}\{b\}$ to have b and then b+y.
- \pcol@measurecolumn to measure V_T , V_P and D_P .
- \pcol@setcolwidth@s and \pcol@setcw@accumwd to accumulate F being the sum of infinite stretch factors in column/gap specifications with the unit of pt, and then used by \pcol@setcw@calcfactors to calculate $(W-W_T)/F$, where W is the sum of natural widths.
- \pcol@setcw@calcfactors to have $(W-W_T)/F$ above or 0 to be used in \pcol@def@extract@fil@iii through \pcol@setcw@filunit made \let-equal to the register by \pcol@setcolwidth@s.

\@tempdima is a \dimen register for temporary use. The usages of this register are as follows.

- In \pcol@makecol and \pcol@startpage, it is used to throw $\pi^h(p_t)$ away when we get it by \pcol@getcurrpinfo because we don't need it.
- In \pcol@outputelt, it has $\pi^h(p)$ to examine if p is a float page.
- In \pcol@ioutputelt, it has $\pi^h(p)$ possibly shrunk by page-wise footnotes to know the backgrounds to be painted for columns etc. After that it has w_c being the width of each \hbox into which the column-page of each column c is put.
- In \pcol@buildcolseprule and its callees \pcol@buildcselt@S and \pcol@buildcselt, the register has the first argment $H = \pi^h(p)$ of the caller macro.
- In \pcol@hfil $\langle c \rangle$, it has $g_c = \text{\col@columnsep} \cdot c$.
- In \Coutputpage, it has the sum of \topmargin, \headheight and \headsep being the distance between tops of imaginary page and its text area.
- In \pcol@startcolumn, it is used to save \@colht which can be shrunk temporarily by page-wise footnotes.
- In \pcol@bg@paintregion@i, it is let have x_0 of $R_a^{[c]}$.
- In \pcol@output@start, it is used to have the room for each column-page in the starting page, and then the height-plus-depth of the pre-environment stuff.
- In \pcol@output@switch, it is used to throw $\pi^h(p)$ away when we get it by \pcol@ getcurrpinfo because we don't need it.
- In \pcol@shiftspanning, it is let have the left-shift amount of a spanning text in column-swapping.
- In \pcol@restartcolumn, it is used to save \@colht which can be shrunk temporarily by page-wise footnotes.
- In $\pcol@unvbox@cclv(ins)$, it has the depth of $\bcox255$ for going back to the baseline of the box, and then has the natural component of $\scalebox{skip}(ins)$ to add its stretch and shrink components only.
- In \pcol@addmarginpar, at first it has the distance between left edges of the leftmost and current columns. Then it is let have the distance between top edges of the column and the marginal text to be put.
- In \pcol@getmparbottom $\langle t \rangle \langle h \rangle$ and \pcol@getmpbelt $\langle t_i \rangle \langle b_i \rangle$, it at first has t and then is let have b_i when the marginal note cannot be put at t.
- In \prolesync , \prolesync denotes and \prolesync denotes the maximum combined height of top floats and the main vertical list.
- In \pcol@makefcolumn and \pcol@makefcolelt, it has the room for floats to be put in a float column.
- In \pcol@makeflushedpage, it has the height-plus-depth of spanning stuffin $\pi^i(p_t)$.
- In \pcol@output@end, at first it is let have $V_P' H$, where H is the height(-plusdepth) of \@outputbox having the ship-out image of the last page, being the negative counterpart of the height-plus-depth of spanning stuff in the last page for setting \mathcal{M} , and then have H to be set in \pcol@bg@preposttop for the background painting of post-environment stuff.
- In \pcol@setcolwidth@r, it has \textwidth $-(C^1-C^0-1)$ \columnsep being the base of w_c .

- In \pcol@setcw@getspec@i, it is let have the natural width of a column/gap specification, to be used in \pcol@setcolwidth@s, \pcol@setcw@accumwd and \pcol@setcw@set, while in the last of them it finally has w_c or g_c .
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, at first it has y, then $y/2^{k_2}$, and then $\lceil y/2^{k_2+k_3} \rceil$, where k_2 and k_3 are scaling parameters for good approximation.
- In \pcol@switchcol, it is let have what \pcol@ensurevspace has so that the dimensional expression in it is evaluated in the macro and the evaluateion result is assigned to $V_E = \pcol@ensurevspace$.
- In \ensurevspace{space}, it is let have $\langle space \rangle$ to ensure the argument is a dimension including forced one.
- In \pcol@fntextbody, it has the height-plus-depth of the \vbox in which the footnote is encapsulated.
- In \pcol@set@color@push, it has the width of the \vbox to be \inserted, which is m sp for a math-mode push of $\gamma_{i,m}$ or 0 for a non-math one γ_i .
- In $\pcol@bg@defext{d}{e}$, it is let have e to confirm e is a proper dimension.

\@tempdimb is a \dimen register for temporary use. The usages of this register are as follows.

- In \pcol@makecol, it is used to measure the height-plus-depth h_i of decapsulated \box255 and its original form to add an element $span(H_i, h_i)$ to $\pi^s(p_t)$ for a spanning text captured in the box.
- In \pcol@ioutputelt, if has the height-plus-depth of spanning stuff $\pi^b(q)$ to be temporarily added to \topmargin.
- In \pcol@buildcolseprule it has $H_0 + h_0$, while in its callee \pcol@buildcselt $\langle H_i \rangle$ $\langle h_i \rangle$ it has $H_{i-1} + h_{i-1}$ and then $H_i + h_i$ where $span(H_i, h_i) \in \pi^s(p)$.
- In \pcol@bg@paintregion@i, it is let have y_0 of $R_a^{[c]}$.
- In \pcol@output@switch, it is let have the height-plus-depth h_i of \@holdpg having a spanning text to add an element $span(H_i, h_i)$ to $\pi^s(p_t)$.
- In \pcol@shrinkcolbyfn, it is let have the inverse of the \skip component of the argument \insert register of the macro, so that in \pcol@startcolumn and \pcol@restartcolumn it has that of $\pi^f(p)$ if p has page-wise footnotes, or 0 otherwise, and then is referred to by \pcol@deferredfootins which then lets the register have the height cap of Φ splitting.
- In \pcol@addmarginpar, \pcol@getmparbottom and \pcol@getmpbelt, it is let have the vertical space to be occupied by the marginal text to be put, being the second argument of \pcol@getmparbottom.
- In \pcol@sync and \pcol@measurecolumn, it has V_B and then, in the former, it has $V_P + v(f)$, V_T or $V_T + V_B + v(f)$ according to the contents of the page to be synchronized.
- In \pcol@makefcolelt, it has the size of vertical space consumed by a float.
- In \pcol@synccolumn, it has $V_T v_c(t)$ being the vertical space from the bottom of $\kappa_c(\beta^b)$ to the synchronization point. If the synchronization point is defined by a column without main vertical list but with top floats, then the register is let have $V_T v_c(t) + \text{textfloatsep} \text{floatsep} + 10000\,\text{pt}$ to be set in $\kappa_c(\xi) = \text{pcol@textfloatsep}$ as the space below the MVL-float biased by 10000 pt to indicate the last float is the MVL-float.

- In \pcol@setcolwidth@r, it has \textwidth $-(C^1-C^0-1)$ \columnsep $-\sum_{d=0}^{k-1} w_d$ being the base of w_c for $c \in [C^0+k, C^1)$ where k is the number of fractions given in the argument of \columnatio.
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, at first it is let have x, then $x \cdot 2^{k_1}$, then $z' = \lfloor (x \cdot 2^{k_1})/\lceil y/2^{k_2+k_3} \rceil \rfloor$, and finally $Z = z \times 1$ pt $= z' \cdot 2^{16-k}$ referred to by \pcol@setcw@calcfactors as $\phi_f = (W_T W)/F$, where k_1 , k_2 and k_3 are scaling parameters for good approximation and $k = k_1 + k_2 + k_3$.
- In \pcol@extract@fil@ii and \pcol@extract@fil@iii, it is let have the infinite stretch factor of a column/gap specification represented with the unit \pcol@setcw@filunit, to be used in \pcol@setcolwidth@s, \pcol@setcw@accumwd, and \pcol@setcw@set.
- In \pcol@fntextbody, it has \textheight \skip\footins as the cap of the footnote

\@tempdimc is a \dimen register for temporary use. It is let have values as follows.

- $H_i (H_{i-1} + h_{i-1})$ in \pcol@buildcselt $\langle H_i \rangle \langle h_i \rangle$.
- x_1 of $R_a^{[c]}$ in \pcol@bg@paintregion@i.
- t + h in \pcol@getmparbottom $\langle t \rangle \langle h \rangle$.
- $\max(t, b_{i-1}) + h$ in \pcol@getmpbelt $\langle t_i \rangle \langle b_i \rangle$ invoked from \pcol@getmparbottom $\langle t \rangle \langle h \rangle$.
- D_T in \pcol@sync, \pcol@measurecolumn and \pcol@synccolumn.
- \floatsep or \@fpsep in \pcol@makefcolumn and \pcol@makefcolelt.
- w_c being the width of column c in \pcol@setcolwidth@r.
- ullet W_T-W in \pcol@setcw@calcfactors.
- At first for calculation of $y/2^{k_2}$ and then $z'/2^k \approx x/y$ in \pcol@setcw@calcf $\langle x \rangle \langle y \rangle$ $\langle z \rangle$ where k_2 and k are scaling parameters for good approximation.

2.1.4 Skip Registers

\baselineskip is TEX's primitive register to have the vertical skip to separate adjacent baselines. It is referred to by \pcol@output and \pcol@output@start to examine if \@colroom is unexpectedly small, and by \pcol@switchcol to give it to \ensurevspace to let \pcol@ensurevspace have the default value.

\topskip is TeX's primitive register to have the vertical skip from the top edge of a page to the baseline of its first vertical item. It is let be 0 by \pcol@output@start if we have pre-environment stuff and is saved in $\pi^t(0)$, while \pcol@startpage lets it be \pcol@topskip, into which \pcol@zparacol saves the value outside paracol environment, saving the value in $\pi^t(p)$. Then the register is restored from $\pi^t(p)$ by \pcol@getpelt and \pcol@sync, while \pcol@synccolumn refers to the value restored by the latter to adjust a synchronization point. The macro \pcol@putbackmvl lets the register have 0 when it starts a spanning text because it originally follows pre-spanning-text stuff in the column-page to be restarted rather than at the page top. The macro \pcol@output@end temporarily lets the register have 0 if we have non-empty columns in the last page, while \endparacol restores it from \pcol@topskip for the pages outside paracol environment.

- \splittopskip is T_EX 's primitive register to have the vertical skip inserted at the beginning of the second half of the box split by \vsplit or T_EX 's internal operation for splitting an \insert at a page break. The register is temporarily let have 0 by \pcol@ deferredfootins when it splits Φ so that the second half does not have any skip at the top. The register is also let have \footnotesep in \pcol@fntextbody for footnote typesetting.
- \parskip is TEX's primitive register to have the vertical skip inserted above each paragraph. It is referred to by \pcol@zparacol to nullify the insertion going to be made by the first \item of a list-like environment, when the macro finds the paracol environment to start is at the very beginning of a list-like environment.
- \fill is an API \skip register to have a skip 0pt plus 1fill. In our macros, however, it is used as a keyword in \pcol@setcw@getspec, \pcol@setcw@getspec@i and \pcol@setcw@fill to extract the infinite stretch factor f given as f\fill in the specification.
- \itemsep is an API\skip register to have the vertical skip inserted above each non-first \item in list-like environments. It is referred to by \pcol@zparacol to nullify the insertion going to be made by the first \item of a list-like environment, when the macro finds the paracol environment to start is at the very beginning of a list-like environment.
- \floatsep is an API \skip register to have the vertical skip between adjacent floats. It is referred to by \pcol@cflt to cancel the skip following the last float, by \pcol@makefcolumn to let \pcol@makefcolelt examine the capacity of a float column in the last page, by \pcol@addflhd and \pcol@hdflelt to measure the total height of top and bottom floats, and by \pcol@sync to calculate the space below the MVL-float.
- \textfloatsep is an API \skip register to have the vertical skip between the main vertical list and top/bottom floats. It is referred to by \pcol@output@start to calculate the room for each column-page in the starting page with bottom floats in the pre-environment stuff, by \pcol@combinefloats to insert a skip below the bottom floats in the pre-environment stuff and last page, by \pcol@measurecolumn to take this skip into account in the calculation of V_P' , by \pcol@addflhd to measure the vertical space for top and bottom floats, and by \pcol@synccolumn to calculate the synchronization point for columns with top floats.
- \dblfloatsep is an API \skip register to have the vertical skip between adjacent page-wise floats, and is used in \pcol@startpage to cancel the skip below the last float.
- \dbltextfloatsep is an API \skip register to have the vertical skip between the last pagewise float and the top of columns, and is used in \pcol@startpage to put the skip.
- \Otopsep is a \skip register to have the vertical skip inserted above the first \item of a list-like environment. The actual value is determined by \Otrivlist from API parameters \topsep, \partopsep and \parskip depending on how the environment appears. The skip in the register is inserted by \pcolOzparacol when it finds the paracol environment to start is at the very beginning of a list-like environment.
- \@fptop is a \skip register to have the vertical skip inserted at the top of a float column, and is used in \pcol@makefcolpage.
- \Offpsep is a \skip register to have the vertical skip between adjacent floats in a float column, and is used in \pcolOmakefcolpage.

\Ofpbot is a \skip register to have the vertical skip inserted at the bottom of a float column, and is used in \pcolOmakefcolpage.

\Otempskipa is a **\skip** register for temporary use. It is used in the following macros.

- \pcol@makecol, \pcol@startpage, \pcol@outputelt, \pcol@output@switch, \pcol@flushcolumn and \pcol@makeflushedpage to throw $\pi^t(p)$ away because we don't need it.
- \pcol@output@start to determine \topskip for the starting page.
- \pcol@setcw@getspec@i and \pcol@setcw@fill to have the width specification of a column or gap.

It is also used in the top level invocation of \pcol@defkw with a glue of 0 pt plus 1 fil minus 1 fil.

2.1.5 Box Registers

\strutbox is an API \box register to have the strut for the current font size. It is used in \pcol@fntextbody{text} to let \splitmaxdepth have its depth, and to let the last line of the footnote $\langle text \rangle$ have its depth at shallowest.

\@cclv is a \box register but T_EX defines that it has the main vertical list when \output routine is invoked. It is referred to by \pcol@makecol when it has a broken spanning text to measure its height-plus-depth for the element to be added to $\pi^s(p_t)$ and to update it combining its contents with pre-spanning-text stuff optionally shifting it left by passing the register to \pcol@shiftspanning. The macro also uses the register together with its callee \pcol@unvbox@cclv to add stretch/shrink factor of \skip\footins at its bottom for a column-page in a page having page-wise footnotes. The macro \pcol@specialoutput examines the register to discard the dummy \vbox inserted in it by \pcol@invokeoutput. The other users \pcol@output@start, \pcol@makenormalcol, \pcol@flushcolumn and \pcol@imakeflushedpage let the register have the main vertical list of pre-environment stuff or a column to be passed to \@makecol, and \pcol@flushcolumn also takes care the skip above page-wise footnotes.

\voidb@x is a \box register to be void (\bot) always. It is used to initialize \pcol@prespan and \pcol@rightpage at their declaration, and is referred to by the following macros.

- \pcol@makecol to make \pcol@currfoot void unless page-wise footnotes in \foot ins is saved into $\pi^f(p)$.
- \pcol@startpage to let $\pi^i(p_t) = \bot$ if the new top page does not have spanning stuff and $\pi^f(p_t) = \bot$ for all float pages and the new top page.
- \pcol@outputelt to initialize \@outputbox.
- \pcol@ioutputelt to examine if S_c is empty.
- \pcol@output@start to let $\pi^f(0) = \bot$, and $\gamma_0^c = \bot$ if $\hat{\gamma}_0^c$ is undefined.
- \pcol@output@switch to let $\kappa_c(\tau^b) = \bot$ if the column does not have column-wise footnotes.
- \pcol@getcurrfoot to let \footins be void if so.
- \pcol@setcurrcolnf to let $\kappa_c(\tau^b) = \bot$ because the column c does not have columnwise footnotes.

- \pcol@putbackmvl to let \pcol@prespan = \bot if a spanning text really starts from the top of a column-page, and $\Gamma_s = \bot$ if the column-page $\kappa_c(\beta)$ to be restarted is non-empty.
- \pcol@savecolorstack to let $\Gamma_s = \bot$ or its first item be \bot if Γ^c or γ_0^c is \bot , respectively.
- \pcol@savefootins to let its argument macro have a void box if \@freelist is exhausted.
- \pcol@makeflushedpage to initialize \@outputbox and \pcol@rightpage to be \bot if the flushed page does not have spanning stuff, and to let $\pi^f(p_t) = \bot$ after putting it in the last page so that \pcol@output@end will be unaware of the page-wise and non-merged footnotes.
- \pcol@flushfloats to let \pcol@rightpage = \perp if parallel-paging is not in effect.
- \pcol@output@end to let \pcol@rightpage = \bot if the last page has nothing other than spanning stuff being page-wise floats and thus we don't have the right parallel-page. The macro also lets $\gamma_0^c = \bot$ for all c and $\Gamma = \bot$.
- \pcol@com@flushpage and \pcol@com@clearpage gives the void box to \pcol@flushclear as its argument to mean these macros are only aware of \ifpcol@flush as the result of pre-flushing column height check. The macro \endparacol also does that if the footnote typesetting is merged.

\@holdpg is a \box register to have the main vertical list when \output is invoked with a special \penalty code. It is let have that by \pcol@specialoutput, and is referred to by \pcol@output@start and \pcol@makenormalcol for pre-environment stuff, and by \pcol@output@switch for the column from which we are leaving.

\Coutputbox is a \box register to have a partial or the complete ship-out image of a column or a page. The usages of the register are as follows.

- In \pcol@@makecol, it has a column-page made by \@makecol for \pcol@flush column and \pcol@imakeflushedpage.
- In \pcol@combinefloats, it has a column-page to which top and bottom floats are combined.
- In \pcol@cflt, it has a column-page to which top floats are combined.
- In \pcol@opcol, it has the complete column-page built by \@makecol.
- In \pcol@startpage, it has the complete float page built by \@tryfcolumn.
- In \pcol@outputelt, it has the complete (left parallel-) page to be shipped out by \@outputpage.
- In \pcol@outputpage@r, it is temporarily made \let-equal to \pcol@rightpage so that the box is shipped out by \pcol@@outputpage being IATEX's \@outputpage instead of the real \@outputbox.
- In \pcol@output@start, it has the pre-environment stuff built by \pcol@makenormalcol.
- In \pcol@combinefootins, it is let have the pre-environment stuff with footnotes.
- In \pcol@flushcolumn, it has a flushed column-page built by \@makecol or a float column built by \@makefcolumn.

- In \pcol@output@flush and \pcol@output@clear, it has a flushed page built by \pcol@makeflushedpage and \pcol@imakeflushedpage in which it has each of flushed column-page built by \@makecol.
- In \pcol@flushfloats, it has the complete (left parallel) page for flushed float columns.
- In \pcol@iflushfloats, it has a float column built by \pcol@makefcolumn.
- In \pcol@output@end, it has the ship-out image of the last page of a paracol environment built by \pcol@makeflushedpage and \pcol@imakeflushedpage.

\@tempboxa is a \box register for temporary use. The usages of the register are as follows.

- In \pcol@makecol, it is used to decapsulate \box255 containing a broken spanning text. In the macro and \pcol@output@switch, it is also used as a waste bascket to make \footins void when it contains page-wise footnotes in a non-top page.
- In \pcol@cflt and \pcol@startpage, it has top column-/page-wise floats combined by the application of \@comflelt/\@comdblflelt to \@toplist/\@dbltoplist respectively.
- In $\pcol@phantom(b)$, it has an empty box whose height and depth are equal to those of the argument box b.
- By \pcol@buildcolseprule and its callees \pcol@buildcselt@S and \pcol@buildcselt, it is let have the painted backgrounds for columns, column-separating gaps and spanning texts in a page, and then is put into the ship-out image of the page by \pcol@ioutputelt, \pcol@imakeflushedpage or \pcol@iflushfloats.
- In \Coutputpage, it is let have the painted background of the right page referred to by its callee \pcolCoutputpageCr.
- In $\pcol@bg@paint@i{body}$, it is let have painted backgrounds built by $\langle body \rangle$.
- In \pcol@bg@paintregion $\langle a \rangle \langle c \rangle$, it is let have painted background of the region $R_a^{[c]}$.
- In \pcol@specialoutput, it is used to discard the dummy \vbox put by \pcol@invokeoutput.
- In $\protect{\protect}$ or it is used to save $\protect{\protect}$ for pre-environment stuff.
- In \pcol@ifempty $\langle box \rangle \langle then \rangle \langle else \rangle$, it is used to examine if $\langle box \rangle$ is empty.
- In \pcol@scancst $\langle box \rangle$ and \pcol@iscancst, it is used to have what Γ or Γ_s has after the scan of $\langle box \rangle \in \{\Gamma, \Gamma_s\}$.
- In \pcol@savecolorstack, it is used to have the \vbox for γ_0^c to be placed at the top of Γ_s .
- In \pcol@deferredfootins, it is used to have the first half split from Φ being the deferred footnotes to be \inserted.
- In \pcol@fntextbody{text}, it is used to encapsulate $\langle text \rangle$ in it.
- In \pcol@icolumncolor, it is used to have a \vbox to be \inserted for the update of γ_0^c .
- In \pcol@set@color@push, it is used to have a \vbox to be \inserted to push γ_i or $\gamma_{i,m}$ to Γ_r .
- In \pcol@reset@color@pop and \pcol@reset@color@mpop, it is used to have a \vbox to be \inserted to add γ_i^- or $\gamma_{i,m}^-$ to Γ_r .

2.1.6 Token Registers

- \output is TEX's primitive to have \output routine. It is let have \pcol@output as its sole token by \pcol@zparacol.
- \everypar is TEX's primitive to have tokens inserted at the beginning of each paragarph. In \pcol@sptext and \pcol@com@endcolumn, it is \globalized to keep its contents after the end of a group. In \pcol@output@switch, its contents are broadcasted to $\kappa_c(\varepsilon)$ for all $c \in [0, C)$ if columns are synchronized with a spanning text. Then these values or that simply given in a column are saved into $\kappa_c(\varepsilon)$ by \pcol@setcurrcol, and then restored from it by \pcol@igetcurrcol.
- \everyvbox is TeX's primitive to have tokens inserted at the beginning of each \vbox. In \pcol@zparacol, after tokens in it are saved into \pcol@everyvbox, it is let have a \therefore reference to \pcol@everyvbox and \pcol@innertrue to turn \ifpcol@inner = true, and then the register itself is made \let-equal to \pcol@everyvbox. In addition, it is let have tokens in \pcol@everyvbox if a \global assignment to the register is made in the paracol just having been closed. Another usage of this register is to insert a painted page background to the \vbox to be \shipout by \pcol@outputpage being IATeX's \@outputpage, and is used for this purpose by \pcol@outputpage@l and \pcol@outputpage@r, and by \pcol@outputpage@ev to nullify this special function for other inside \vboxes.

\Centure temporary use. It is used in \pcolCoutputCswitch to broadcast \everypar to $\kappa_c(\varepsilon)$ for all $c \in [0, C)$.

2.1.7 Switches

- \if@twocolumn is a switch to be true iff multi-column pages are being typeset. It is turned true by \pcol@zparacol, and then turned false by \endparacol. In addition, it is turned false when \pcol@output finds that the \output request for a page break outside paracol is sneaked into our own \output routine, in order to avoid that LATEX's original \output routine misunderstands it is working on a two-columned document. The switch is examined by LATEX's own macros including old \end@dblfloat kept in our own \pcol@end@dblfloat. It is also examined by \pcol@zparacol before being turned true to ensure it is false or to complain about the inappropriateness otherwise.
- \if@firstcolumn is a switch to be *true* iff the first column is being typeset. Its truth value is determined by \pcol@addmarginpar to tell \pcol@addmarginpar, \pcol@getmparbottom@i and \pcol@setmpbelt@i the margin which a marginal note goes to.
- \if@twoside is a switch to be true iff two-sided page typesetting is in effect and thus even numbered page may have their own left margins, headers and footers different from those for odd numbered pages. Besides the initialization by the main class file such as article.cls according to the class option twoside, the switch is \globally turned false by \pcol@ twosided for the case in which API macro \twosided does not have 'p' in its optional argument, and then \globally turned true by \pcol@twosided@p which is invoked when the argument contains 'p', or the API macro does not have the argument at all. Then the switch is referred to by \pcol@outputpage@l, \pcol@outputpage@r and \pcol@bg@ swappage to decide the left margin of even numbered pages, i.e., \evensidemargin if the switch is true or \oddsidemargin otherwise. The switch is also referred to by \pcol@ com@cleardoublepage to have a blank page if the switch is true and the command \cleardoublepage is used in an odd-numbered page.

- \if@reversemargin is a switch to be *true* iff \reversemarginpar is specified to reverse the side which marginal notes go to. It is examined by \pcol@addmarginpar as a factor to decide the margin which a marginal note goes to, and by \pcol@do@mpbout@i for the same purpose but for marginal notes in pre-environment or post-environment stuff.
- \if@mparswitch is a switch to be *true* iff it is specified by, for example, twoside option of a class such as article, that marginal notes in even numbered pages go to thier left margin. It is examined by \pcol@do@mpbout@i as a factor to decide the margin which a maginal note goes to in pre-environment or post-environment stuff.
- \if@nobreak is a switch to be true iff the last paragraph is for a sectioning command. The switch is saved into $\kappa_c(\sigma)$ together with \if@afterindent by \pcol@setcurrcol, and then restored from it by \pcol@igetcurrcol. The macro \pcol@output@switch refers to it to broadcast its value set by a spanning text to $\kappa_c(\sigma)$ for all $c \in [0, C)$, while \pcol@output@start and \pcol@restartcolumn insert \penalty = 10000 by \nobreak if the switch is true. This conditional \nobreak is also done by \pcol@icolumncolor, \pcol@set@color@push, \pcol@reset@color@pop and \pcol@reset@color@mpop to avoid a break after an \insert. The macro \pcol@zparacol also exmaines the switch, but with the truth value in it given outside paracol environment, to invoke \@nbitem if true when the macro finds the paracol environment to start is at the very beginning of a list-like environment.
- \if@newlist is a switch to be *true* in the duration after a list-like environment starts and until its first \item appears. The switch is examined by \pcol@zparacol to know if the paracol environment to start is at the very beginning of a list-like environment and, if so, is turned *false* by the macro after it inserts vertical skips pretending the first \item is given.
- \if@inlabel is a switch to be *true* in the duration after an \item appears and until its first paragraph is given. The switch is examined by \pcol@zparacol together with \if@newlist to know if the paracol environment to start is at the very beginning of a list-like environment (false) and not trivlist-like one (true).
- \if@afterindent is a switch to be *true* iff a sectioning commmand tells that the first paragraph following it is to be indented. The switch is saved into $\kappa_c(\sigma)$ together with \if@nobreak by \pcol@setcurrcol, and then restored from it by \pcol@iigetcurrcol. The macro \pcol@output@switch refers to it to broadcast its value set by a spanning text to $\kappa_c(\sigma)$ for all $c \in [0, C)$.
- \iffcolmade is a switch to be true iff a float column or float page is built by \Ottyfcolumn or \Omakefcolumn. The value is set by \Ottyfcolumn for $\kappa_c(\lambda_d)$ is referred to by \pcolO output, \pcolOstartcolumn and \pcolOfreshpage, while that for \Odbldeferlist is referred to by \pcolOstartpage. The value set by \Omakefcolumn for $\kappa_c(\lambda_d)$ is referred to by \pcolOflushcolumn, while that for \Odbldeferlist is referred to by \pcolO outputOclear. The macros \pcolOflushfloats and \pcolOiflushfloats also refer to the switch to build pages having only float columns and turn the switch true or false by themselves to know such pages are still to be built or not. The macro \pcolOoutputOend also turns the switch true if a last page will be followed by page(s) having float columns to tell that to \pcolOflushfloats.

\if@tempswa is a switch for temporary use. The usages of the switch are as follows.

- In \pcol@checkshipped, it is turned *true* iff S_c for all $c \in [0, C)$ have column-pages to be shipped out, and then it is examined by \pcol@opcol.
- In \pcol@nextpage and \pcol@nextpelt, it is *true* until \pcol@nextpelt finds the first q such that q > p and $\pi^h(q) \ge 0$ to mean q is not for a float page, so that we let p = q to skip float pages following to the old p if any.
- In \pcol@outputcolumns and \pcol@outputelt, it is *true* until \pcol@outputelt finds the first q such that $q \ge p_b$ and $\pi^h(q) \ge 0$ to mean q is not for a float page, and the arguemnt of \pcol@outputcolumns is 0 to mean that it is not for page flushing, so that we ship out q and all float pages following it if any.
- In \@outputpage it is let have the value of \ifpcol@bg@painted indicating if background painting for the left page is done, and then it is examined by \pcol@ outputpage@l to determine whether the background is put into the final ship-out image.
- In \pcol@makenormalcol, it is *true* iff the footnotes in pre-environment stuff is included in \@outputbox which the macro builds.
- In \pcol@output@switch, at first it holds \if@nobreak of the spanning text if columns are synchronized with it to broadcast \if@nobreak to all $\kappa_c(\sigma)$. Then it is turned true iff \ifpcol@sync = true for synchronization or \ifpcol@clear = true for flushing, so as to invoke \pcol@sync. And finally, it is turned true iff \ifpcol@clear = false or \ifpcol@sync = true, so as to invoke \pcol@restartcolumn.
- In \pcol@restartcolumn, it is turned *true* iff footnote typesetting is page-wise and $p < p_t$.
- In \pcol@scancst, it is initialized to be true. Then it is referred to by \pcol@iscancst for each $\gamma \in \Gamma_r$ to update γ_0^c and then turned false when the first one is found.
- In \pcol@savecolorstack, it is true iff either $\Gamma \neq \bot$ or $\gamma_0^c \neq \bot$, i.e., Γ^c to be saved is not \bot
- In \pcol@getmparbottom, it is intialized to be false and then may be turned true by \pcol@getmpbelt if it finds a gap between two marginal notes to accommodate that to be added, and then examined by \pcol@getmparbottom to know the fact.
- In \pcol@sync, it is turned *true* iff the synchronized or flushed page can be built by \pcol@synccolumn.
- In \pcol@makefcolumn having non-empty $\kappa_c(\lambda_t)$, it is turned false iff the macro is acting on a column in the last page, $\kappa_c(\lambda_d)$ is emptied by the macro itself, and the total size of the floats to be put in the float column being built by the macro is less than \@fpmin, to mean it is possible that the floats in $\kappa_c(\lambda_t)$ is put in the float column as top floats.
- In \pcol@measurecolumn and \pcol@addflhd, it is set to be false iff both top floats and the main vertical list are empty, so that \pcol@measureupdate examines it for the update of V_T and D_T . Then it is kept false iff both of footnotes and bottom floats are empty, so that \pcol@measurecolumn examines it for the update of V_P and \pcol@measureupdate does for V_P' and D_P .
- In \pcol@makeflushedpage, it is made false iff p_t is the last page, $V_P' = -\infty$ to mean all columns are empty and $\pi^f(p_t) = \bot$, so as to make the spanning stuff in $\pi^i(p_t)$ a float in post-environment stuff if \ifpcol@dfloats also false. Then it is

kept false if $\t false$ if $\t false$ or $\pi^i(p_t) = \bot$ to mean nothing is shipped out for last page. Then it is made false iff p_t is the last page without deferred floats and merged footnote typesetting is in effect, i.e., the switch is true iff page-wise footnotes are put in the page to be flushed.

- In \pcol@imakeflushedpage, it is turned true iff $\kappa_c(\rho_t) = \infty$ and $V_P' = \pi^h(p_t)$ to mean the floats in $\kappa_c(\lambda_t)$ should be put in a float column in the last page as usual.
- In \pcol@iflushfloats, it is turned *true* iff one or more columns have non-empty $\kappa_c(\lambda_d)$ after shipping a page for float columns out, so that \if@fcolmade is let have its value after scanning all columns.
- In \pcol@output@end, it is turned *true* iff we built float columns, or the main vertical list in the last page is empty and the page is not the starting page, so that we create a new page for the post-environment stuff.
- In \globalcounter{ctr}, it is turned true iff $\langle ctr \rangle \in \Theta^g$ already.
- In \pcol@cmpctrelt(θ), it is turned *true* iff θ is not in Θ_0 or $val(\theta) \neq val_0(\theta)$, so that θ is added to \@gtempa being the list of local counters to be synchronized.
- In \pcol@switchcolumn[d], it is turned false iff $0 \le d < C$ so that we complain c is invalid if the switch is true.
- In \pcol@ac@caption@def $\langle s \rangle \langle t \rangle$, \@tempswatrue or \@tempswafalse is given as its first argument s by \pcol@ac@caption@enable or \pcol@ac@caption@disable respectively, so that \if@ac@caption@if@ $\cdot t$ is made \let-equal to s and \pcol@ac@caption examines it for enabling/disabling \addcontentsline respectively. The macros \pcol@ac@caption@if@lof and \pcol@ac@caption@if@lot are initialized to be \let-equal to \@tempswatrue as the default.
- In \pcol@icolumncolor, it is turned *true* iff we are in a \vbox or in restricted horizontal or math mode.
- In \pcol@backgroundcolor@i, it is exmained if the root of the invocation chain is \backgroundcolor which turns the switch *true*, or \nobackgroundcolor which turns it *false*, to determine whether the background of a region is painted or not.

2.2 Macros

2.2.1 Procedural Macros

\par is TEX's primitive to end/start paragraphs, but may be modified by IATEX to have some special functionality occasionally. The macro \pcol@output makes it \let-equal to \@@par in which the TEX's orinigal definition is kept, while \pcol@zparacol and \pcol@ par use it as is.

\space is an API macro to have a space token. It is used in \pcol@output, \pcol@icolumncolor, \pcol@defcseprulecolor@i and \pcol@backgroundcolor@ii for warning messages, and in \pcol@def@extract@fil to \define the macro \pcol@extract@fil having spaces in its argument specification.

\nointerlineskip is an API macro to let \prevdepth = −1000 pt to inhibit TEX's baseline progress mechanism. It is used in \pcol@ioutputelt, \pcol@makeflushedpage and \pcol@imakeflushedpage to joint boxes without \baselineskip between them, in \pcol@outputpage@ev to suppress the \baselineskip insertion after the first box of painted background in the final ship-out image, and in \pcol@bg@paint@i for the same purpose for the box having painted backgrounds.

- \offinterlineskip is an API macro to let \baselineskip = $-1000\,\mathrm{pt}$, \lineskip = 0 and \lineskiplimit = \maxdimen to supress \baselineskip insertion for all boxes following this macro. It is used in \pcol@bg@paint@i to do that in the box in which painted backgrounds are built.
- \thepage is an API macro to have the representation of the counter page. It is used in \pcol@ output for a warning message.
- \stepcounter $\langle \theta \rangle$ is an API macro to increment the counter θ and zero-clear its descendant counters. It is used in \pcol@startpage for the counter page, and in \pcol@iffootnotetext for footnote.
- \nobreak is an API macro to insert \penalty = 10000 to inhibit line or page breaks. It is used in \pcol@output@start, \pcol@restartcolumn, \pcol@icolumncolor, \pcol@set@color@push, \pcol@reset@color@pop and \pcol@reset@color@mpop to meet the page-break inhibition request made by \if@nobreak = true.
- $\begin{tabular}{ll} $$ \addvspace{$skip$} is an API macro to insert a vertical $$\langle skip$$ if $$ \advspace{$skip$}$, or a skip of $$\langle skip$$ + $$\advspace$. The macro is used in $$\advspace$ when it finds the paracol environment to start is at the very beginning of a list-like environment, to insert $$\advspace$ instead of $$\advspace$ in$
- $\label{eq:local_pen_local} $$ \an API macro to insert a page break \penalty = \langle pen \rangle if \end{order} is an API macro to insert a page break \penalty = \langle pen \rangle if \end{order} if \end{order} is used in \penalty which is reinserted after the \penalty. The macro is used in \penaltoutput@start and \penaltoutput@start an$
- \footnotesize is an API macro to set the font size for footnotes. It is used in \pcol@ fntextbody for footnote typesetting.
- $\[r]_{w}_{h} \]$ is an API macro to draw a vertical rule of w width and h tall, optionally raised by r. It is used in $\[color of footnote \]$ is at least as tall as $\[color of footnote \]$ is at least as tall as $\[color of footnote \]$.
- $\mbox{\mbox{$\$

- \footnote[num]{text} is an API macro to give a footnote $\langle text \rangle$ optionally with its number $\langle num \rangle$. In \pcol@zparacol it is made \let-equal to \pcol@footnote to implement its starred version and the adjustment of footnote at \end{paracol}, while its original version is kept in \pcol@footnote.
- \footnotemark[num] is an API macro to give a footnote mark optionally with the number \(num \) which the mark represents. In \pcol@zparacol it is made \let-equal to \pcol@footnotemark to implement its starred version and the adjustment of footnote at \end \{paracol\}, while its original version is kept in \pcol@@footnotemark.
- \footnotetext[num]{text} is an API macro to give a footnote \langle text \rangle optionally with its number \langle num \rangle but without putting the mark in the footnoted text. In \pcol@zparacol it is made \let-equal to \pcol@footnotetext to implement its starred version, while its original version is kept in \pcol@@footnotetext.
- \footnoterule is an API macro to draw a horizontal line above footnotes, or to insert whatever it has above them. With page-wise footnote typesetting, it is redefined in \pcol@zparacol so that it refers to \textwidth instead of \columnwidth for drawing the horizontal line or whatever defined, while the original version is kept in \pcol@footnoterule. Then it is used in \pcol@putfootins to separate footnotes from the stuff above them, with the original or modified definition.
- \newpage is an API macro to break a page. It is used in \pcol@switchcol as the argument of \pcol@visitallcols to break the column-pages visited in the column-scan when the synchronized column-switching requires explicit page breaks.
- \dblfigrule is an API macro to draw a horizontal line between the last page-wise floats and the main vertical list, or to insert whatever it has between them. The macro is used in \pcol@startpage to build spanning stuff in the page p in $\pi^b(p)$.
- \topfigrule is an API macro to draw a horizontal line between the last column-wise top float and the main vertical list, or to insert whatever it has between them. The macro is used in \pcol@cflt and \pcol@synccolumn to insert it below the last (real) top float. It is also made \let-equal to \relax temporarily by \pcol@imakeflushedpage when it put floats in a float column as top floats. Note that the macro and its bottom counterpart \botfigrule should produce a vertical list whose total height and depth is 0, because LaTeX's float mechanism and thus our macros believe so.
- \normalcolor is an API macro to have color specification stuff for normal coloring. The macro is used in \pcol@putfootins to specify the color of footnotes to be put in \@outputbox, in \normalcolumncolor[c] to define that the default color of the column c is the normal color, in \normalcolseprulecolor to specify that the color for column-separating rules is \normalcolor, and in the initial definition of \pcol@colseprulecolor to give the default color for column-separating rules.
- \color[mode] {color} is an API macro defined in coloring pacakes to start text coloring with $\langle color \rangle$ optionally with $\langle mode \rangle$. The macro is used in \pcol@xcolumncolor[mode] {color}[c] and \pcol@ycolumncolor{color}[c] to define the default color of the column c is $\langle color \rangle$ optionally with $\langle mode \rangle$, in \pcol@defcseprulecolor@x and \pcol@defcseprulecolor@y to define the color of column-separating rules, and in \pcol@backgroundcolor@x to define the color for background painting of a region.

- \pfmtname is an API macro defined in pLATEX to have its format name pLaTeX2e (so far). It is used in the top level assignment of the constant switch \ifpcol@bfbottom.
- \PackageError\langle \langle msg\langle msg\langl
- $\label{eq:packageWarning} $$\operatorname{pkg}(msg)$ is a developer's API macro to report a warning message $$\langle msg\rangle$ with the package identification $$\langle pkg\rangle$. The macro is used in $$\operatorname{pcol@ignore}$ to complain an API macro appears in paracol inappropriately, in $$\operatorname{pcol@intextbody}$ if the footnote is taller than $$\operatorname{textheight} \skip\footins$, in $$\operatorname{pcol@mn@warning}$ to show $$\operatorname{marginnote}$ is emulated, and in $$\operatorname{pcol@icolumncolor}$, $$\operatorname{pcol@defcseprulecolor@i}$ i and $$\operatorname{pcol@backgroundcolor@ii}$ to complain $$\operatorname{columncolor}$, $$\operatorname{colseprulecolor}$$/\operatorname{normalcolseprulecolor}$ or $$\operatorname{backgroundcolor}$$ is used without coloring packages respectively.$
- \@@par is an internal macro to keep TEX's original primitive \par in it. The macro is used in \pcol@output to let \par act with its original definition, and in \pcol@switchcol and \pcol@flushclear as the argument given to \pcol@visitallcols to give TEX's page builder the chance of page break in column-scanning.
- \@height is an internal macro having the keyword height. It is used in \pcol@buildcolsep rule, \pcol@buildcselt, \pcol@bg@paintregion@i, \pcol@output@start, and \pcol@ putbackmvl to draw a \hrule for column-separating rule in the first two, a \vrule to be painted in the third, and an invisible \hrule in the fourth and last.
- \@width is an internal macro having the keyword width. It is used in \pcol@buildcolsep rule, \pcol@buildcselt, \pcol@bg@paintregion@i, \pcol@output@start, and \pcol@ putbackmvl to draw a \hrule for column-separating rule in the first two, a \vrule to be painted in the third, and an invisible \hrule in the fourth and last.
- \@plus is an internal macro having the keyword plus. It is used in the following macros.
 - \pcol@makecol to \define \@textbottom with the body of a vertical skip with small infinite stretch and shrink.
 - \pcol@combinefloats for a skip of the same amount in \@textbottom above and that of negative amount to *move* the effect.
 - \pcol@hfil for skips having 1fil infinite stretch with g_c or $g_c/2$ to make it sure the series of columns and column-separating gaps does not cause underfull.
 - \pcol@synccolumn to put a 1 fil infinte stretch below the main vertical list together with a small infinte shrink in the column-page being flushed and having a synchronization point, and a vertical skip with a small infinite stretch to push up the main vertical list above a synchronization point.

- \pcol@setcw@getspec@i to add 0 pt plus 1000 pt minus 1000 pt to \@tempskipa to ensure the register have stretch and shrink components.
- \pcol@setcw@fill to let \@tempskipa = 0 pt plus f fil as the infinite stretch factor of f.

It is also used in the top level assignment of 0 pt plus 1 fil minus 1 fil to \@tempskipa for the invocatoin of \pcol@defkw.

\@minus is an internal macro having the keyword minus. It is used in the following macros.

- \pcol@makecol to \define \@textbottom with the body of a vertical skip with small infinite stretch and shrink.
- \pcol@combinefloats for a skip of the same amount and that of negative amount.
- \pcol@synccolumn to put a small infinite shrink together with a stretch of 1 fil at the bottom of the main vertical list in a column-page being flused and having a synchronization point.
- \pcol@setcw@getspec@i to add 0 pt plus 1000 pt minus 1000 pt to \@tempskipa to ensure the register have stretch and shrink components.

It is also used in the top level assignment of 0 pt plus 1 fil minus 1 fil to \@tempskipa for the invocatoin of \pcol@defkw.

\hb@xt@ is an internal macro having the sequence "\hbox to". It is used in \pcol@ ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to put each column-page in a \hbox of \columnwidth wide and to enclose all of them in a \hbox of \textwidth wide.

 $\ensuremath{\mbox{\sc Nod}}\$ is an internal macro to do $\ensuremath{\mbox{\sc Nod}}\$. It is used in the following macros.

- \pcol@zparacol for \column* and \pcol@com@column*.
- \pcol@remctrelt $\langle \theta \rangle$ for \cl@- θ .
- \definethecounter $\langle \theta \rangle \langle c \rangle \langle rep \rangle$ for \pcol@thectr@ $\cdot \theta \cdot c$,
- \pcol@loadctrelt $\langle \theta \rangle \langle val_c(\theta) \rangle$ for \pcol@ctr@ $\cdot \theta$.
- \pcol@defcolumn for \pcol@com@column*.
- ullet \pcol@defcseprulecolor@i for \pcol@colseprulecolor[$\cdot c$].

We also use this macro in top level \definitions of \pcol@com@nthcolumn*, \pcol@com@leftcolumn* and \pcol@com@rightcolumn* for the starter of the environments nthcolumn*, leftcolumn* and rightcolumn*.

 $\colon colon col$

- \pcol@bg@columnleft for \pcol@columnwidth $\cdot c$ and \pcol@columnsep $\cdot c$.
- ullet \pcol@columnwidth for \pcol@columnwidth $\cdot c.$
- $\pcol@bg@columnsep.c.$
- \pcol@ccuse for γ_0^c = \pcol@columncolor@box $\cdot c$ or $\hat{\gamma}_0^c$ = \pcol@columncolor $\cdot c$.
- \column* for \pcol@com@column*.

- \pcol@zparacol for \pcol@colpream·0.
- \pcol@storectrelt $\langle \theta \rangle$ for \pcol@ctr@ $\cdot \theta$.
- \pcol@cmpctrelt $\langle \theta \rangle$ for \c@-\theta and \pcol@ctr@-\theta.
- \pcol@synccounter for \pcol@counters $\cdot c$ for the column c.
- \pcol@syncctrelt $\langle \theta \rangle$ for \c@ $\cdot \theta$.
- \pcol@stepcounter $\langle \theta \rangle$ for \pcol@counters·c for the column c, and for \clo. θ .
- \bullet \pcol@switchcol to the column c for \pcol@colpream c.
- \pcol@aconlyelt $\langle t \rangle \langle c \rangle$ for \pcol@ac@def@ $\cdot t$.
- \pcol@ac@def@lof $\langle eord \rangle$ and \pcol@ac@def@lot $\langle eord \rangle$ for \pcol@ac@caption@- $\langle eord \rangle$.
- \pcol@ac@caption $\langle type \rangle [\langle lcap \rangle] \langle cap \rangle$ for \pcol@ac@caption@if@-t and for \ext@- $\langle type \rangle$.
- \footnotelayout $\{l\}$ for pcol@fnlayout $@\cdot l$.
- \pcol@twosided[T] for pcol@twosided@ $\cdot t$ where $t \in T$.

\@gobble\langle discards its argument \langle arg\rangle. It is used in \pcol@output@start, \pcol@icolumncolor and \pcol@set@color@push for temporarily letting \aftergroup be \@gobble to nullify \aftergroup with \reset@color invoked in \pcol@set@color, being the original version of \set@color, and in \pcol@zparacol to make \pcol@bg@paintbox \let-equal to \@gobble to nullify it if any coloring packages have not been loaded. In addition, the macros \pcol@F and \pcol@Fe for logging are made \let-equial to \@gobble at the top level to nullify them.

 $\label{eq:continuous} $$ \end{argunity} $$ \end{argunity} is an internal macro to do $$ \langle then \rangle$ or $$ \langle else \rangle$ if $$ \langle cs \rangle$ is undefined or defined respectively. It is used in the following macros; $$ \pcol@bg@caintregion$$ \langle a \rangle \langle c \rangle$ to examine if either $$ \pcol@bg@color@\cdot a \cdot @\cdot c$ or $$ \pcol@bg@color@\cdot a$ is defined; $$ add $$ \contentsonly$$$ \langle t \rangle \langle c \rangle$ to stop the execution if $$ \pcol@ac@def@\cdot t$ is not defined; $$ \pcol@twosided[T]$ to stop the execution if $$ \pcol@twosided@\cdot t$ is not defined; $$ \pcol@backgroundcolor@i$ to stop the execution if $$ \pcol@bg@e\cdot a$ is not defined for a region a; and $$ \pcol@backgroundcolor@i$ to stop the execution if $$ \pcol@bg@mayhavecol\cdot a$ is not defined for a region a.$

 $\cline{char}\langle char \rangle \langle then \rangle \langle else \rangle$ is an internal macro to do $\langle then \rangle$ or $\langle else \rangle$ if the character following to the macro is $\langle char \rangle$ or not respectively. It is used in the following macros to examine if they are followed by a '['.

```
\paracol, \pcol@zparacol, \columnratio,
\pcol@com@column* (initial definition), \pcol@com@switchcolumn,
\pcol@iswitchcolumn, \pcol@adjustfnctr, \pcol@ifootnotetext,
\twosided, \marginparthreshold, \columncolor, \pcol@columncolor,
\normalcolumncolor. \colseprulecolor, \pcol@defcseprulecolor,
\normalcolseprulecolor, \pcol@backgroundcolor,
\pcol@backgroundcolor@w.
```

It is also used in \pcol@backgroundcolor@iii and \pcol@backgroundcolor@iv if they are followed by a '('.

- \@ifstar\langle then \langle \langle else \rangle is an internal macro to do \langle then \rangle or \langle else \rangle if the character following to
 the macro is '*'. It is used in \pcol@yparacol, \globalcounter, \pcol@switchcolumn,
 \pcol@footnote, \pcol@footnotemark and \pcol@footnotetext to examine if the optional '*' is specified.
- $\mbox{\comparison} \mbox{\comparison} \mbox{\comp$

```
\pcol@checkshipped, \pcol@output@start, \pcol@output@switch,
\pcol@sync, \pcol@makeflushedpage, \pcol@freshpage,
\pcol@output@end, \pcol@synccounter, \pcol@com@syncallcounters,
\pcol@stepcounter, \pcol@visitallcols.
```

The macro is also used in the following macros for the ranges following macro name, where $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$ and c is the column they are working on.

The other users have a little bit more complicated range as follows.

- \pcol@flushcolumn to iterate float column building for a column c in pages q such that $q \in (\kappa_c(\beta^p), p_t)$.
- \pcol@setcolwidth@r to make assignment of w_c for $c \in [\min(C^0+k,C^1-1),C^1)$ where k is the number of fractions given as the first or second argument of \columnratio and kept in \pcol@columnratioleft or \pcol@columnratioright, respectively.
- \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to calculate $\lceil y/2^{k_2+k_3} \rceil$ finding k_3 by iterating y/2 until the result becomes less than 2^{15} , to calculate $z'/2^k$ with the range [0, k), to calculate $z'/2^{k-16}$ with the range [0, k-16), and to calculate $z' \cdot 2^{16-k}$ with the range [0, 16-k), where $z' \cdot 2^{16-k} = Z = z \times 1$ pt and k_2 , k_3 and k are scaling parameters for good approximation.
- $\ensuremath{\texttt{Qfor}\langle cs \rangle} := \langle list \rangle \ensuremath{\texttt{do}\langle body \rangle}$ is an internal macro to iterate $\langle body \rangle$ for each element of the comma-separated $\langle list \rangle$ letting $\langle cs \rangle$ have the element. The macro is used in \pcol@

setcolwidth@r to scan its argument $\langle ratio \rangle$ defined by \columnratio, and in \pcol@setcw@scan to scan its argment $\langle spec \rangle$ defined by \setcolumnwidth.

 $\label{eq:continuous} $$ \end{cases} := \langle list \rangle \end{cases} \end{cases} is an internal macro to iterate $\langle body \rangle$ for each non-space token in $\langle list \rangle$ letting $\langle cs \rangle$ have the token. The macro is used in $$\pcol@bg@paint@ii$, $$\pcol@setcw@getspec and $$\pcol@twosided$ to scan their arguments, in $$\pcol@setcw@getspec@i to scan a column/gap specification to remove spaces from it, and in $$\pcol@twosided[T]$ to scan all tokens being two-sided typesetting features in T.$

 $\langle elm \rangle \langle lst \rangle \langle suc \rangle \langle fail \rangle$ is an internal macro to remove the first element from $\langle lst \rangle$, $\langle lst \rangle$ is not empty. Otherwise, it performs $\langle fail \rangle$. The macro is used in the following macros to obtain an \insert from \@freelist.

- \pcol@opcol for the completed column-page.
- \pcol@startpage for float pages and spanning stuff for page-wise top floats.
- \pcol@output@start for the pre-environment stuff, and column-pages and γ_0^c of all columns.
- \pcol@output@switch for the column-page from which we are leaving.
- \pcol@iscancst for γ_0^c .
- \pcol@savefootins for footnotes.
- \pcol@flushcolumn for float columns and the empty column-page in p_t .
- \pcol@synccolumn for an MVL-float on a synchronization if its point defined by a column whose main vertical list is empty.
- \pcol@output@end for the page-wise floats in the last page if the main vertical list of the page is empty.
- \pcol@icolumncolor for γ_0^c .

The macro is also used in $\color{colored}$ ioutputelt to obtain completed column-pages from S_c .

 $\cline{car}\cline{ca$

 $\cons(lst)(elm)$ is an internal macro to add $\cons(lst)(elm)$ to the tail of (lst).

- \pcol@makecol to add span(H, h) to the tail of $\pi^s(p_t)$.
- \pcol@opcol to add the completed current column-page $\kappa_c(\beta)$ to S_c .
- \pcol@startpage to add $\pi(p_t 1)$ and float pages to Π .
- \pcol@outputelt to return spanning stuff $\pi^i(q)$ in a shipped-out float page q to \@freelist, or to add $\pi(q)$ to Π if the page q is kept.
- \pcol@ioutputelt to return spanning stuff $\pi^i(q)$, page-wise footnotes $\pi^f(q)$ and/or column-pages $s_c(q)$ for all $c \in [0, C)$ in a shipped-out page q to \@freelist.
- \pcol@output@start to return the current column-page $\kappa_0(\beta)$ to \@freelist.
- \pcol@output@switch to add span(H,h) to the tail of $\pi^s(p_t)$.

- \pcol@restartcolumn to return the current column-page $\kappa_c(\beta)$ to be resumed, and its footnotes $\kappa_c(\tau)$ if any, to \@freelist.
- \pcol@getmparbottom $\langle t \rangle \langle h \rangle$ to add $mpar(\max(t,b_n),\max(t,b_n)+h)$ to the tail of the list $M_{\{L,R\}}^{\{l,r\}}$, and its callee \pcol@getmpbelt $\langle t_i \rangle \langle b_i \rangle$ to add $mpar(t_i,b_i)$ or $mpar(\max(t,b_{i-1}),\max(t,b_{i-1})+h)$ to the so-far tail of the list in rebuilding.
- \pcol@flushcolumn to return footnotes $\kappa_c(\tau)$ in the current column-page of c to be flushed to \@freelist if any, and to add the flushed column-page and float columns to S_c .
- \pcol@makefcolelt to add a float to \@toplist or $\kappa_c(\lambda_d)$.
- \pcol@synccolumn to add an MVL-float for synchronization to $\kappa_c(\lambda_t)$.
- \pcol@makeflushedpage to return spanning stuff $\pi^i(p_t)$ and/or page-wise footnotes $\pi^f(p_t)$ in the top page to be flushed to \@freelist if any.
- \pcol@imakeflushedpage to return column-wise footnotes in $\kappa_c(\tau)$ s.t. $\kappa_c(\beta^p) = p_t$ to \@freelist if any.
- \pcol@output@end to return $\pi^f(p_t)$, all current column-pages $\kappa_c(\beta)$, and all $\gamma_0^c \neq \bot$ to \@freelist.
- \pcol@end@dblfloat to add a page-wise float in \@currbox to \@dbldeferlist.
- \globalcounter $\langle \theta \rangle$ to add a global counter θ to Θ^g .
- \pcol@iremctrelt $\langle \theta \rangle$ to add a local counter θ to Θ^l .
- \pcol@storectrelt $\langle \theta \rangle$ to add a pair $\langle \theta, val_c(\theta) \rangle$ to Θ_c for a column c.
- \pcol@savectrelt(θ) to add a pair $\langle \theta, val(\theta) \rangle$ to Θ_c for a column c.
- \pcol@cmpctrelt $\langle \theta \rangle$ to add a counter θ to the list of local counters to be synchronized.
- \addcontentsonly $\langle t \rangle \langle c \rangle$ to add a pair $\langle t, c \rangle$ to T.
- \pcol@backgroundcolor@ii to add a region whose background is painted to \pcol@bg@defined.
- $\cdr\langle a_1\rangle\langle a_2\rangle\cdots\langle a_n\rangle$ \Quad in internal macro to be expanded to $\langle a_2\rangle\cdots\langle a_n\rangle$. It is used in \pcol\Quad getcurrpinfo\langle cs\rangle to extract \pi(p_t) from \pcol\Quad currpage = \Quad \Quad to \define \langle cs\rangle letting it have \pi(p_t).
- $\label{eq:condition} $$ \operatorname{ded}(macro)_{body} $ is an internal macro to do \operatorname{def}(macro)_{body} $ with the $$ \operatorname{ded}(macro)_{body} $ is kept in the expansion. It is used in $$ fntextbody to \operatorname{define }\c. $$$
- \cline{msg} is an internal macro to report a warning message \cline{msg} without the line number in which the cause lies. It is used in $\cline{pcol@output}$ if a page with floats and very short main vertical list is built.
- \@eha is an internal macro having a help message saying the command causing an error is ignored. It is used in \pcol@zparacol, \pcol@setcw@calcf, \pcol@switchcolumn, \pcol@switchenv, and \addcontentsonly as the argument of \PackageError.
- \@ehb is an internal macro having a help message saying the error causes a serious problem. It is used in \pcol@ovf, \pcol@zparacol and \pcol@set@color@push as the argument of \PackageError.

- $\ensuremath{\texttt{Qparmoderr}}$ is an internal macro to complain about misplacement of a macro or environment which is expected to appear in "outer par mode". It is used in $\ensuremath{\texttt{pcol@zparacol}}$ if it finds $\ensuremath{\texttt{lifinner}} = true$.
- \@Esphack is an internal macro to put back the horizontal skip and space factor saved by \@bsphack at the end of an environment. It is used in \pcol@end@dblfloat.
- \reset@font is an internal macro \let-equal to \normalfont to use a starndard font. It is used in \pcol@fntextbody for footnote typesetting.
- \set@color is an internal macro to start coloring of texts following it. By default it is \relax but may have a definition to put a \special for coloring with the color in \current@ color. In the following macros, it is examined if \set@color = \relax and/or some local definition is given to \set@color.
 - \pcol@output lets \set@color = \pcol@set@color i.e., lets it regain its original definition because we don't need any special operations in \output routine.
 - \@outputpage performs background painting if \set@color ≠ \relax.
 - \pcol@zparacol performs set-up operations for text coloring, including making \set@color \let-equal to \pcol@set@color@push saving its original definition into \pcol@set@color, and enabling background painting macros if \set@color \neq \relax, while these background painting macros are nullified otherwise.
 - \pcol@icolumncolor complains that no color packages have been loaded if \set@ color = \relax, and then otherwise temporarily lets it be the original saved in \pcol@set@color to \insert a \vbox to update γ_0^c or to do the update immediately.
 - \pcol@iicolumncolor temporarily lets \set@color = \relax so that \color or \normalcolor invoked in the macro just defines \current@color to be set into $\hat{\gamma}_0^c$ without doing any other coloring operations.
 - \pcol@defcseprulecolor@i complains that no color packages have been loaded if \set@color = \relax, while otherwise the macro temporarily lets \set@color = \relax to invoke \color (or \normalcolor) to check if its arguments are properly given.
 - \pcol@backgroundcolor@ii complains that no color packages have been loaded if \set@color = \relax, while otherwise its descendent \pcol@backgroundcolor@x temporarily lets \set@color = \pcol@backgroundcolor@y to \define \pcol@bg@color@a[@·c] to be \current@color.
- \reset@color is an internal macro to finish text coloring started by \set@color. By default it is undefined but may have some definition to put a \special to finish coloring. It is used in \pcol@clearcolorstack so as to apply it to all elements in Γ^c , in \pcol@iscancst to put it to the main vertical list in the case that γ_0^c was \bot and then updated, in \pcol@iscancst icolumncolor to apply it to all elements in $\hat{\Gamma}^c$, and in \pcol@reset@color@pop and \pcol@reset@color@mpop to have an uncoloring \special in the \vbox for γ_i and $\gamma_{i,m}$.
- \color@begingroup is an internal macro to open a group in which a color is specified. It is used in \pcol@putfootins to enclose footnotes with \normalcolor, and in \pcol@fntextbody{text} to enclose the coloring in the footnote \langle text \rangle.
- \color@endgroup is an internal macro to close a group in which a color is specified. It is used in \pcol@putfootins to enclose footnotes with \normalcolor, and in \pcol@fntextbody{text} to enclose the coloring in the footnote \langle text \rangle.

- $\ensuremath{\mbox{\tt Qstpelt}}\langle\theta\rangle$ is an internal macro to zero-clear the counter θ for the implementation of $\ensuremath{\mbox{\tt Stepcounter}}$. It is used in $\ensuremath{\mbox{\tt pcol@stepcounter}}$ to clear the descendent counters of a global counter θ^g listed in $\ensuremath{\mbox{\tt pcol@cl@}}$.
- \@nbitem is an internal macro to insert a vertical skip of \@outerparskip \parskip above the first \item of a list-like environment when \if@nobreak = true. It is used by \pcol@zparacol when it finds the paracol environment to start is at the very beginning of a list-like environment and \if@nobreak = true.
- **\Operboxrestore** is an internal macro to set up typesetting parameters for paragraphs encapsulated in a box. It is used in **\pcolOfntextbody** for paragraphs in a footnonte.
- $\ensuremath{\texttt{Offinalstrut}}\langle box \rangle$ is an internal macro to add an invisible vertical rule whose depth is that of a $\langle box \rangle$. It is used in $\ensuremath{\texttt{Npcol@fntextbody}}$ to make the last line of the footnotes is as deep as $\ensuremath{\texttt{Strutbox}}$ at shallowest.
- \@sect is an internal macro to implement sectioning commands. The original definition of the macro is kept in \pcol@ac@enable@toc, while \pcol@ac@def@toc makes it \let-equal to \pcol@ac@enable@toc or \pcol@ac@disable@toc, the latter of which uses the original version temporarily disabling \addcontentsline.
- \@svsechd is an internal macro (locally) \defined in \@sect and \@ssect to keep the section header of a sectioning command such as \paragraph which puts the header as the leading text of the paragraph following the command rather than putting it as an individual paragraph. The macro is \globalized in \pcol@sptext so that it is properly referred to in \everypar for the paragraph led by the text in case that a spanning text has the sectioning command only and thus the \definition of the macro must survive after we close the group in which the spanning text is put.
- \@svsec is an internal macro (locally) \defined in \@sect to keep \thesection etc. to be displayed as the leading part of the section header. The macro is \globalized in \pcol@ sptext together with \@svsechd because it is in the body of \@svsechd.
- \@caption is an internal macro to implement \caption. The original definition of the macro is kept in \pcol@ac@caption@latex, while \pcol@ac@caption@def makes it \let-equal to \pcol@ac@caption which uses the original version temporarily disabling \addcontentsline if necessary.
- \end@float is an internal macro to close a column-wise float environment. It is used in \pcol@end@dblfloat (but never invoked because we havd \if@twocolumn true always).
- \end@dblfloat is an internal macro to close a page-wise float environment. It is replaced with our own \pcol@end@dblfloat.
- \@endfloatbox is an internal macro to close a \vbox for a float. It is used in \pcol@end@ dblfloat.
- \Clargefloatcheck is an internal macro to examine if a float is too large. It is used in \pcolO endOdblfloat.
- \Offloatplacement is an internal macro for \output routine to reinitialize column-wise float placement parameters. It is used in our own version of it, \pcolOfloatplacement.

- \@dblfloatplacement is an internal macro for \output routine to reinitialize page-wise float placement parameters. It is used in \pcol@startpage and \pcol@output@clear prior to processing page-wise floats in \@dbldeferlist. As discussed in item-(2) of §1.8, this macro in 2015 or later version of LATEX lets \f@depth = 1sp.
- \@xympar is an interal macro to perform the last operations for \marginpar. In \pcol@ zparacol it is made \let-equal to \pcol@xympar for the emulation of \marginnote, while its original version is kept in \pcol@cxympar.
- \p@footnote is an internal macro to have the prefix to \thefootnote in the printed reference of the counter footnote. It is used in \pcol@fntextbody to produce \@currentlabel.
- \Othefnmark is an internal macro to have \thefootnote¹³⁰. It is used in \pcolOfntextbody to produce \Ocurrentlabel.
- $\ensuremath{\texttt{dest}}$ is an internal macro to implement $\ensuremath{\texttt{footnote}}$ and $\ensuremath{\texttt{text}}$. In $\ensuremath{\texttt{pcol@zparacol}}$, it is made $\ensuremath{\texttt{let-equal}}$ to $\ensuremath{\texttt{pcol@fntext}}$.
- $\mbox{\colored}$ is an internal macro to typeset the footnote $\langle fn \rangle$. It is used in $\mbox{\colored}$ fntextbody{\text} to typeset the footnote $\langle text \rangle$ with some other stuff.
- **\@emptycol** is an internal macro for **\output** routine to put back an empty page to the main vertical list. It is used **\pcol@output** if a page with floats and very short main vertical list is built.
- \@specialoutput is an internal macro for \output routine to process an \output request made by IATEX's original \clearpage, \end{float} and \marginpar. It is used in \pcol@ specialoutput to process the request for floats or marginal notes.
- \@opcol is an internal macro for \output routine to output a page or to keep the first column until the second one is completed. This macro is used in \pcol@output to process a sneaked \output request from outside of paracol, and in \pcol@output@end for the case page-wise floats are left at \end{paracol} and they are put in float pages.
- \@makecol is an internal macro for \output routine to build the ship-out image of a column in \@outputbox consisting of top floats, main vertical list in \box255, footnotes in \footins, and bottom floats¹³¹. It is used in \pcol@output to process a sneaked \output request from outside of paracol, in \pcol@makecol for a column-page to be flushed by \pcol@flushcolumn and \pcol@makeflushedpage, in \pcol@makecol for an ordinary column-page, and in \pcol@output@start and \pcol@makenormalcol for pre-environment stuff.
- \@textbottom is an internal macro for \output routine to be put at the bottom of \@outputbox in which a column-page is stored, by \@makecol. This macro is temporarily re\defined by \pcol@makecol for a column-page having synchronization points so that it has a vertical skip of inifinite stretch and shrink to push up/down the stuff below the last synchronization point in order to adjust its top to the point. After that, its original definition kept in \pcol@textbottom is restored. Another modifiers of the macro are as follows; \pcol@makenormalcol to make the macro \let-equal to \relax temporarily to avoid the insertion of whatever the macro has in \@makecol; and \pcol@makeflushedpage to let the macro have \vfil temporarily so that empty columns in a last page are made full size without underfull.

 $^{^{130}\}mathrm{Or}$ \thempfootnote in minipage environment.

¹³¹In pL^ATEX, the order of footnotes and bottom floats are reversed.

- \@outputpage is an internal macro for \output routine to output a page kept in \@outputbox together with the header and footer. The original definition of this macro is saved in \pcol@outputpage to be used in \pcol@outputpage@l and \pcol@outputpage@r being callees of our own revised version of \@outputpage. Therefore, any \output request to result in page ship-out reaches our own \@outputpage and then LATEX's one after we perform operations for parallel-paging and background painting onto the ship-out image.
- \@combinefloats is an internal macro for \output routine to combine top and bottom floats in \@toplist and \@botlist respectively with \@outputbox in which the main vertical list and footnotes have been put by \@makecol, and to have the result in \@outputbox again. In \pcol@zparacol, it is made \let-equal to our own \pcol@combinefloats so that \@makecol and \pcol@makenormalcol uses it instead of the original one. However, if \pcol@output finds that the \output request for a page break outside paracol is sneaked into our own \output routine, it makes this macro \let-equal to \pcol@combinefloats in which IATEX's version is kept so that IATEX's original \output routine works perfectly as original.
- \@cflt is an internal macro for \output routine to put all top floats in \@toplist and related stuff such as the vertical skip of \textfloatsep into \@outputbox together with its old contents being the main vertical list and footnotes 132. It is used in \pcol@combinefloats if the column-page being processed does not have synchronization points.
- \@cflb is an internal macro for \output routine to put all bottom floats in \@botlist and related stuff such as the vertical skip of \textfloatsep into \@outputbox together with its old contents being top floats, the main vertical list and footnotes 132. It is used in \pcol@combinefloats.
- $\cdot \cdot \cdot\cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot$
- $\cline{Comdblflelt}\langle flt \rangle$ is an internal macro for $\cline{Comdblflelt}\langle flt \rangle$ being a page-wise float to the tail of $\cline{Comdblflelt}$ which finally has the spanning stuff for page-wise floats. It is used in $\cline{Comdblflelt}$ to apply to each element of $\cline{Comdblflelt}$ to have the spanning stuff.
- \@startcolumn is an internal macro for \output routine which tries to build a float column for the floats in \@deferlist and, if the column is not built, tries to move floats to \@toplist and \@botlist. This macro is used in \pcol@output to process a sneaked \output request from outside of paracol, and in \pcol@output@end for the case pagewise floats are left at \end{paracol} after which they become column-wise ones.
- $\ensuremath{\mbox{\tt Qtryfcolumn}}\langle lst \rangle$ is an internal macro for $\ensuremath{\mbox{\tt output}}$ routine which examines if a float column or a float page can be built with some floats in $\ensuremath{\mbox{\tt clumn}}$ and, if so, builds the page in $\ensuremath{\mbox{\tt Outputbox}}$ removing floats put in the page from $\ensuremath{\mbox{\tt clumn}}$. It is used in $\ensuremath{\mbox{\tt pcol@startpage}}$ for page-wise floats in $\ensuremath{\mbox{\tt outputbox}}$ and in $\ensuremath{\mbox{\tt pcol@startcolumn}}$ for column-wise floats in $\kappa_c(\lambda_d)$.
- $\langle \mathit{gscolelt} \langle \mathit{flt} \rangle$ is an internal macro for $\backslash \mathit{output}$ routine which examines if a column-wise float $\langle \mathit{flt} \rangle$ can be added to $\backslash \mathit{@toplist}$ or $\backslash \mathit{@botlist}$ being the list of the floats to be put at the top or bottom of a page respectively. Then, if the examination succeeds, $\langle \mathit{flt} \rangle$ is added to $\backslash \mathit{@toplist}$ or $\backslash \mathit{@botlist}$, while it is added to $\backslash \mathit{@deferlist}$ otherwise. It is used in $\backslash \mathit{pcol@trynextcolumn}$ to apply to each element of (the copy of) $\kappa_c(\lambda_d)$.

¹³²In pLATEX, footnotes are not in \@outputbox because of the reversal of footnotes and bottom floats.

- $\langle flt \rangle$ is an internal macro for \output routine which examines if a page-wise float $\langle flt \rangle$ can be added to \@dbltoplist being the list of the floats to be put at the top of a page, and if so, adds $\langle flt \rangle$ to \@dbltoplist, while it is added to \@dbldeferlist or \@deferlist depending on I^TEX's version otherwise as discussed in item-(3) of §1.8. It is used in \pcol@startpage to apply to each element of (the copy of) \@dbldeferlist.
- \@addmarginpar is an internal macro for \output routine to add a marginal note. Its original definition is kept in \pcol@addmarginpar and used in \pcol@addmarginpar being our own \@addmarginpar.
- $\mbox{\column}\langle lst\rangle$ is an internal macro for $\mbox{\column}$ routine to build a float column with some floats at the head of a float list $\langle lst\rangle$ and to remove the floats from the list. It is used in $\mbox{\colored}$ pcol@flushcolumn and $\mbox{\column}$ for $\kappa_c(\lambda_d)$ of column-wise floats, and in $\mbox{\column}$ for $\mbox{\column}$

2.2.2 Structural Macros

- $\ensuremath{\mbox{\sc Velt}} \langle a_1 \rangle \cdots \langle a_n \rangle$ is an internal control sequence to represent a list element having n subelements. The sequence is often made $\ensuremath{\mbox{\sc let-equal}}$ to a macro which processes $\langle a_1 \rangle \cdots \langle a_n \rangle$ and is applied to all members in a list. It is also made $\ensuremath{\mbox{\sc let-equal}}$ to $\ensuremath{\mbox{\sc relax}}$ on a manipulation of a list, such as element addition and concatenation, by $\ensuremath{\mbox{\sc def}}$ The usages of the sequence are as follows.
 - \pcol@F@count \defines \@elt as a macro to increment \@tempcnta by one to measure the cardinality of \@freelist.
 - \pcol@cflt lets \@elt = \@comflelt for $\kappa_c(\lambda_t)$, and then \@elt = \relax to concatenate \@freelist and $\kappa_c(\lambda_t)$.
 - \pcol@setpageno lets \@elt = \pcol@setpnoelt for Π .
 - \pcol@setpnoelt and \pcol@setmpbelt let \@elt = \relax to add $\pi(q)$ to Π . It also uses \@elt to \define \pcol@currpage with \@elt{ $\pi^p(q)$ } $\langle \pi^i(q) \rangle \langle \pi^f(q) \rangle \{\pi^s(p)\}$ { $\pi^m(p)$ }.
 - \pcol@defcurrpage lets \@elt = \relax to \xdefine \pcol@currpage with \@elt{ $\pi^p(q)$ } $\langle \pi^i(q) \rangle \langle \pi^f(q) \rangle \{\pi^s(p)\} \{\pi^m(p)\}.$
 - \pcol@nextpage lets \@elt = \pcol@nextpelt for Π .
 - \pcol@getcurrpage lets \@elt = \pcol@getpelt for Π^+ .
 - \pcol@startpage lets \@elt = \@sdblcolelt for (the copy of) \@dbldeferlist, and \@elt = \@comdblflelt for \@dbltoplist. It also lets \@elt = \relax for the concatenation of \@dbldeferlist and \@deferlist, and that of \@freelist and \@dbltoplist.
 - \pcol@outputcolumns lets \@elt = \pcol@outputelt with two arguments for (the copy of) Π .
 - \pcol@ioutputelt \defines \pcol@bg@footnoteheight and \pcol@bg@float height with \@elt to let painting macros add elements in them to have the height of the background regions $R_{\{n,N\}}$ and $R_{\{f,F\}}$ to be painted.
 - \pcol@buildcolseprule lets \@elt = \pcol@buildcselt@S and then \@elt = \pcol@buildcselt for $\pi^s(p)$, and then \defines \pcol@bg@columnheight with \@elt to add H'_n and \@maxdepth or 0 for the background region $R^c_{\{c,g\}}(n+1)$ where $n = |\pi^s(p)|$.

- \pcol@buildcselt@S \defines \pcol@bg@spanningtop and \pcol@bg@spanning height with \Qelt to define the region $R_S(i)$.
- \pcol@buildcselt \defines \pcol@bg@columnheight, \pcol@bg@spanningtop and \pcol@bg@spanningheight with \@elt to define regions $R^c_{\{c,g\}}(i)$ and $R_s(i)$.
- \pcol@bg@calculate $\langle z \rangle \langle z_0 \rangle \{F\}$ lets \@elt = \pcol@bg@advance to let \@elt $\langle f \rangle$ in F do $z \leftarrow z + f$.
- \pcol@bg@negative{ F^- } lets \@elt = \pcol@bg@nadvance to let \@elt $\langle f \rangle$ in F^- do $z \leftarrow z f$, and then lets \@elt = \pcol@bg@advance to go back to addition.
- \pcol@output@start lets all floats f imported in \@dbldeferlist have depth 0 by \defining \@elt\langle f \to do it, \edefines \pcol@bg@textheight with \@elt having height-plus-depth of pre-environment stuff for background painting of it, and \defines $\pi^m(0)$ having one element in M_L^l or M_L^r for \@mparbottom in pre-environment stuff.
- \pcol@makenormalcol lets \@elt = \relax to concatenate \@freelist and \@midlist.
- \pcol@trynextcolumn lets \@elt = \@scolelt for (the copy of) $\kappa_c(\lambda_d)$.
- \pcol@scancst and \pcol@iscancst let \@elt = \relax to \edefine the list $M = (m \mid \gamma_{j,m}^- \in \Gamma_r, \ j \ge i)$ for $\gamma_{i,*}^-$, and then the latter \defines \@elt as a macro with an argument m to examine $m \in M$ for $\gamma_{i,m}$.
- \pcol@addmarginpar lets \@elt = \pcol@setmpbelt for Π^+ .
- \pcol@getmparbottom lets \@elt = \pcol@getmpbelt for the list $M_{\{L,R\}}^{\{l,r\}}$. It also lets \@elt = \relax for the addition of $mpar(h_i, t_i)$ to the list by itself and \pcol@getmpbelt.
- \pcol@mparbottom@zero has \@elt in its body to have mpar(0,0) for each $M \in \{M_X^x \mid X \in \{L,R\}, x \in \{l,r\}\}$ the macro has.
- \pcol@bias@mpbout@i{y}\@elt{t}{b}\@nil has \@elt in its argument specification, and \defines \reserved@b with \@elt for mpar(t + y, b + y).
- \pcol@getmparbottom@last@i{y} $mpar(t_1, b_1) \cdots mpar(t_n, b_n)$ \@nil at first \defines \reserved@b with \@elt for mpar(y, y) and then \defines \@elt to do it for $mpar(t_i, b_i)$ for all $i \in [1, n]$.
- \pcol@makefcolumn lets \@elt = \pcol@makefcolelt for (the copy of) $\kappa_c(\lambda_d)$ to examine if each float in it can be put in a float column to be built, and then \define it to put floats in $\kappa_c(\lambda_t)$ into $\kappa_c(\beta^b)$.
- \pcol@addflhd lets \@elt = \pcol@hdflelt for its argument $\kappa_c(\lambda_t)$ or $\kappa_c(\lambda_b)$, and then \@elt = \relax to give the default.
- \pcol@makeflushedpage \edefines \pcol@bg@floatheight with \@elt letting it be \relax.
- \pcol@imakeflushedpage \defines \pcol@bg@footnoteheight with \@elt.
- \pcol@output@end uses \@elt in the argument specification of the \definition of \pcol@do@mpbout@elem, lets \@elt = \relax to add the spanning stuff of the last page to the head of \@dbldeferlist, and uses it in the body of \pcol@bg@textheight and \pcol@bg@footnoteheight to be \defined for background painting of page-wise footnotes.

- \pcol@zparacol lets \@elt = \pcol@remctrelt for Θ^g , \@elt = \pcol@thectrelt for Θ^l , \@elt = \pcol@loadctrelt for Θ_0 , \@elt = \pcol@cmpctrelt for Θ^l , \@elt = \pcol@defcomelt for \pcol@localcommands, and then \@elt = \relax to give the default.
- \globalcounter{ctr} defeines \Qelt{ θ } for Θ^g to check if there is $\theta \in \Theta^g$ such that $\theta = \langle ctr \rangle$.
- \pcol@localcommands has the sequence of \@elt{com} for all local commands $\setminus \langle com \rangle$.
- \pcol@gcounters has \@elt{page} as its initial definition.
- \pcol@removecounter $\langle \Theta' \rangle \langle \theta \rangle$ lets \@elt = \pcol@iremctrelt for (the copy of) its argument Θ' to remove θ from it.
- \pcol@sscounters $\langle elt \rangle$ lets \@elt = $\langle elt \rangle$, where $\langle elt \rangle$ = \pcol@storectrelt or $\langle elt \rangle$ = \pcol@savectrelt, for Θ^l , and then \@elt = \relax to \xdefine Θ_c .
- \pcol@com@synccounter $\langle \theta \rangle$ gives \@elt{ θ } as the argument of \pcol@synccounter.
- \pcol@synccounter $\langle lst \rangle$ lets \@elt = \relax to have the list $\langle lst \rangle$ in \reserved@a by \edef, \@elt = \pcol@loadctrelt for Θ_c , and then \@elt = \pcol@syncctrelt for $\langle lst \rangle$.
- \pcol@stepcounter $\langle \theta \rangle$ lets \@elt = \pcol@stpldelt for Θ^l , \@elt = \pcol@stpclelt for $\zeta(\theta)$, and then \@elt = \@stpelt for $\zeta(\theta)$.
- \pcol@switchcol lets \@elt = \pcol@setctrelt for Θ_c , \@elt = \pcol@aconlyelt for T, and then \@elt = \relax to give the default.
- \pcol@icolumncolor \defines \Qelt\(\hat{\gamma}_i\) to apply \reset@color for rewinding and \pcol@set@color for reestablishing to each $\hat{\gamma}_i \in \hat{\Gamma}^c = (\hat{\gamma}_0^c, \hat{\Gamma})$ by \pcol@scancst@ shadow, in which \Qelt is explicitly applied to $\hat{\gamma}_0^c$ if it is defined and then implicitly done to $\hat{\Gamma} = \pcol@colorstack@shadow$.
- \pcol@set@color@push lets \@elt = \relax to push a color information into $\hat{\Gamma}$, with save/restore of its original value.
- \resetbackgroundcolor lets \@elt = \pcol@resetbackgroundcolor to scan \pcol@bg@defined containing \@elt{ a_i' } to let \pcol@bg@color· a_i' for each of i.

\@empty is a macro always having nothing. Its major usages are to examine if a macro often having a list is empty, and to make such a macro empty. The following macros use \@empty to examine the emptiness of the objects in parentheses.

```
\label{eq:continefloats} $(\kappa_c(\lambda_t),\,\kappa_c(\lambda_b))$ $$\operatorname{col@checkshipped}(S_c)$ $$\operatorname{col@startpage}(\pi(p_t),\,\mathbb{C})$ $$\operatorname{col@makenormalcol}(\mathbb{C})$ $$\operatorname{col@makenormalcol}(\mathbb{C})$ $$\operatorname{col@getmparbottom}(\pi^m(p))$ $$\operatorname{col@getmparbottom@last}(\pi^m(p_t))$ $$\operatorname{col@getmparbottom@last}(\pi^m(p_t))$ $$\operatorname{col@getmparbottom@last}(\pi^m(p_t))$ $$\operatorname{col@getmparbottom}(\kappa_c(\lambda_d))$ $$\operatorname{col@makefcolumn}(\kappa_c(\lambda_t),\,\kappa_c(\lambda_d))$ $$\operatorname{col@makefcolumn}(\kappa_c(\lambda_t),\,\kappa_c(\lambda_d))$ $$\operatorname{col@makefcolumn}(\kappa_c(\lambda_t),\,\kappa_c(\lambda_d))$ $$\operatorname{col@addflhd}(\kappa_c(\lambda_t),\,\kappa_c(\lambda_b))$ $$\operatorname{col@synccolumn}(\kappa_c(\lambda_t))$ $$$
```

```
\label{eq:colombiased} $\operatorname{lushedpage}\left(\kappa_c(\lambda_d)\right) \rightarrow \operatorname{lushedpage}\left(\kappa_c(\lambda_d)\right) \rightarrow \operatorname{lushfloats}\left(\kappa_c(\lambda_d)\right) \rightarrow \operatorname{lushfloats}\left(\kappa_c(\lambda_d)\right) \rightarrow \operatorname{lushedpage}\left(\operatorname{default}\left\langle x_d'\right\rangle \left(x_d'\right) \rightarrow \operatorname{lushedpage}\left(\operatorname{default}\left\langle x_d'\right\rangle \left(x_d'\right) \right) \rightarrow \operatorname{lushedpage}\left(\operatorname{lushedpage}\left(\operatorname{default}\left\langle x_d'\right\rangle \left(x_d'\right)\right) \rightarrow \operatorname{lushedpage}\left(\operatorname{lushedpage}\left(\operatorname{lushedpage}\left(x_d'\right)\right) \right) \rightarrow \operatorname{lushedpage}\left(\operatorname{lushedpage}\left(\kappa_c(\lambda_d)\right)\right) \rightarrow \operatorname{lushedpage}\left(\kappa_c(\lambda_d)\right) \rightarrow \operatorname{lushedpage}\left(\kappa_c(\lambda_d
```

The following macros use \@empty to empty the objects in parentheses.

```
\label{eq:constraints} $$\operatorname{col}(C) \cap (\Pi, \pi(p_t)) \rightarrow \mathbb{C}(C) \cap (\Pi, \pi(p_t)) \cap \mathbb{C}(C) \cap (\Pi, \pi(p_t)) \cap \mathbb{C}(C) \cap (H_c(\lambda_d)) \cap \mathbb{C}(C) \cap (H_c(\lambda_d)) \cap \mathbb{C}(C) \cap (H_c(\lambda_d)) \cap \mathbb{C}(C) \cap \mathbb{C}(C
```

\@currentlabel is an internal macro to have the reference to be associated with the \label following it. It is defined in \pcol@fntextbody to have the reference to the footnote with \@thefnmark.

\ext@figure is an internal macro having "lof" being the extention of the file for list of figures. It is used in \pcol@ac@caption $\langle type \rangle [\langle lcap \rangle] \langle cap \rangle$ to have "lof" when $\langle type \rangle =$ figure.

\ext@table is an internal macro having "lot" being the extention of the file for list of tables. It is used in \pcol@ac@caption $\langle type \rangle [\langle lcap \rangle] \langle cap \rangle$ to have "lot" when $\langle type \rangle = table$.

\@currbox is an internal macro which conventionally has an \insert for floats, etc. The following macros use \@currbox having the objects in parentheses.

```
\pcol@opcol (\kappa_c(\beta))
\pcol@startpage (\pi^i(p_t))
\pcol@ioutputelt (s_c(q))
\pcol@output@start (\pi^i(0), \kappa_c(\beta), \gamma_0^c)
\pcol@output@switch (\kappa_c(\beta))
\pcol@restartcolumn (\kappa_c(\beta))
\pcol@igetcurrcol (\kappa_c(\beta))
\pcol@setcurrcol (\kappa_c(\beta))
\pcol@putbackmvl (\kappa_c(\beta))
\pcol@iscancst (\gamma_0^c)
\pcol@addmarginpar (left marginal note)
\pcol@flushcolumn (\kappa_c(\beta), s_c(q))
\pcol@makefcolumn (\kappa_c(\beta))
\pcol@measurecolumn (\kappa_c(\beta))
\pcol@synccolumn (\kappa_c(\beta))
\pcol@imakeflushedpage (\kappa_c(\beta))
```

```
\pcol@freshpage (\kappa_c(\beta))
\pcol@output@end (top float, \kappa_c(\beta))
\pcol@end@dblfloat (page-wise float)
\pcol@icolumncolor (\gamma_0^c)
```

\@marbox is an internal macro which has an \insert for left marginal notes. It is used in \pcol@xympar.

\@currlist is an internal macro which has an list of \inserts for floats and marginal notes given to output. It is used in \pcol@addmarginpar to get the right marginal note from its head.

\@freelist is an internal macro having available \inserts for floats originially, but also column-pages, spanning stuff, footnotes and default column-color in our usage. Besides the acquisition of an \insert from it shown in the description of \@next, it is used by the following macros to return the objects in parentheses to \@freelist.

```
\label{eq:constraints} $\operatorname{pcol@cflt}\left(\kappa_c(\lambda_t)\right)$ $\operatorname{pcol@cflt}\left(\pi^i(q)\right)$ $\operatorname{pcol@coutputelt}\left(\pi^i(q),\,\pi^f(q),\,s_c(q)\right)$ $\operatorname{pcol@coutputelt}\left(\pi^i(p_t),\,\pi^f(p_t),\,s_c(q)\right)$ $\operatorname{pcol@coutput@start}\left(\kappa_0(\beta)\right)$ $\operatorname{pcol@makenormalcol}\left(\operatorname{pmidlist}\left(\operatorname{pre-environment}\left(\operatorname{stuff}\right)\right)\right)$ $\operatorname{pcol@restartcolumn}\left(\kappa_c(\beta),\,\pi^f(p)\,\operatorname{or}\left(\kappa_c(\tau)\right)\right)$ $\operatorname{pcol@savefootins}\left(\pi^f(p)\,\operatorname{or}\left(\kappa_c(\tau)\right)\right)$ $\operatorname{pcol@savefootins}\left(\kappa_c(\tau)\right)$ $\operatorname{pcol@makefcolpage}\left(\kappa_c(\lambda_t)\right)$ $\operatorname{pcol@makeflushedpage}\left(\pi^i(p_t),\,\pi^f(p_t)\right)$ $\operatorname{pcol@makeflushedpage}\left(\kappa_c(\tau)\right)$ $\operatorname{pcol@output@end}\left(\pi^f(p_t),\,\kappa_c(\beta),\,\gamma_0^c\right)$ $
```

In addition \pcol@F@count scans its element to have its cardinality.

\@nil is an internal control sequence which is conventionally used to terminate a variable length argument. It is used in the following macros.

- \pcol@getcurrpinfo for the invocation of \@cdr.
- \pcol@bias@mpbout@i{y}\@elt{t}{b}\@nil to capture t and b following the convention in \pcol@do@mpb@all@ii.
- \pcol@getmparbottom@last@i $\{y\}$ $mpar(t_1,b_1)$ \cdots $mpar(t_n,b_n)$ \@nil to capture $mpar(t_i,b_i)$ for all $i\in[1,n]$.
- \pcol@do@mpb@all@i{ M_L^l }{ M_L^r }{ M_R^r } to terminate the list $M \in \{M_X^x \mid X \in \{L,R\}, x \in \{l,r\}\}$ in the invocation of \pcol@do@mpb@all@ii.
- \pcol@do@mpb@all@ii{y} $mpar(t_1,b_1)\cdots mpar(t_n,b_n)$ \@nil to capture $mpar(t_i,b_i)$ for all $i\in[1,n]$, and then to terminate them passed to \pcol@bias@mpbout@i or \pcol@getmparbottom@last.
- \pcol@setcw@scan for the invocation of \pcol@setcw@getspec $\langle w_d' \rangle / \langle g_d' \rangle / \langle garbage \rangle$ \@nil.

- \pcol@setcw@getspec@i for the invocation of \pcol@extract@fil $\langle n \rangle$ plus $\langle f \rangle$ minus $\langle garbage \rangle$ \@nil and thus in the \definition of it in \pcol@def@extract@fil.
- \pcol@defkw has \@nil in its argument specification to terminate the argument 0pt plus 1fil minus 1fil.
- \pcol@extract@fil@i, \pcol@extract@fil@ii and \pcol@extract@fil@iii have \@nil in their argument specifications as the terminator, and thus \@nil appears in their invocations in \pcol@extract@fil, \pcol@extract@fil@i and \pcol@extract@fil@ii respectively, and in the \definition of \pcol@extract@fil@iii in \pcol@def@extract@fil@iii.
- \pcol@iadjustfnctr and \pcol@iifootnotetext to terminate their argument [[+-]disp] passed to \pcol@calcfnctr.
- \backgroundcolor and \nobackgroundcolor to terminate their first argument given to \pcol@backgroundcolor so that its descendants \pcol@backgroundcolor@x and \pcol@backgroundcolor@z finally capture everything not processed by their ancestors.
- \current@color is an internal macro having color information to be put into .dvi as a part of the argument of coloring \special. It is referred to by \pcol@bg@paintregion@i, \pcol@output@start, \pcol@icolumncolor, \pcol@iicolumncolor, and \pcol@set@color@push, \pcol@backgroundcolor@y.
- \@dbldeferlist is an internal macro having the list of page-wise floats whose page appearance are not yet fixed. It is scanned and then updated in \pcol@startpage and \pcol@output@clear, while \pcol@output@start lets it have \@deferlist made before \begin {paracol}, and \pcol@output@end adds page-wise floats to be put in the empty last page to it and then move the whole of the list to \@deferlist. As discussed in §1.8, 2015 or later version of LATEX no longer uses this list, but we stick with it for page-wise floats produced in paracol environments and thus have its top level definition with empty body in paracol.
- $\cline{Collist}$ is an internal macro having the list of page-wise floats which $\cline{Collist}$ decided to be put in the new page. The macro $\cline{Collist}$ cans it to put all floats into the page p_t as its spanning stuff $\pi^i(p_t)$, and then empties it after returning all floats to $\cline{Collist}$.
- \@deferlist is an internal macro having the list of column-wise floats whose page appearance are not yet fixed. It is scanned and then updated in \pcol@startcolumn, \pcol@trynextcolumn, \pcol@flushcolumn, \pcol@makefcolumn and \pcol@iflushfloats, while the following macros also act on it.
 - \pcol@output@start moves it to \@dbldeferlist because it is created before \begin{paracol}.
 - \pcol@startpage uses it as the interface with \@addtodblcol of 2015 or later version of LATEX as discussed in item-(3) of §1.8.
 - \pcol@setcurrcol and \pcol@igetcurrcol saves/restores it into/from $\kappa_c(\lambda_d)$, respectively.
 - \pcol@makefcolelt $\langle flt \rangle$ returns $\langle flt \rangle$ to the list if $\langle flt \rangle$ cannot be put in the float column which the macro is working on.

- \pcol@measurecolumn examines its emptiness to let \ifpcol@dfloats = true iff not empty.
- \pcol@output@end lets it have \@dbldeferlist so that it processed as column-wise floats after \end{paracol}.
- \@toplist is an internal macro having the list of column-wise floats which is decided to be put at the top of the current column-page by float environments or by \pcol@trynextcolumn. This list is scanned by \pcol@cflt if its invoker \pcol@combinefloats finds the macro is not empty. The list is also scanned by \pcol@makecol, \pcol@output@switch and \pcol@measurecolumn using \pcol@addflhd for the measurement of the combined size of top floats, while \pcol@setcurrcol and \pcol@igetcurrcol saves/restores the list into/from $\kappa_c(\lambda_t)$ respectively. In addition our macros may add an element or build the entire list in the following two cases. One case is for a synchronization for which \pcol@synccolumn lets the main vertical list in $\kappa_c(\beta^b)$ be a float, namely MVL-float to be added to this list. Another case is for a float column in the last page for which \pcol@makefcolumn and \pcol@makefcolelt build this list for deferred floats. In the latter case, the list is scanned by \pcol@makefcolpage invoked from \pcol@makefcolumn itself, \pcol@flushcolumn and \pcol@makeflushedpage.
- \@botlist is an internal macro having the list of column-wise floats which is decided to be put at the bottom of the current column-page by float environments or by \pcol@ trynextcolumn. The emptiness of this list examined by \pcol@combinefloats to invoke the scanner \@cflb unless empty, by \pcol@output@start to calculate the room for each column-page in the starting page, and by \pcol@makenormalcol to decide whether \@makecol is used or not for building pre-environment stuff. The list is also scanned by \pcol@measurecolumn for the measurement of the combined size of bottom floats, while \pcol@setcurrcol and \pcol@igetcurrcol saves/restores the list into/from $\kappa_c(\lambda_b)$ respectively.
- \@midlist is an internal macro having the list of in-text floats which has already been put in the current column-page but is kept to check the ordering of the succeeding floats. The list is emptied by \pcol@makenormalcol after returning all elements in it to \@freelist, while \pcol@setcurrcol and \pcol@igetcurrcol saves/restores the list into/from $\kappa_c(\lambda_m)$ respectively.
- \f@depth is an internal macro having 1sp or being \let-equal to \z@ to specify the float category, page-wise or column-wise respectively, which float-related macros work on. As discussed in item-(2) of §1.8, this feature introduced in 2015 version of LATEX is nullified in paracol environments and thus the setting with 1sp done by \@dblfloatplacement is overriden by \pcol@startpage and \pcol@output@clear when they invoke the macro.
- \clockpt is an internal macro having the list of all counters defined by \newcounter and the counter page. The original usage of this macro is to log the values of all counters into .aux by \include, but we use it to obatin all counters in \pcol@zparacol and \pcol@globalcounter@s.
- \cl@\theta is an internal macro having the list $\zeta(\theta)$ of descendant counters of the counter θ whose increment by \stepcounter lets them 0. The macro \pcol@remctrelt moves it to \pcol@cl@\theta and re\defines it to have \pcol@stepcounter{\theta}.
- \reserved@a is an internal macro for temporary use. Its usages are as follows.

- In \pcol@Fe, it is used to keep the cardinality of \@freelist in \pcol@F@n to log it by \pcol@FF after \pcol@F@n is let have another measurement result.
- In \pcol@iLogLevel $\langle l \rangle \langle name \rangle$, it is used to implement \let\ $\langle name \rangle = \langle name \rangle \cdot l'$ where l' is the roman representation of the level l.
- In \pcol@setpageno, it has Π^+ so that we update Π and $\pi(p_t)$ scanning their original contents.
- In \pcol@getcurrpinfo, it has $\pi(p_t)$ so that we give its five components to \pcol@getpinfo as its first five arguments.
- In \Coutputpage, it has a sequence of background painting for both left and right parallel-pages to be shipped out outside paracol environment.
- In \pcol@outputpage@ev, it has the expansion result of \meaning\yoko to be compared with \reserved@b having \string\yoko for examining if \yoko is a primitive of underlying TFX.
- In \pcol@bg@paintregion $\langle a \rangle \langle c \rangle$, it is let have $a' = a \cdot @ \cdot c$ or a' = a, and then referred to by \pcol@bg@paintregion@i to use \pcol@bg@color·a', and by \pcol@bg@addext $\langle z \rangle \{s\} \{d\}$ to use \pcol@bg@ext@· $d \cdot @ \cdot a'$.
- In \pcol@specialoutput, it is \let-equal to \pcol@output@f corresponding to \outputpenalty = \pcol@op@f, or \@specialoutput.
- In \pcol@output@start, it is let have a background painting macro \pcol@bg@paintbox and the definition of a parameter \pcol@bg@textheight for it.
- In \pcol@output@switch, it is \let-equal to \@nobreaktrue or \@nobreakfalse according to \if@nobreak in the leaving column to broadcast it to other columns.
- In \pcol@ifempty $\langle box \rangle \langle then \rangle \langle else \rangle$, it has $\langle then \rangle$ or $\langle else \rangle$ according to the emptiness of $\langle box \rangle$.
- In \pcol@clearcolorstack, it is \defined to put an uncoloring \special by \reset@color for its argument γ_i in \pcol@iscancst.
- In \pcol@restorecst, it is \defined to put a coloring \special in its argument γ_i by \unvbox done in \pcol@iscancst.
- In \pcol@addmarginpar, at first it is made let equal to 0 or C_L according to $c < C_L$ or not. Then it is let have Π^+ to be scanned to find $\pi^m(p)$.
- In \pcol@getmparbottom@i, it is let have one of $M_{\{L,R\}}^{\{l,r\}}$ according to the side margin which the marginal note to be added goes to, and then it is referred to by \pcol@getmparbottom.
- In \pcol@setmpbelt@i, it is let have what $\pi^m(p)$ should have after the update of a list of marginal notes in it, and then \pcol@setmpbelt updates $\pi(p)$ with the new $\pi^m(p)$ in the macro.
- In $\pcol@bias@mpbout{y}$ and $\pcol@getmparbottom@last{y}$, it is let have $\pcol@bias@mpbout@i{y}$ and $\pcol@getmparbottom@last@i{y}$ respectively, so that they are invoked in $\pcol@do@mpb@all@ii$.
- In \pcol@makeflushedpage, it is let have an invocation of \pcol@bg@paintbox for page-wise floats in $\pi^i(p_t)$ together with the condition of the background painting.
- In \pcol@output@end, it is let have the invocation of \pcol@bg@paintbox for background painting of page-wise footnotes with the condition to do it and a \definition of \pcol@bg@footnoteheight.

- In \pcol@defcomelt $\langle com \rangle$, it is used to implement \let\ $\langle com \rangle = \pcol@com@\langle com \rangle$.
- In \pcol@setcolumnwidth, it is made \let-equal to \pcol@setcolwidth@s or \pcol@setcolwidth@r according to \pcol@columnratioleft = \relax or not.
- In \pcol@setcolwidth@r, it is used to have the fraction r_d being a comma-separated list element in its argument $\langle ratio \rangle$ defined by \columnratio and scanned by a \@for loop.
- In \pcol@setcw@scan $\langle C^0 \rangle \langle C^1 \rangle \{spec\}$, at first it is let have $\langle spec \rangle$, then the result of adding ',' as many as $C^1 C^0$ to the tail, and finally each element in the extended $\langle spec \rangle$ in a \@for loop.
- In \pcol@setcw@getspec@i $\langle default \rangle \langle x'_d \rangle$, it is let have $\langle x'_d \rangle$ from which all space tokens are removed.
- In \pcol@setcw@calcfactors, it is used as a waste bascket to throw away $(W_T W)/(F \times 1 \, \text{pt})$ calculated by \pcol@setcw@calcf.
- In \pcol@extract@fil@i $\langle n \rangle$. $\langle m \cdot unit \rangle$ \@nil, it has $\langle n \rangle$. $\langle m \cdot unit \rangle$, and is referred to by \pcol@extract@fil@ii.
- In \globalcounter{ctr}, it is used to have $\langle ctr \rangle$ for the \ifx-comparison with each $\theta \in \Theta^g$.
- In \pcol@remctrelt $\langle \theta \rangle$, it is used to implement \let\pcol@cl@ $\cdot \theta = \cl@\cdot \theta$,
- In \pcol@removecounter $\langle \Theta' \rangle \{\theta\}$, it is used to have θ for the \ifx-comparison in \pcol@iremctrelt.
- In \pcol@thectrelt $\langle \theta \rangle$, it is used to implement \let\pcol@thectr@ $\cdot \theta = \text{the} \cdot \theta$, and then is made \let-equal to \pcol@thectr@ $\cdot \theta \cdot 0$.
- In \pcol@synccounter $\langle lst \rangle$, it has $\langle lst \rangle$.
- In \pcol@setctrelt $\langle \theta \rangle \langle val_c(\theta) \rangle$, it is made \let-equal to \pcol@thectr@ $\cdot \theta \cdot c$.
- In \pcol@switchenv, it is used to save \switchcolumn which is redefined in the macro, and then to invoke \switchcolumn with the original definition.
- In \pcol@fntext{text}, it is \let-equal to \pcol@fntextother or \pcol@fntext top according to the footnote \langle text \rangle is deferred or not.
- In \pcol@calcfnctr $\langle num \rangle$ \@nil, it has the first token of $\langle num \rangle$ for \ifx-comparison with '+' and '-'.
- In \pcol@twosided[T], it is let have each non-space token in T given by a \@tfor loop.

\reserved@b is an internal macro for temporary use. It is used in the following macros to keep a list shown in paraentheses so that we update the list in the scan of list elements.

```
\label{eq:local_continuous_continuous} $$\operatorname{Odd}(S) \rightarrow (H) \rightarrow
```

In addition, it is used in the following macros.

- In \pcol@outputpage@ev, it has the expansion result of \string\yoko to be compared with \reserved@a having \meaning\yoko for examining if \yoko is a primitive of underlying TFX.
- In \pcol@bg@paint@ii, it has a token in the arguments K_b , K_g and K_c of the macro scanned by \@tfor.
- In \pcol@output@switch, it is \let-equal to \@afterindenttrue or \@after indentfalse according to \if@afterindent in the leaving column to broadcast it to other columns.
- In \pcol@clearcolorstack, it is \defined to put an uncoloring \special by \reset@color for its argument γ_0^c in \pcol@scancst.
- In \pcol@restorecst, it is \defined to put a coloring \special in its argument γ_0^c by \unvcopy done in \pcol@scancst.
- In \pcol@scancst and \pcol@iscancst, after the reference for the purposes shown in the two items above, it has $M=(m\,|\,\gamma_{j,m}^-\in\varGamma_r,\ j\geq i)$ for $\gamma_{i,*}^-$ and in the latter is scanned to find m for $\gamma_{i,m}$ in M.
- In \pcol@addmarginpar, it is made let equal to C_L or C according to $c < C_L$ or not.
- In \pcol@bias@mpbout@i{y}\@elt{t}{b}\@nil, it is let have mpar(t+y,b+y), and in \pcol@getmparbottom@last@i{y} $mpar(t_1,b_1)\cdots mpar(t_n,b_n)$ \@nil it is let have mpar(y,y) or $mpar(t_n,b_n)$, so that they are let be a $M^{\{l,r\}}_{\{L,R\}}$ by \pcol@do@mpb@all@ii.
- In \pcol@setcw@getspec@i $\langle default \rangle \langle x'_d \rangle$, it is let have each non-space token in $\langle x'_d \rangle$ to remove space tokens from it.
- In $\protect\protec$
- In \pcol@extract@fil@ii $\langle unit \rangle$ \@nil, it is let have $\langle unit \rangle$.
- In \globalcounter{ θ }, it has $\theta_i^g \in \Theta^g$ for \ifx-comparison with θ .
- In \pcol@iremctrelt $\langle \Theta' \rangle \{\theta\}$, it has θ for \ifx-comparison with θ' to be removed from Θ^g or Θ .
- In \pcol@calcfnctr $\langle num \rangle$ \@nil, it has '+' and then '-' for \ifx-comparison with the first token of $\langle num \rangle$.
- In \pcol@backgroundcolor@ii, it has \pcol@backgroundcolor@x or \pcol@back groundcolor@z according that the region of background painting and its color is defined or undefined.
- \reserved@c is an internal macro for temporary use. It is used in \pcol@startpage to save \@deferlist in it and then to restore the list from it, and in \pcol@scancst to have \relax or the macro itself to iterate the macro recursively.
- \reserved@d is an internal macro for temporary use. It is used in \pcol@iscancst as a \chardef register to have 0 if m for $\gamma_{i,m}$ is not in the list $M = (n \mid \gamma_{j,n}^- \in \Gamma_r, j \geq i)$, or 1 if found.
- \Qgtempa is an internal macro used as a \globally modifiable scratchpad. Its usages are as follows.
 - In \pcol@ifempty $\langle box \rangle \langle then \rangle \langle else \rangle$, it has \lastpenalty in a \vbox whose value is examined outside the \vbox for the emptiness check of $\langle box \rangle$.

- In \pcol@addmarginpar, it is given to \@xnext as the target to have the second and successive elements of \@currlist which we cannot modify.
- In \pcol@zparacol and \pcol@cmpctrelt, it has the list of counters to be synchronized.
- In \pcol@setcw@getspec@i $\langle default \rangle \langle x'_d \rangle$, it is made \@empty or \relax according to x'_d has \fill or not.
- In \pcol@storectrelt, \pcol@savectrelt and \pcol@sscounters, it has the new version of Θ_c .

3 Register Declaration

3.1 \count Registers

Here we declare registers and switches. The first group is for \count registers.

\pcol@currcol

The register \pcol@currcol has the zero-origin ordinal c of the column which we were in when \output is invoked. Therefore, for example, in the process of \switchcolumn, the register has c from which we are switching to another column. The register is initialized to be 0 by \pcol@ output@start, and then set to \pcol@nextcol = d by \pcol@restartcolumn to switch to (or stay in) d. Note that these two assignments are \global while other macros may locally use the register to, for example, scan all columns $c \in [0, C)$. Besides two macros above, the following macros refer to the register to know which column we are in (or which column is processed by their invokers).

```
\pcol@Log@iii, \pcol@Log@ii, \pcol@FF, \pcol@makecol, \pcol@opcol, \pcol@bg@columnleft, \pcol@bg@columnwidth, \pcol@bg@columnsep, \pcol@output@switch, \pcol@getcurrcol, \pcol@setcurrcol, \pcol@clearcolorstack, \pcol@restorecolorstack, \pcol@addmarginpar, \pcol@getmparbottom@i, \pcol@setmpbelt@i, \pcol@invokeoutput133, \thecolumn, \pcol@sscounters, \pcol@setctrelt, \pcol@com@switchcolumn, \pcol@switchcol, \pcol@visitallcols, \pcol@aconlyelt, \pcol@flushclear. \pcol@columncolor, \normalcolumncolor, \pcol@icolumncolor,
```

Among the macros above, \columncolor and \normalcolumncolor could refer to the register outside paracol environment and thus before the initialization by \pcol@output@start. Therefore, the register is also initialized to be 0 after its declaration to assure safe reference.

The following macros use the register for the scan of all $c \in [0, C)$ by themselves or their invokers.

```
\pcol@output@start, \pcol@output@switch, \pcol@sync, \pcol@flushcolumn, \pcol@measurecolumn, \pcol@synccolumn, \pcol@makeflushedpage, \pcol@flushfloats, \pcol@freshpage, \pcol@output@end, \pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter.
```

The macros $\protect\operatorname{pcol@imakeflushedpage}$ and $\protect\operatorname{pcol@iflushfloats}$ also use the register for scanning but for $[C^0, C^1)$ given by their arguments.

In addition \pcol@ccuse, \pcol@ifccdefined and \pcol@ccxdef refer to the register to have the control sequence \pcol@columncolor $\cdot c = \hat{\gamma}_0^c$ or \pcol@columncolor@box $\cdot c = \gamma_0^c$ where c is for the current column or for all columns depending on their invokers.

¹³³Only for logging.

\pcol@nextcol

The register \pcol@nextcol has the zero-origin ordinal d of the column to which we are switching, or in which we are staying, to be set into \pcol@currcol by \pcol@restartcolumn. The main usage of the register is to set the switching target in \pcol@switchcolumn, but other macros use it to specify the (temporary) target of \pcol@switchcol; the tallest column in \pcol@sync; 0 in \pcol@zparacol, \pcol@sptext and \endparacol; all in [0, C) but $c = \pcol@currcol$ in \pcol@visitallcols; and c in \pcol@flushclear to stay in the current column c. The other user of this register is \pcol@invokeoutput but only for logging.

\pcol@ncol \pcol@ncolleft The register \polencol has the number of columns C given as the argument of \polencol whose callee \polencol being the sole modifier of the register \polencol assigns C to the register to give safe reference to \polencol unvoked after a paracol is closed. In addition for the reference in \polencol before the first paracol, the register is initialized with zero after the declaration.

The following macros refer to the register to scan all columns $c \in [0, C)$.

\pcol@checkshipped, \pcol@output@start, \pcol@output@switch, \pcol@sync, \pcol@makeflushedpage, \pcol@freshpage, \pcol@output@end, \pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter, \pcol@visitallcols.

The register \c col@ncolleft has C_L being the number of columns in the left parallel-page if parallel-paging is in effect, or have C otherwise. Similar to C, the number C_L is given as the optional argument of \c col@zparacol and is \c globally assigned to the register by the sole modifier \c col@zparacol, unless the optional argument is not less than C which is assigned to C_L if this exception is found. The reason of the \c global assignment and the initial zero-clearing after the declaration is same as that for C, i.e., for the reference in \c coutputpage outside paracol.

The following macros examines if $C_L < C$, i.e., if parallel-paging is in effect.

\pcol@outputelt, \@outputpage, \pcol@output@start, \pcol@output@flush,
\pcol@output@clear, \pcol@makeflushedpage, \pcol@flushfloats,
\pcol@output@end, \pcol@zparacol,

In the macros listed above, \cline{CL} , \cline{CL} , \cline{CL} and \cline{CL} , \cline{CL} to their respective callees \cline{CL} to let them work on the left and right parallel-pages repsectively. The callees above also pass the pair to \cline{CL} swapcolumn to swap the scanning order of columns if column-swapping is in efect.

They also pass the pair to \pcol@buildcolseprule which then passes it to \pcol@bg@paintcolumns and \pcol@bg@paintbox by binding it to $[C_b^0, C_b^1) = [\pcol@bg@from, \pcol@bg@to)$ referred to by \pcol@bg@paint@i and its callee \pcol@bg@paint@ii to define the range of columns to be painted is $[C_b^0, C_b^1)$. Similar passing is done by (our own version of) \@outputpage, but it directly uses $[0, C_L)$ and $[C_L, C)$ as the sources and the target painting macros are \pcol@bg@paintpage, \pcol@bg@paintpage and \pcol@bg@paintbox. Note that C_b^1 is initialized to be \let-equal to C because it may be referred to without binding 134 .

The macro \pcol@addmarginpar also referes to C_L to know if the column c on which it is working on is in the left or right parallel-page, i.e., $c < C_L$ or not, to decide the margin to which a marginal note is put, and to pass $[0, C_L)$ or $[C_L, C)$ to \pcol@swapcolumn to calculate the distance to the left or right margin from the column. The examination of $c < C_L$ is also done in related macros \pcol@getmparbottom@i and \pcol@setmpbelt@i.

 $^{^{134}\}mathrm{This}$ meaningless reference has no harmful side effects.

Similar column-range specification is done for the argument pair $[C^0, C^1)$ of \pcol@setcolumnwidth invoked from \pcol@zparacol. Then the arguments are passed to the callees \pcol@setcolwidth@r or \pcol@setcolwidth@s, the latter of which also passes them to its callee \pcol@setcw@scan, to define the width of columns in $[C^0, C^1)$ and thier separators.

The other references to C are made by $\col@com@switchcolumn$ and $\col@com@switchcolumn$ to examine c < C, to wraparound C-1 to 0 for the former and to complain if $c \ge C$ for the latter.

\pcol@page

The register \pcol@page has the zero-orgin ordinal p of the page which we are in. The register is initialized to be 0 not only by \pcol@output@start to give the obvious starting point, but also by \pcol@freshpage for page flushing which clears $\Pi = \pcol@pages$ to give us another type of starting point. Then the register is incremented by \pcol@nextpage to advance one page, by \pcol@nextpelt to skip a float page, and by \pcol@startpage for a float page to be created. The other type of updates of the register is done by \pcol@restartcolumn which lets p be $\kappa_c(\beta^p)$ when we revisit the column c belonging to the page p. Note that, besides these \global updates, \pcol@flushcolumn locally updates the register to scan $\Pi = \pcol@pages$, and \pcol@freshpage also performs local updates but in more weird manner. Besides the updates discussed above, the macros \pcol@log@iii, \pcol@Log@ii, \pcol@FF, \pcol@makecol, \pcol@opcol, \pcol@setpageno, \pcol@getcurrpage, \pcol@startcolumn, \pcol@output@switch, \pcol@addmarginpar and \pcol@fntext refer to the register to know which page they are operating on.

\pcol@basepage

The register \pcol@basepage has the ordinal p_b of the base page being the oldest page not shipped out yet. The register is initialized to be 0 by \pcol@output@start and \pcol@freshpage together with \pcol@page, and then incremented by \pcol@outputelt when it ships the page p_b out. The macros \pcol@setpageno, \pcol@nextpage, \pcol@getcurrpage and \pcol@addmarginpar refer to the register in their scans of Π or Π^+ to know the zero-origin ordinal of the element for the current page p is $p-p_b$.

\pcol@toppage

The register \pcol@toppage has the ordinal p_t of the top page having the most advanced column-pages, or leading column-pages in short. The register is initialized to be 0 by \pcol@output@start and \pcol@freshpage together with \pcol@page, and then let be $p = \pcol@page$ by \pcol@startpage to start a new page p. The macros \pcol@makecol, \pcol@opcol, \pcol@startcolumn, \pcol@output@switch and \pcol@restartcolumn refer to the register to examine if they are working on a column-page in the top page, while \pcol@flushcolumn and \pcol@fntext examines if the current column-page is behind the top page. The register is also referred to by \pcol@Log@iii, \pcol@Log@ii and \pcol@FF for logging.

\pcol@footnotebase

The register $\colorspace{1mu}$ pcolorspace is let have the value of $\colorspace{1mu}$ cofootnote at the start of a paracol environment by $\colorspace{1mu}$ pcolorspace{1mu} to give the base value b_f for relative numbering of footnote done in $\colorspace{1mu}$ colorspace{1mu} and $\colorspace{1mu}$ footnoteext. The register is also referred to by $\colorspace{1mu}$ where $n_f = \colorspace{1mu}$ colorspace{1mu} where $n_f = \colorspace{1mu}$ colorspace{1mu} is the number of footnotes in the paracol environment to be closed.

\pcol@nfootnotes

The register \pcol@nfootnotes is to accumulate the number of footnotes n_f in a paracol environment. Therefore, it is zero-cleared by \pcol@zparacol, then incremented by \pcol@ifootnote and \pcol@ifootnotemark for \footnote and \footnotemark, and finally referred to by \endparacol to let \c@footnote = $b_f + n_f$.

\pcol@mcid

The register \pcol@mcid has the number of pushes of color stack by coloring commands in math mode between two consecutive invocations of \output. The register is zero-cleared by \pcol@

output because we are definitely in the main vertical mode and thus all pops corresponding to pushes in math mode must have been applied to .tex's color stack. Then the register is referred to by \pcol@set@color@push when it is invoked in math mode, to increment it and then examine if it does not exceed the limit \pcol@mcpushlimit to mean the math-mode coloring still can be made. The macro then uses the value of the register as the identifier of the push operation given to \output through an \insertion.

```
1
2 %% Register Declaration
3
4 \newcount\pcol@currcol \global\pcol@currcol\z@
5 \newcount\pcol@nextcol
6 \newcount\pcol@ncol \global\pcol@ncol\z@
7 \newcount\pcol@ncolleft \global\pcol@ncolleft\z@
8 \newcount\pcol@page
9 \newcount\pcol@basepage
10 \newcount\pcol@toppage
11 \newcount\pcol@footnotebase
12 \newcount\pcol@nfootnotes
13 \newcount\pcol@mcid
```

3.2 Switches

The second declaration group is for switches.

\ifpcol@output

The switch \ifpcol@output is true iff \pcol@output@start which turns the switch true has been invoked but \pcol@output@end which does false has not yet. Then the switch is examined by \pcol@output to detect an \output request sneaked from outside of the paracol environment. The other users \@outputpage and \pcol@reset@color@pop examine this switch to know if the macro is invoked inside or outside of paracol environment, while the macro \pcol@output@start temporarily turns the switch false when it ships out a page having preenvironment stuff only.

\ifpcol@nospan

The switch \ifpcol@nospan is true iff a page p does not have spanning stuff, i.e., $\pi^i(p) = \bot$. It is set by by \pcol@getpinfo for the examination in \pcol@ioutputelt, \pcol@makeflushedpage and \pcol@output@end.

\ifpcol@sync

The switch \ifpcol@sync is true iff \pcol@output@switch is invoked for synchronized column-switching by \switchcolumn* or its relative environment openers, or pre-flushing column height check prior to page flushing or environment closing. Therefore, the switch is \globally turned true by \pcol@iswitchcolumn and \pcol@sptext for the synchronizing column-switchinging but then temporarily turned false by \pcol@switchcol invoked by them for column-scanning and then turned true again by the macro. For pre-flushing column height check, the macro \pcol@flushclear turns the switch true. The other macro turns this switch is \pcol@output@switch at the end of which the switch is turned false to go back to the default state. The macros examining this switch are \pcol@output@switch, \pcol@putbackmvl, \pcol@sync, \pcol@invokeoutput (for logging) and \pcol@switchcol.

\ifpcol@sptextstart \ifpcol@sptext

The switch \ifpcol@sptextstart is true iff \pcol@output@switch is invoked from \pcol@sptext prior to a spanning text. That is, the switch is \globally¹³⁵ let true and then false by

 $^{^{135}}$ Not necessary to be \globally turned but we dare to do that to clearly distinguish that from the local turning in \pcol@putbackmvl.

\pcol@sptext before and after the invocation of synchronized \pcol@switchcol prior to the spanning text. Then the switch is examined by \pcol@putbackmvl after the synchronization to save the pre-spanning-text stuff, being all stuff in main vertical list prior to the synchronization, so that the spanning text is split from the stuff and is captured afterward by \pcol@makecol and/or \pcol@output@switch. The macro also locally turns the switch false if it does not follow the synchronization, i.e., its invocation is for column-scanning or is caused by presynchronization page break, to do the saving only when it follows the synchronization. The switch is also examined in \pcol@output to inhibit the warning and forced page break even when $\kappa_0(\beta^r) = \text{Qcolroom} < 1.5 \text{baselineskip}$, because we may let it have a small value when the spanning text starts near the page bottom to capture the text portion in the page by \pcol@makecol. In addition, it is examined by \pcol@switchcol to invoke \pcol@colpream·c, where c = -1 if true or c = pcol@currcol otherwise.

The macro \pcol@sptext then \globally turns another switch \ifpcol@sptext true before putting the spanning text into the main vertical list so that \pcol@makecol for the page break in the text and \pcol@output@switch for closing capture the text to place it appropriately especially when column-swapping is in effect. Then the switch is \globally turned false by \pcol@output@switch to give the default state after it broadcasts \if@nobreak, \if@afterindent and \everypar to all columns.

\ifpcol@clear

The switch \ifpcol@clear is true iff \pcol@output@switch is invoked for pre-flushing column height check, page flushing or environment closing. Therefore, the switch is turned true by \pcol@flushclear in the first case, and by \pcol@makeflushedpage in the latter two. These two macros also turned the switch false after the direct/indirect invocation of \pcol@output@switch to give the default state. The switch is examined by \pcol@output@switch and its descendants \pcol@sync, \pcol@flushcolumn and \pcol@synccolumn for synchronization, and by \pcol@invokeoutput for logging.

\ifpcol@flush

The switch \ifpcol@flush is turned true by \pcol@sync iff it finds that the page to be synchronized or to be flushed is too tall because the sum of the total height of top floats and main text in a column and that of bottom floats and footnotes in another column is larger than $\pi^h(p_t) - v^f - V_E$, where v^f is the total height-plus-depth of the page-wise footnotes if p_t has them or 0 otherwise, and V_E is the amount given by \ensurevspace in synchronization or 0 in flushing. Then the switch is examined in \pcol@sync itself to restart the tallest column if true, in \pcol@putbackmvl to check if a spanning text is really to start, in \pcol@switchcol to have a explicit page break in each column if true, and in \pcol@flushclear also to have a page break if true. The last examiner \pcol@flushclear may turn the switch true when it is invoked from \endparacol if the last page leaves deferred and non-merged page-wise footnotes for which an explicit page break is also required.

\ifpcol@outputflt

The switch \ifpcol@outputflt is used in \pcol@outputelt to know whether a float page is to be shipped out (true) or not. The switch is initialized to be true by \pcol@outputcolumns which invokes \pcol@outputelt for all $\pi(p) \in \Pi$. Then if \pcol@outputcolumns is invoked from \pcol@opcol to ship the oldest page p_b out, the switch is turned false when we visit the second non-float page. That is, all float pages following the first (oldest) page are shipped out but others are not. On the other hand, if \pcol@outputcolumns is invoked from \pcol@sync to ship out all pages including float pages in Π , the switch is kept true throughout all invocations of \pcol@outputelt.

\ifpcol@lastpage \ifpcol@lastpagesave

The switch \ifpcol@lastpage is used to know whether the following macros work on the *last* page of a paracol environment to do special operations if so.

- \pcol@combinefloats adds \textfloatsep below bottom floats of each column if any so that the floats are well seperated from the post-environment stuff.
- \pcol@sync examines V_P' instead of V_P for the pre-flushing column height check.
- \pcol@makefcolumn trys to make deferred floats as top floats.
- \pcol@makeflushedpage builds a short page of V_P' tall, leaves spanning stuff from shipout if $V_P' = \text{pcol@colht} = -\infty$ so that it becomes a float in post-environment stuff, and leaves page-wise footnotes untouched if merged footnote typesetting is in effect. This macro itself turns this switch false if \ifpcol@dfloats = true to mean one or more columns in the last page have deferred column-wise floats and thus the last page must be full size.
- \pcol@imakeflushedpage leaves the background of page-wise footnotes unpainted, and lets the depth of the last page be 0 in background painting and packing of column-pages.

The switch is initialized to be <code>false</code> by \pcol@zparacol, then turned <code>true</code> by \endparacol, and then finally turned <code>false</code> by \pcol@output@end again for float pages following the last page if any. The macro \pcol@flushcolumn saves the switch into \ifpcol@lastpagesave then turning it <code>false</code> during it works on column-pages in non-top and thus non-last pages to keep \@makecol and \pcol@makefcolumn from misunderstanding the pages are last, and then restore the switch when the macro reaches to the top page. This saving and temporary turning <code>false</code> is also done in \pcol@flushclear when it forces a page break so that the \output routine working on the broken non-last page correctly recognizes that. Another temporary turning is made by \pcol@makenormalcol but in reverse to let the switch be <code>true</code> so that its indirect callee \pcol@combinefloats puts a vertical skip of \textfloatsep below the bottom floats in pre-environment stuff.

\ifpcol@scfnote

The switch \ifpcol@scfnote is turned *true* by \pcol@fnlayout@p and \pcol@fnlayout@m (through \pcol@fnlayout@p) to indicate footnotes in all columns are merged and page-wise, while \pcol@fnlayout@c turns it *false* to make footnote typesetting column-wise, being default as well. The switch is examined by the following macros to do special operations for page-wise footnotes if it is *true*.

- \pcol@makecol shrinks \@colht and put the stretch/shrink factor of \skip\footins at the bottom of the column-page to be built by the macro if the page has footnotes. If the column-page is in the top page p_t , the macro also saves \footins into \pcol@currfoot which then will be saved into $\pi^f(p_t)$ by \pcol@startpage, or \footins is discarded otherwise
- \pcol@startcolumn, if it is invoked from \pcol@output to start a column-page in a page p, \inserts $\pi^f(p)$ through \footins, and also the deferred footnotes in Φ by \pcol@ deferredfootins, if $p = p_t$.
- \pcol@output@switch saves \footins into $\pi^f(p_t)$ if the macro is to leave a column-page in the top page, or discards it otherwise.
- \pcol@restartcolumn to restart a column-page in a page p \inserts $\pi^f(p)$ through \footins, and also the deferred footnotes in Φ by \pcol@deferredfootins, if $p = p_t$.
- \pcol@sync examines whether the total height of page-wise footnotes is too large to let them reside in the page to be synchronized or flushed as a whole.

- \pcol@zparacol redefines \footnoterule so that it refers to \textwidth rather than \columnwidth to determine the width of the rule above footnotes.
- \pcol@fntext invokes \pcol@fntextother to add the footnote given to it to Φ as a deferred footnote if $p < p_t$.
- \pcol@fntextbody lets \hsize be \textwidth rather than \columnwidth to typeset the footnote given to it.

\ifpcol@mgfnote

The switch \ifpcol@mgfnote is turned true by \pcol@fnlayout@m to indicate footnotes in the starting page and last page of a paracol environment are merged with those in pre- and post-environment stuff, while \pcol@fnlayout@p and \pcol@fnlayout@c turn it false to put them above/below the columns in the starting/last page respectively, being default as well. The switch is examined by the following macros to do special operations for merged page-wise footnotes if it is true.

- \pcol@makenormalcol leaves \footins untouched rather than putting it as a part of pre-environment stuff.
- \pcol@makeflushedpage leaves \footins untouched rather than putting it as a part of the last page of paracol if it works on the page.
- \endparacol does not let \pcol@flushclear examine the existence of deferred footnotes in pre-flushing column height check for the last page.

\ifpcol@fncounteradjustment

The switch \ifpcol@fncounteradjustment is turned true by the API macro \fincounter adjustment, which is also invoked from \pcol@fnlayout@p and \pcol@fnlayout@m (through \pcol@fnlayout@p), to let \c@footnote = $b_f + n_f$ by \endparacol. The macro \nofncounter adjustment turns the switch false to give the default state.

\ifpcol@inner

The switch \ifpcol@inner is turned false by \pcol@zparacol to mean we are outside any \vboxes, while the macro also lets \everyvbox in the paracol environment has the operation to turn the switch true so that it is true whenever we are in a \vbox. The switch is examined by \pcol@set@color@push and \pcol@icolumncolor, the former of which also turns it true if we are in restricted horizontal mode, to make an \output request for color stack manipuration and, in the former, to reserve the stack popper by \aftergroup, iff the switch is false.

\ifpcol@firstpage

The switch \ifpcol@firstpage is \globally turned true or false by \pcol@output@start if it captures pre-environment stuff as a spanning stuff or not because it is too large, respectively. Then the switch is examined by \pcol@ioutputelt or \pcol@makeflushedpage when they finds a spanning stuff to be combined to the page to be printed so as to paint the background for the color of page-wise floats unless the switch is true to mean the stuff is pre-environment one rather than floats. Then \pcol@outputelt or \pcol@makeflushedpage itself \globally turns the switch false after printing a page because we no longer have pre-environment stuff in the paracol environment we are in.

\ifpcol@havelastpage

The switch \ifpcol@havelastpage is, after intialized false, \globally turned true by \pcol@ output@end if it finds the last page of the paracol environment is connected to the post-environment stuff, or false otherwise. Then the switch is examined by (our own version of) \@outputpage which paints the background of the page to be printed iff the switch is true because a part of the page was produced by a paracol environment. Then the macro \globally turns the switch false because so far background painting should be disabled.

\ifpcol@paired

The switch \ifpcol@paired is true if the parallel-paged typesetting should be done in paired mode in which the pair of left and right parallel-pages comprises a virtual page, while it is false if non-paired to treat the left and right pages as individual ones. Therefore, the switch is \globally turned false by \pcol@yparacol when \begin{paracol} paracol} has the optional argument for the number of columns in the left parallel-page followed by *, or turned true otherwise by \paracol for giving default or by \pcol@zparacol if it finds $C_L \geq C$ to mean parallel-paging is not in effect in reality 136 .

The other macros \pcol@ioutputelt, (our own version of) \@outputpage, \pcol@output@ start, \pcol@imakeflushedpage, \pcol@iflushfloats and \pcol@output@end also refer to the switch so that, if false, they temporarily let \c@page = page(p) + 1 in building the shipout image of the right component of the parallel-page pair of the page p in order to have the appropriate page number parity for the right component. Among them, \@outputpage has another mode dependant operation, if the switch is true, to decrement \c@page by one before shipping out the right component to cancel the increment in the ship-out process of the left component. The macro \pcol@addmarginpar also examines the switch to decide the margin for marginal notes in non-paired parallel-pages. Another examiner \pcol@zparacol lets \ifpcol@swapcolumn = false only in the paracol environment to start if the switch is true because column-swapping is meaningless in non-paired parallel-paging.

\ifpcol@swapcolumn \ifpcol@swapmarginpar \ifpcol@bg@swap \ifpcol@bg@gswap The switch \ifpcol@swapcolumn, \ifpcol@swapmarginpar and \ifpcol@g@swap specify that, if *true*, columns, marginal notes, and background painting in even numbered pages are swapped, respectively. That is, \ifpcol@swapcolumn lets columns be put from right to left, \ifpcol@swapmarginpar lets marginal notes go to the opposite side from that in odd numbered pages, and \ifpcol@bg@swap makes background painting mirrored.

Besides the initial setting to let them $false \geqslant \globally$ after the declaration, the switches are \globally turned false by \globally turned for the cases in which API macro $\to \globally$ turned does not have 'c', 'm' or 'b' in its optional argument respectively, and then \globally turned true by \globally turned \globally turned by \globally turned \globally turned by \globally turned by \globally turned \globally turned by \globally turned \globally turned by \globally or 'b' respectively, or the API macro does not have the argument at all¹³⁷. The switch \globally if pool@swapcolumn is also turned \globally by \globally pool@sparacol but locally if non-paired parallel-paging is specified because column-swapping is meaningless in the environment. Another modifier is (our own version of) \globally but setting and examining the switch in this macro is also local and is to decide the ship-out order of left and right parallel-pages.

Besides the local use by \@outputpage, \ifpcol@swapcolumn is then examined by the following macros to do special operations if it is *true* and we are in an even numbered page.

- \pcol@swapcolumn to reverse the order of column visiting in \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats.
- \pcol@shiftspanning to shift a spanning text to the left edge of text area.
- \pcol@bg@paint@ii to mirror the background painting of columns and column-separating gaps.

¹³⁶The initialization to let the switch *false* is not necessary because it is examined only after the first \paracol even in the \@outputpage outside paracol environment, but we dare to do this for the sake of clearity.

¹³⁷\ifpcol@swapcolumn is also turned *true* and *false* by backward compatible API macros \swapcolumn inevenpages and \noswapcolumninevenpages respectively.

On the other hand, examiners of \ifpcol@swapmarginpar and \ifpcol@bg@swap are sole for each, namely \pcol@addmarginpar and \pcol@bg@paint@i respectively. If each switch is true and we are in an even numbered page, the former reverses \if@firstcolumn from the value having been set for non-swapping case, while the latter mirrors the background painting of the regions excepting columns and column-separating gaps.

A related switch \ifpcol@bg@@swap is let be *true* if \ifpcol@swapcolumn or \ifpcol@bg@swap is *true* and we are working on a even numbered page by \pcol@bg@swappage for mirrored background painting of columns and column-separating gaps, or other regions respectively, and then examined by \pcol@bg@paintregion@i for mirroring.

\ifpcol@bg@painted

The switch \ifpcol@bg@painted is \globally turned false at the beginning of \pcol@bg@paint@i, and then \globally turned true by \pcol@bg@paintregion if it paint the region specified by its argument, i.e., \backgroundcolor for the region is declared. Then the switch is examined by \pcol@bg@paint@i to combine the painted region with others, by (our own version of) \@outputpage and \pcol@outputpage@r to incorporate painted regions into shipout image.

\ifpcol@bfbottom

The switch \ifpcol@bfbottom is true if \@makecol puts bottom floats at the bottom of a column as done by the macro in LATEX's standard implementation, or false otherwise and thus bottom floats can be followed by footnotes as done in pLATEX. Since we know only pLATEX is exceptional, we let the switch false iff \pfmtname is defined and has pLaTeX2e in its body. The switch is examined by \pcol@measurecolumn to determine which footnotes or bottom floats determine D_P if both of them exist.

\ifpcol@dfloats

The switch \ifpcol@dfloats is true iff one or more columns (in a last page) have deferred column-wise floats. Therefore, it is turned false by \pcol@sync before it invokes \pcol@measurecolumn which turns it true when it finds a column c such that $\kappa_c(\lambda_d) \neq \emptyset$. Then the switch is examined by \pcol@makeflushedpage to make a last page $full\ size$, and by \pcol@output@end to flush these floats.

- 14 \newif\ifpcol@output \global\pcol@outputfalse
- $15 \newif\ifpcol@nospan$
- 16 \newif\ifpcol@sync \pcol@syncfalse
- 17 \newif\ifpcol@sptextstart \pcol@sptextstartfalse
- 18 $\mbox{newif\ifpcol@sptext} \pcol@sptextfalse$
- 19 \newif\ifpcol@clear \pcol@clearfalse
- $20 \neq 0$
- $21 \verb|\newif\ifpcol@outputflt|$
- 22 \newif\ifpcol@lastpage
- 23 \newif\ifpcol@lastpagesave
- $24 \verb|\newif\ifpcol@scfnote| \pcol@scfnotefalse|$
- 25 \newif\ifpcol@mgfnote \pcol@mgfnotefalse
- $27 \neq 27$
- 28 \newif\ifpcol@firstpage
- 29 \newif\ifpcol@havelastpage \global\pcol@havelastpagefalse
- 31 \newif\ifpcol@swapcolumn \global\pcol@swapcolumnfalse
- $32 \mbox{\ensuremath{\mbox{\sc Newif\sc Newif\sc Newsparginpar}}} \mbox{\sc Newif\sc Newif\sc Newif\sc Newsparginpar\sc Newsparginpar\s Newsparginpar\sc Newsparginpar\s Newsparginpar\sc Newsp$
- 33 \newif\ifpcol@bg@swapfalse
- 34 \newif\ifpcol@bg@@swap
- 35 \newif\ifpcol@bg@painted
- $36 \neq 16$

- 37 \def\reserved@a{pLaTeX2e}
- 38 \ifx\reserved@a\pfmtname \pcol@bfbottomfalse \else \pcol@bfbottomtrue \fi
- 39 \newif\ifpcol@dfloats

3.3 \dimen and \skip Registers

The next declaration group is for six \dimen and one \skip registers.

\pcol@prevdepth

The \dimen register \pcol@prevdepth is set to the depth of the last item added to the main vertical list of column c from which we switch to another column d, i.e., \prevdepth seen in \pcol@invokeoutput before \output request. The value of the register is then set into \prevdepth also by \pcol@invokeoutput after \output for the column d. The value of the register is stored in $\kappa_c(\delta)$ by \pcol@setcurrcol and then restored into the register by \pcol@igetcurrcol for the use in \pcol@invokeoutput above and in \pcol@measurecolumn, which may let the register and $\kappa_c(\delta)$ have ∞ if the column-page c is empty. The register is also updated by \pcol@synccolumn for empty main vertical list case, and by \pcol@output@end to be set into \prevdepth for the first vertical item of post-environment stuff.

\pcol@colht

The \dimen register \pcol@colht has V_P' being the height of the tallest column in the last page taking \textfloatsep below bottom floats into account if any. The register is initialized to be $-\mbox{\sc harmonic}$ by \pcol@sync and then is examined and updated in \pcol@measurecolumn to find the tallest column. Besides the internal use of this exploration, its result is referred to by \pcol@sync as the threshold of pre-flushing column height check, and by \pcol@makeflushedpage through its argument given by \pcol@output@end to know the height of multi-column stuff in the last page. The macro \pcol@makeflushedpage also lets the register have 0 if the last page has nothing but non-merged page-wise footnote. The other usage of this register is in \pcol@freshpage to keep the value of \@colht of the page made by \flushpage or \clearpage so that it is given to \@colroom = $\kappa_c(\beta^r)$ of each column c in case a column c' s.t. c' < c made another page for float columns updating \@colht.

\pcol@textfloatsep

The \dimen (not \skip) register \pcol@textfloatsep has \maxdimen if a column-page does not have synchronization points, to let top floats are inserted in usual way. If it has, the register may hold the vertical space amount inserted after top floats in a column-page instead of \textfloatsep so that, if a column only with top floats defines the first synchronization point, the space for floats are extended to the synchronization point. In this extension case, the register has the amount above biased by 10000 pt to distinguish the case from another case with ordinary top floats in which the register has non-biased \textfloatsep. In addition, if the register is less than \maxdimen including a value equal to \textfloatsep, top floats are packed in a \vbox so that stretch/shrink factor of \floatsep cannot move synchronization points. After the default setting to be \maxdimen by \pcol@zparacol and \pcol@floatplacement, the value of the register is stored in $\kappa_c(\xi)$ by \pcol@setcurrcol and then restored into the register by \pcol@igetcurrcol for the use in \pcol@makecol, \pcol@combinefloats, \pcol@cflt, \pcol@output@switch, \pcol@measurecolumn, \pcol@addflhd and \pcol@synccolumn.

\pcol@lrmargin \pcol@bg@leftmargin

The \dimen register \pcol@lrmargin is let have $\mu = \text{textwidth} - \text{linewidth}$ by \pcol@ zparacol, so that \linewidth for column c is let have $w_c - \mu$ by \pcol@invokeoutput, which also sets \parshape if $\mu > 0$.

The other usage of this register is to have the left or right margin for background painting in the alias \pcol@bg@leftmargin for strict local use in \pcol@bg@paint@i and its descendent macros for background painting. That is, the register is aliased as \pcol@bg@leftmargin by \pcol@bg@paint@i, let have left or right margin by \pcol@bg@swappage, and then referred to by \pcol@bg@pageleft.

\pagerim

The API \dimen register \pagerim has the size of page rims specified by users. Since the rims are the area for which background painting is inhibited, the register is used in area specification macros \pcol@bg@paperwidth, \pcol@bg@paperheight, \pcol@bg@pageleft and \pcol@bg@pagetop, in which the register has the negative counterpart of the specified value set by \pcol@bg@paint@i.

\pcol@topskip

The \skip register \pcol@topskip keeps the value of \topskip at \begin{paracol} for the ordinary usage of \topskip which may have 0 in the starting and last page temporarily. After the initialization by \pcol@zparacol, it is referred to by \pcol@getpinfo for pages without spanning stuff and thus pre-environment stuff, by \pcol@startpage to let \topskip and $\pi^t(p)$ has it for non-starting page p, by \pcol@output@start for the second page if it finds pre-environment stuff is too large to combine with the multi-column stuff, and by \endparacol to recover \topskip for the pages following the last page.

\belowfootnoteskip

The API \skip register \belowfootnoteskip has the amount of the space added below non-merged pre-environment footnotes. The register is initialized with the default 0 pt, and then used in \pcol@output@start to measure the room in the first page, and in \pcol@combinefootins to add the space.

- 40 \newdimen\pcol@prevdepth
- 41 \newdimen\pcol@colht
- 42 \newdimen\pcol@textfloatsep
- 43 \newdimen\pcol@lrmargin
- 44 \newdimen\pagerim \pagerim\z@
- 45 \newskip\pcol@topskip
- 46 \newskip\belowfootnoteskip \belowfootnoteskip\z@

3.4 \box Registers

The next declaration group is for the following \box registers.

\pcol@topfnotes

The \box register \pcol@topfnotes is the implementation of Φ to have the list of deferred footnotes. The register is made void by \pcol@output@start and then is made grown by \pcol@fintextother with a deferred footnote added by the macro. The macro \pcol@deferredfootins invoked from \pcol@startcolumn and \pcol@restartcolumn tries to \insert the contents of the register through \footins but may keep some of trailing ones in it if the total height of the footnotes is too large, while \pcol@output@end does the \insertion without height capping. The macro \endparacol with non-merged page-wise footnote type-setting also refers to the register to pass it to \pcol@flushclear as its argument so as to make an explicit page break if the register has some deferred footnotes.

\pcol@prespan

The \box register \pcol@prespan keeps the pre-spanning-text stuff during a spanning text is processed by T_EX and our own \output routine. That is, the macro \pcol@putbackmvl saves the contents $\kappa_0(\beta^b)$ of the column 0 to be restarted into the register instead of putting it back to the main vertical list, or makes the register \bot if the column has nothing, when the restart follows the synchronization with \ifpcol@sptextstart = true. Then the contents of the register is put back to the main vertical list together with the box having spanning text after its vertical size is registered in the list $\pi^s(p)$ of spanning text postions and heights, by \pcol@makecol when the text sees a page break, or by \pcol@output@switch when the text is completed.

\pcol@rightpage

The \box register \pcol@rightpage is used to build (a part of) the ship-out image of a right parallel-page in it. The macros;

\pcol@outputelt, \pcol@ioutputelt, \pcol@makeflushedpage, \pcol@flushfloats, \pcol@output@flush, and \pcol@output@clear

work on the register together with \@outputbox for the left parallel-page to pass both of them to (our of version of) \@outputpage. The macro \pcol@output@end also uses the register to paint the background of the empty counterpart of non-merged page-wise footnotes in it, or to make the register \perp when it have an empty last page but with spanning stuff of page-wise floats. After closing a paracol environment, the contents of the register will be shiped out by \@outputpage invoked outside paracol environment when the post-environment stuff sees a page break, or referred to by \pcol@output@start as the pre-environment stuff in the right parallel-page. This right pre-environment stuff then will be combined with column-pages in the right parallel-page by \pcol@ioutputelt or \pcol@imakeflushedpage for shipping-out, or by the latter indirectly invoked from \pcol@output@end as the last right parallel-page again. Therefore the \setbox of the register in \pcol@output@start, \pcol@makeflushedpage, \pcol@imakeflushedpage and \pcol@output@end must be done \globally^138.

\pcol@colorstack@saved

The \box register \pcol@colorstack@saved is Γ_s to keep the color context Γ^c of column c until its current column-page becomes non-empty to avoid that the column-page only has coloring \specials for color stack establishing and rewinding to let \pcol@ifempty misjudge the column-page is non-empty. It is let have γ_0^c , if defined, and Γ by \pcol@savecolorstack invoked from \pcol@startcolumn and \pcol@output@start, and from \pcol@restartcolumn through \pcol@putbackmvl when we know or find the (re)starting column-page is empty. The macro \pcol@putbackmvl also makes the \box register \bot when the restarting column-page is not empty and thus the column-page has had coloring \specials for establishing color context at its beginning. Then the register is given to \pcol@restorecst by \pcol@clearcst@unvbox to put leading coloring \specials for establishing of the column-page when we complete it by \pcol@opcol or leave from it by \pcol@output@switch.

\pcol@tempboxa

The \box register \pcol@tempboxa is used to have stuff temporarily as follows.

- The macro \pcol@buildcolseprule and its callee \pcol@buildcselt builds the column-separating rule in the register for a page to be shipped out, while its contents is put into each column-separating gap by \pcol@hfil.
- In (our own version of) \@outputpage, the register has the background painting of the (left parallel-) page, which is inserted into the ship-out image by its callee \pcol@outputpage@l through \everyvbox and its contents \pcol@outputpage@ev.
- In \pcol@scancst and its callee \pcol@iscancst to scan Γ_r^c , Γ^c or Γ_s , the sequence of (un)coloring \specials to be put into the main vertical list is build in it.

\pcol@tempboxb

The \box register \pcol@tempboxb is used in \pcol@iscancst to extract the top (last) element of Γ , Γ_r or Γ_s .

- 47 \newbox\pcol@topfnotes
- 48 \newbox\pcol@prespan \setbox\pcol@prespan\box\voidb@x
- $49 \verb|\newbox\pcol@rightpage \global\setbox\pcol@rightpage\box\voidb@x|$
- $50 \newbox\pcol@colorstack@saved$
- 51 \newbox\pcol@tempboxa
- 52 \newbox\pcol@tempboxb

 $^{^{138} \}mbox{The \global setting in \pcol@makeflushedpage}$ and \pcol@imakeflushedpage, together with \@outputbox which does not need \global assignment, is also required by the sake of simplicity in its implementation, incidentally.

3.5 \insert Register Set

The next declaration is for the following \insert register set.

\pcol@colorins

The register set \pcol@colorins is to \insert a \vbox containing a (un)coloring \special for color pushing or popping, or the definition of a new default color of the current column. In order to make it sure that an \insertion does not affect \pagetotal and is given to \output with \box255 containing the corresponding coloring \special put in the main vertical list, \count\pcol@colorins and \skip\pcol@colorins are let be 0, while \dimen\pcol@colorins is let be \maxdimen to allow a column-page to have vitually infinite number of \insertions.

The \insertion is done by \pcol@icolumncolor for a default color definition, \pcol@set@color@push for color pushing, and \pcol@reset@color@pop and \pcol@reset@color@mpop for color popping in non-math and math mode respectively. Then \inserted \vboxes are packed into \box\pcol@colorins and is given to \output as Γ_r to be scanned by \pcol@clearcolorstack to reform it as Γ , and then scanned by \pcol@restorecolorstack or saved into $\Gamma_s = \text{pcol@colorstack@saved}$ by \pcol@savecolorstack. The register is also referred to by \pcol@scancst $\langle box \rangle$ to examine if $\langle box \rangle$ is this register or \pcol@colorstack@saved, and is made Γ by \pcol@output@end after the final reestablishment of the color stack.

- 53 \newinsert\pcol@colorins
- 54 \count\pcol@colorins\z@ \skip\pcol@colorins\z@ \dimen\pcol@colorins\maxdimen

3.6 \toks Register

The last declaration is for the following \toks register.

\pcol@everyvbox

The register \pcol@everyvbox acts as \everyvbox in paracol environments. That is, by \pcol@zparacol, \everyvbox is made \let-equal to this register so that updates and references of \everyvbox is made to this register, while the real \everyvbox is let have the reference to the register and \pcol@innertrue to make \ifpcol@inner = true in every \vbox. Besides \pcol@zparacol, the register is reffered to by \pcol@restoreeveryvbox to examine if it has been \globally updated, i.e., its contents is not \pcol@dummytoken.

55 \newtoks\pcol@everyvbox

4 Logging Tools

Prior to the \definitions of macros to implement paracol's functions, we define a few macros for debug logging.

\pcol@ShowBox

The macro \pcol@ShowBox $\langle b \rangle$ puts a logging \message showing the height, depth and width of the \box (or \insert) register b, or "(VOID)" if $b=\bot$. Then, if $b\ne\bot$, b's contents is dumped into .log file making overfull intentionally by putting b into \box0 of null height, together with \vskip of 1pt if b's height is 0, with setting \vfuzz = 0.

\pcol@LogLevel \pcol@iLogLevel \pcol@Log \pcol@Log@iii \pcol@Log@ii \pcol@Log@i \pcol@Logstart \pcol@Logstart@ii \pcol@Logstart@i \pcol@Logend \pcol@Logend@ii \pcol@Logend@i \pcol@Logfn \pcol@Logfn@ii \pcol@Logfn@i

The macro \pcol@Level $\langle l_1 \rangle \langle l_2 \rangle \langle l_3 \rangle$ defines the detailedness of logging done by logging macros. It invokes \pcol@iLogLevel $\{l_i\}\{cs\}$ to let the following $\langle cs \rangle$ be $\langle cs \rangle \otimes \langle l_i' \rangle$ where l_i' is the \romannumeral representation of l_i .

- \pcol@Log $\langle cs \rangle \{m\} \langle f \rangle$ is to log the contents of the \insert register f containing footnotes which is referred to by the macro $\langle cs \rangle$ in a context shown by m. The macro \pcol@Log@ iii $(l_1=3)$ logs the detailed contents of f by $\colon Box$, while $\colon Box$ $(l_1=2)$ just shows the height of f and $\pcol@Log@i$ $(l_1=1)$ does nothing.
- \pcol@Logstart{m} and \pcol@Logend{m} put logging \messages 'S:m' and 'E:m' respectively to show the beginning and end of a procedure in the macro whose name is at the head of m, if $l_2=2$ and thus they are \left-equal to \pcol@Logstart@ii and \pcol@Logend@ii. If $l_2 = 1$, \pcol@Logstart@i and \pcol@Logend@i do nothing.
- \poolength{m} puts a logging $\mbox{message } m$ whose head is the macro name for footnotes whose information such as the ordinal number of the footnote processed by the macro may be shown in m as well, if $l_3 = 2$ and thus it is \let-equal to \pcol@Logfn@ii. If $l_3 = 1$, \pcol@Logfn@i does nothing.

```
57 %% Logging Tools
58
59 \def\pcol@ShowBox#1{%
   \ifvoid#1\message{(VOID)}%
60
61
    \else
      62
      {\vfuzz\z@ \showboxdepth\@M \showboxbreadth\@M
63
64
       \setbox\z@\vbox to\z@{\ifdim\ht#1=\z@ \vskip1\p@\fi \copy#1}}%
65
66 \def\pcol@LogLevel#1#2#3{%
    \pcol@iLogLevel{#1}{pcol@Log}%
    \pcol@iLogLevel{#2}{pcol@Logstart}%
    \pcol@iLogLevel{#2}{pcol@Logend}%
69
    \pcol@iLogLevel{#3}{pcol@Logfn}}
70
71 \def\pcol@iLogLevel#1#2{%
    \expandafter\let\expandafter\reserved@a
72
      \csname #2@\romannumeral#1\endcsname
73
    \expandafter\let\csname #2\endcsname\reserved@a}
74
75 \def\pcol@Log@iii#1#2#3{\message{\string#1{#2%
      (\number\pcol@page:\number\pcol@currcol/\number\pcol@toppage)}}%
    \pcol@ShowBox#3\message{end\string#1}}
77
78 \def\pcol@Log@ii#1#2#3{\message{\string#1{#2%
      (\number\pcol@page:\number\pcol@currcol/\number\pcol@toppage)}=\the\ht#3}}
80 \def\pcol@Log@i#1#2#3{}
81 \def\pcol@Logstart@ii#1{\message{S\string#1}}
82 \def\pcol@Logend@ii#1{\message{E\string#1}}
83 \def\pcol@Logstart@i#1{}
84 \def\pcol@Logend@i#1{}
85 \def\pcol@Logfn@ii#1{\message{\string#1}}
86 \def\pcol@Logfn@i#1{}
87 \pcol@LogLevel111
```

\pcol@F@write \pcol@F \pcol@FF

Another debugging tool is for investigating memory leak problems. Since paracol uses \insert registers for various purposes, management operations of them especially that for proper release

\pcol@F@count \pcol@F@n \pcol@Fb

\pcol@Fe

of them are crusial for the correctness of the implementation. A source of toughness in debugging *memory leak* caused by missing a release of a register back to **\Offreelist** is that the resulting shortage is revealed long after the leakage to make it hard to find the point of the leakage.

The set of macros is to help such debugging by logging the aquire and release of \insert registers into a file named $\langle job \rangle$.fls associated with \pcol@F@write where $\langle job \rangle$ is given by \jobname. After opened when paracol is loaded, the file is written by \pcol@FF{ m_a }{ m_b } with a line of the following form with text messages m_a and m_b , where $p = \pcol@page$, $c = \pcol@currcol$, $p_t = \pcol@toppage$, $m_b = \pcol@page$, and $m_b = \pcol@page$ is the cardinality of \@deferlist counted by \pcol@F@count.

```
\langle m_a \rangle (\langle p \rangle : \langle c \rangle / \langle p_t \rangle : \langle \pi \rangle) = \langle n_b \rangle \langle m_b \rangle
```

The argument $\langle m_b \rangle$ is empty when \pcol@FF is invoked from \pcol@F $\langle m_a \rangle$ for snapshot, while $\langle m_b \rangle = `<= \langle n_b \rangle$ ' when invoked from \pcol@Fe $\langle m_a \rangle$ paired by \pcol@F0 = \pcol@F@count by which the cardinality of \@freelist is given to $\langle n_b \rangle$ through \pcol@F@n and then \reserved@ a. Therefore, by the pair of \pcol@Fb and \pcol@Fe, the consumption or restitution in a series of operations surrounded by the pair is logged in the file.

In the production version, the logging is disabled of course by \letting \pcol@F and \pcol@Fe be \@gobble and \pcol@Fe write is disabled as well by a pair of \iffalse and \fi.

```
89 \iffalse
90 \newwrite\pcol@F@write
91 \immediate\openout\pcol@F@write\jobname.fls
93 \def\pcol@F#1{\pcol@FF{#1}{}}
94 \def\pcol@FF#1#2{\pcol@F@count
     \immediate\write\pcol@F@write{#1(\number\pcol@page:\number\pcol@currcol/%
       \number\pcol@toppage:\number\c@page)=\pcol@F@n #2}}
96
97 \def\pcol@F@count{{\@tempcnta\z@
       \def\@elt##1{\advance\@tempcnta\@ne}\@freelist
       \xdef\pcol@F@n{\number\@tempcnta}}}
100 \let\pcol@Fb\pcol@F@count
101 \def\pcol@Fe#1{{\let\reserved@a\pcol@F@n \pcol@FF{#1}{<=\reserved@a}}}
102 \let\pcol@F\@gobble
103 \let\pcol@Fb\relax
104 \let\pcol@Fe\@gobble
105
```

5 \output Routine

\pcol@ovf

Before giving the definitions of macros in \output routine, we define the macro \pcol@ovf invoked if \@freelist is empty on an acquision of an \insert by \@next and thus we have to abort the execution by \PackageError with a message notifying the shortage. The additional help message is \@ehb as in \@fltovf. This macro is used in \pcol@opcol, \pcol@startpage, \pcol@output@start, \pcol@output@switch, \pcol@iscancst, \pcol@savefootins, \pcol@flushcolumn, \pcol@synccolumn, \pcol@output@end and \pcol@icolumncolor.

```
106 %% \output Routine
107
108 \def\pcol@ovf{%
109 \PackageError{paracol}{Too many unprocessed columns/floats}\@ehb}
110
```

\pcol@output

The macro \pcol@output is the paracol's version of \output which is let have this macro as its sole token by \pcol@zparacol. The structure of this macro is same as that of IATEX's \output but the following replacements are made 139.

- \@specialoutput → \pcol@specialoutput to process LATEX's genuine functions including the customized marginal note placement, and paracol's own special output functions; starting first page, color context management, column-switching, page flushing with/without float flusing, and building the multi-column part of the last page.
- \@makecol → \pcol@makecol for a special care for current column-page having synchronization point and/or page-wise footnotes.
- \@opcol \rightarrow \pcol@opcol to hold the current column-page which just has completed.
- \@startcolumn \rightarrow \pcol@startcolumn to creat a new column-page. The argument \@ne is to distinguish the invocation in this macro from that in \pcol@freshpage so that the \insertions of $\pi^f(p)$ and Φ are done only when a new column-page is created with ordinary page break.

In addition, before we start the main body of \output routine, we add two operations for coloring. One is to make \set@color \let-equal to \pcol@set@color, i.e, to let it regain its original definition throughout \output routine, because no manipulation of color stack is necessary 140. The other is to zero-clear the counter \pcol@mcid because we are definitely in the main (non-internal) vertical mode and thus all push/pop pairs of the coloring in math mode have been processed.

Further, before we start the sequence for non-special \output request on page breaks, we examine if $\t view = true$ to mean $\t view$ order to cope with \output request sneaking. This sneaking happens when \begin{paracol} is at a crtical position of page breaking at which the pre-environment stuff has already exceeds \vsize but TEX cannot make the \output request for the page break at \par at the beginning of \pcol@zparacol because it sees \penalty = 10000 due to, e.g., a sectioning command just preceding \begin{paracol}. In this case, the request is postponed until TFX see a \penalty less than 10000 and thus it is made with some non-special \outputpenalty greather than -10000 when TeX sees the dummy request of \penalty = -10004 in \pcol@ invokeoutput for \pcol@output@start. At this timing, \pcol@zparacol has already let \output have \pcol@output of course but the request must be processed by original \output because it is made outside of the paracol environment which has just started. Therefore, if \forall ifpcol@output = false, we have to perform the operation sequence as the original \forall does. Furthermore, we have to take care of the fact that a few our own settings related to \output routine has already been made in \pcol@zparacol, namely \if@twocolumn = trueand \@combinefloats = \pcol@combinefloats, which should make the macros in the original sequince confused especially by the former. Therefore, we turns $\inf to sequence the sequence that the$ \@combinefloats have the original definition kept in \pcol@@combinefloats¹⁴¹ temporarily, i.e., only in the group automatically surrounding the invocation of **\output**.

Another addition is to assign \Omaxdepth to \maxdepth in order to nullify the temporary setting to 0 done in \Omaxdepth. By this assignment, in paracol environments TeX's

 $^{^{139} \}mathrm{Besides}$ the logging with \pcol@Logstart and \pcol@Logend.

¹⁴⁰Though this operation is not necessary because \everyvbox should work for any \set@color because they should be in a \vbox, we dare to do it for clearity.

 $^{^{141}}$ Though we know \pcol@combinefloats acts exactly as \@combinefloats because \pcol@zparacol initializes \pcol@textfloatsep = ∞ and \ifpcol@lastpage = false. On the other hand, we don't cancel the re\defitnition of \footnoterule because it should be \textwidth = \columnwidth outside of paracol environments.

page builder always refers to the value in $\mathbb Q$ maxdepth. Yet another addition is to add $\mathbb Q$ to short $\mathbb Q$ to the condition for the warning of too short $\mathbb Q$, because a spanning text can start near the bottom of a page with a small $\mathbb Q$ colroom less than $1.5 \times \mathbb Q$ and thus the warning is unnecessary and inappropriate when $\mathbb Q$ the specific parameters $\mathbb Q$ and $\mathbb Q$ the specific parameters $\mathbb Q$ and $\mathbb Q$ the specific parameters $\mathbb Q$ and $\mathbb Q$ are specific parameters $\mathbb Q$

```
111 \def\pcol@output{\let\par\@@par \let\set@color\pcol@set@color
     \global\pcol@mcid\z@
112
113
     \pcol@Logstart{\pcol@output\number\outputpenalty
114
       (\number\c@page:\number\pcol@currcol)}%
115
     \ifnum\outputpenalty<-\@M
116
       \pcol@specialoutput
     \else\ifpcol@output
117
       \pcol@makecol
118
119
       \pcol@opcol
120
       \pcol@startcolumn\@ne
       \@whilesw\if@fcolmade\fi{\pcol@opcol \pcol@startcolumn\@ne}%
121
122
       \@twocolumnfalse \let\@combinefloats\pcol@@combinefloats
123
       \@makecol
124
       \@opcol
125
       \@startcolumn
126
127
       \@whilesw\if@fcolmade\fi{\@opcol \@startcolumn}%
128
     \fi\fi
129
     \global\maxdepth\@maxdepth
130
     \ifnum\outputpenalty>-\@Miv
       \ifdim\@colroom<1.5\baselineskip
131
         \ifdim\@colroom<\textheight
132
           \ifpcol@sptextstart
133
              \global\vsize\@colroom
134
            \else
135
              \@latex@warning@no@line{Text page \thepage\space
136
                                        contains only floats}%
137
              \@emptycol
138
           \fi
139
140
         \else
141
            \global\vsize\@colroom
         \fi
142
143
       \else
         \global\vsize\@colroom
144
       \fi
145
146
     \else
       \global\vsize\maxdimen
147
148
     \pcol@Logend\pcol@output}
149
150
```

6 Completing Column-Page

\pcol@@makecol

The macro $\colon=0.00$ is used in $\colon=0.00$ in the macro $\colon=0.00$ is used in $\colon=0.00$ in the ship-out image of a column-page. The reason why we need our own version is that a variation of $\colon=0.00$ implements its own $\colon=0.00$ in the resulting $\colon=0.00$ implements its own $\colon=0.00$ in the resulting $\colon=0.00$ in the macro $\colon=0.00$ is that a variation of $\colon=0.00$ implements its own $\colon=0.00$ in the resulting \col

depth larger than $\mbox{\ensuremath{\mbox{0maxdepth}}}$ if the column-page has column-wise footnotes whose last line is unusually deep. To cope with the problem, this macro at first invokes $\mbox{\ensuremath{\mbox{0maxdepth}}}$ and then reshape $\mbox{\ensuremath{\mbox{0colpht}}}$ assigning $d = \mbox{\ensuremath{\mbox{0maxdepth}}}$ to $\mbox{\ensuremath{\mbox{cap}}}$ to cap its depth, unless this macro is used for the last page with d = 0 because depth of the last component of the $\mbox{\ensuremath{\mbox{0colpht}}}$.

```
151 %% Completing Column-Page
```

152

153 \def\pcol@@makecol#1{\@makecol

154 \setbox\@outputbox\vbox to\@colht{\boxmaxdepth#1\unvbox\@outputbox}}

\pcol@makecol

The macro \pcol@makecol is invoked solely from \pcol@output to build the shipping image of the current column-page which just has completed in \@outputbox. This macro has two additional functions to its original version \@makecol^{142} invoked in this macro.

First, if $\kappa_c(\xi) \neq \infty$ to mean the column-page has synchronization points, \@makecol is invoked with a special \definition of \@textbottom to put a vertical skip having 1/10000 fil as its stretch and shrink. This modification is to nullify not only finite stretches (as \raggedbottom does) but also finite shrinks possibly inserted just below the last synchronization point to move up the first visible item upward a little bit if active. Therefore, \flushbottom setting is nullified for column-pages having synchronization points and a small exceess from the bottom of a column-page cannot be absorbed by shrinks but visible at the bottom 143 . Note that the original definition of \@textbottom is saved in \pcol@textbottom before the invocation of \@makecol and is restored after that 144 .

Second, if $\c ext = true$ and c = 0 to mean a spanning text encounters a page break, we have the first half (or second or succeeding part if the text lays across three or more pages) of the text in $\c ext = 1$. Therefore, we add an element $span(H_n, h_n)$ to the tail of the list of spanning texts $\pi^s(p_t) = \c ext = 1$. Where H_n is the height of pre-spanning-text stuff in $\c ext = 1$ plus the total height of top floats calculated by $\c ext = 1$ and $\c ext = 1$ and

The addition, however, is not made if $h_n=0$ because painting its background is harmful if an extension is specified to make the region visible, while not painting or drawing a segment of column-separating rule is very natural. Note that this $h_n=0$ case includes that in which \box255 has nothing but its height-plus-depth is non-zero because of discarding leading skips of the spanning text as pre-break skips. This special case is detected by decapsulating \box255 by \unvcopy and examining the height-plus-depth of the result¹⁴⁶. Also note that the list to be added is always for the top page, i.e., $\pi^s(p_t)$ and thus we get and update it by \pcol@getcurrpinfo and \pcol@defcurrpage, because the spanning text immediately follows a synchronization point in p_t . Then we let \box255 have the pre-spanning-text stuff followed by the spanning text being the original contents of \box255, which may be shifted left by $W_T - w_c = \text{textwidth} - \text{columnwidth}$ by the macro \pcol@shiftspanning if column-swapping is in effect so that its left edge is aligned to that of the leftmost column, i.e., of the text area.

¹⁴²Not \pcol@makecol because the depth capping of \@outputbox is done by \pcol@opcol when it saves the box into $\kappa_c(\beta^b)$.

¹⁴³That is, the author gives higher priority to the perfect alignment of the items following a synchronization point.

¹⁴⁴This save/restore cannot be done by a grouping because \@makecol builds \@outputbox by local assignments.

145Since we have a synchronization point before a spanning text always, pre-spanning-text stuff or its sole contents \vbox has a vertical skip at its tail to make the its depth 0 as discussed in §11.7.

¹⁴⁶We cannot do \setbox\@cclv\vbox{\unvbox\@cclv} because it erases the effect of pre-break skip following some visible material.

The third addition is for page-wise footnotes. If they are presented in \footins, we shrink \@colht by its height plus depth by \pcol@shrinkcolbyfn and put the stretch and shrink factor of \skip\footins at the bottom of \box255 by \pcol@unvbox@cclv to remove footnotes from the column-page but keeping the stretch/shrink contribution to the page breaking by their existence. Then we save \footins into a new \insert to be referred to as \pcol@currfoot^{147} by \pcol@savefootins if $p = p_t$ so that it is saved in $\pi^f(p)$ by \pcol@startpage afterward, or simply discard the contents of \footins otherwise because $\pi^f(p)$ has already been fixed. Note that these saving/discarding make \footins void and thus \@makecol will not put footnotes.

On the other hand, if footnote typesetting is column-wise, \footins is kept unchanged so that its contents will be put by \@makecol if it has something. As for \pcol@currfoot, it should have its default value \voidb@x = \bot assigned to it beforehand, so that, if $p = p_t$, \pcol@startpage will make $\pi^f(p) = \bot$ unless page-wise footnotes are given in \footins.

```
155 \def\pcol@makecol{\let\pcol@textbottom\@textbottom
     \ifdim\pcol@textfloatsep=\maxdimen\else
156
       \def\@textbottom{\vskip\z@\@plus.0001fil\@minus.0001fil}\fi
157
     \ifpcol@sptext \ifnum\pcol@currcol=\z@
158
       \pcol@getcurrpinfo\@tempcnta\@tempdima\@tempskipa
159
       \setbox\@tempboxa\vbox{\unvcopy\@cclv}%
160
       \@tempdimb\ht\@tempboxa \advance\@tempdimb\dp\@tempboxa
161
162
       \ifdim\@tempdimb>\z@
163
         \dimen@\ht\pcol@prespan \pcol@addflhd\@toplist\pcol@textfloatsep
164
         \@cons\pcol@sptextlist{{\number\dimen@}{\number\@tempdimb}}%
165
166
       \pcol@defcurrpage{\number\@tempcnta}\pcol@spanning\pcol@footins
167
                        {\pcol@sptextlist}{\pcol@mparbottom}%
168
       \setbox\@cclv\vbox{\unvbox\pcol@prespan \pcol@shiftspanning\@cclv
169
                          \unvbox\@cclv}%
170
     \fi\fi
171
     \def\pcol@currfoot{\voidb@x}%
172
     \ifpcol@scfnote \ifvoid\footins\else
173
       \pcol@shrinkcolbyfn\@colht\footins\relax
174
       \setbox\@cclv\vbox{\pcol@unvbox@cclv\footins}%
175
176
       \ifnum\pcol@page=\pcol@toppage
         \pcol@Log\pcol@makecol{save}\footins
177
         \pcol@Fb
178
         \pcol@savefootins\pcol@currfoot
179
         \pcol@Fe{makecol(pagefn)}%
180
181
         \pcol@Log\pcol@makecol{discard}\footins
182
183
         \setbox\@tempboxa\box\footins
       \fi
184
     \fi\fi
185
     \pcol@Logstart\pcol@makecol
186
     \ifvoid\footins\else \pcol@Log\@makecol{put}\footins \fi
187
     \@makecol
188
     \pcol@Logend\pcol@makecol
189
     \let\@textbottom\pcol@textbottom}
```

\@combinefloats \pcol@combinefloats \pcol@combinefloats

The macro $\protect\operatorname{pcol@combinefloats}$ being our own version of $\protect\operatorname{qual}$ by $\protect\operatorname{pcol@combinefloats}$; and

¹⁴⁷Not in \pcol@footins because it is destroyed in \pcol@startpage just before saving operation into $\pi^f(p)$.

also used in \pcol@makenormalcol explicitly. The customization is twofold for both of top and bottom floats.

For the top floats, we invoke the original \cline{Ccflt} if $\kappa_c(\xi) = \infty$ to mean the column-page to be shipped out does not have synchronization points, or otherwise our own \cline{Ccflt} which we will discuss shortly. Prior to the invocation of \cline{Ccflt} , in addition, we let \cline{Ccflt} waxdepth so that the macro refers to the value used throughout a paracol environment instead of that modified by \cline{Ccflt} by the following sequence.

```
\label{eq:colored} $\operatorname{pcol@flushcolumn}(c) \to \operatorname{pcol@flushcolumn}(c+k) \to \operatorname{pcol@makecol} \to \operatorname{pcol@combinefloats} \to \operatorname{qcoflt} $$
```

For the bottom floats, we invoke the original $\colon 10001$ always but, if the column-page has synchronization points, we insert vertical skips of s=0 pt plus 0.0001 fil minus 0.0001 fil and -s before and after the invocation respectively. Since $\colon 10001$ fil minus 0.0001 fil and -s before and after the invocation respectively. Since $\colon 10001$ fil minus 0.0001 fil and -s before and after the invocation respectively. Since $\colon 10001$ fil minus 0.0001 fil minus 0.0001

In addition, if $\ightharpoonup = true$ to mean the column-page is in the last page, we insert $\ightharpoonup (\ightharpoonup)$ when the post-environment stuff. The switch is also true in the invocation from $\graphoonup (\ightharpoonup)$ makenormalcol for pre-environment stuff, so that the bottom floats in it are well separated from the top of multi-column stuff in the starting page.

On the other hand, the original \@combinefloats saved in \pcol@combinefloats by \pcol@zparacol is used in \pcol@output to restore the original when it finds \output request sneaking.

```
191 \def\pcol@combinefloats{%
     \global\maxdepth\@maxdepth
192
193
     \ifx\@toplist\@empty\else
       \ifdim\pcol@textfloatsep=\maxdimen \@cflt \else \pcol@cflt \fi
195
196
     \ifx\@botlist\@empty\else
       \ifdim\pcol@textfloatsep=\maxdimen \@cflb
197
198
         \setbox\@outputbox\vbox{\unvbox\@outputbox
199
          \\vskip\z@\@plus.0001fil\@minus.0001fil\%
200
201
202
        \setbox\@outputbox\vbox{\unvbox\@outputbox
203
           204
205
       \ifpcol@lastpage
206
         \setbox\@outputbox\vbox{\box\@outputbox \vskip\textfloatsep}%
207
       \fi
208
     \fi}
```

 $^{^{148}\}mathrm{The}$ insertion point is common to LATEX and pLATEX.

\pcol@cflt

The macro \pcol@cflt is invoked solely from \pcol@combinefloats if the column-page for which the macro combines the top floats has synchronization points. The macro has the same structure as LaTeX's version \@cflt but has three modifications. The first one is that the floats are packed in a \vbox rather than listed in \@outputbox to nullify the stretch and shrink of \floatsep to keep the synchronization point from moving by them 149. The second is that we use \@maxdepth instead of \maxdepth to make it clear we always use the value common throughout a paracol environment. The third is that the \textfloatsep is replaced with \pcol@textfloatsep = $\kappa_c(\xi)$ (definitely finite) which can have a value different from \textfloatsep when the float space is enlarged for synchronization. If this enlargement is required, $\kappa_c(\xi)$ is biased by 10000 pt and thus is assuredly 150 larger than 5000 pt. If so, the insertion of \topfigrule should be inhibited because it has already been inserted by \pcol@ synccolumn or there are no real floats but we only have the float for main vertical list prior to the synchronization point, or MVL-float in short.

```
209 \def\pcol@cflt{%
     \let\@elt\@comflelt
210
     \setbox\@tempboxa\vbox{}%
211
     \@toplist
212
     \setbox\@outputbox\vbox{%
213
        \boxmaxdepth\@maxdepth
214
       \box\@tempboxa
215
       \vskip-\floatsep
216
217
       \ifdim\pcol@textfloatsep>5000\p@
          \advance\pcol@textfloatsep-\@M\p@
218
219
       \else
          \topfigrule
220
       \fi
221
       \vskip\pcol@textfloatsep
222
       \unvbox\@outputbox}%
223
     \let\@elt\relax
224
     \pcol@Fb
     \xdef\@freelist{\@freelist\@toplist}%
226
227
     \pcol@Fe{cflt}%
228
     \global\let\@toplist\@empty}
```

\pcol@opcol

The macro \pcol@opcol is invoked from \pcol@output for the ordinary completed column-page built by \pcol@makecol, or from the loop creating float columns in \pcol@output or \pcol@freshpage. At first it saves the column-page of column c in \@outputbox, which \pcol@makecol or \@tryfcolumn just has built for an ordinary or float column respectively, in an \insert acquired from \@freelist by \@next, and then adds it to the tail of $S_c = \text{pcol@shipped} \cdot c$ by \@cons. In this saving operation, we add the sequence of uncoloring \specials at the bottom to clear color stack by \pcol@clearcst@unvbox giving it \@outputbox to be \unvboxed and possibly coloring \specials for the column-page's color context saved in Γ_s at the top, so that the succeeding column-page in printing order starts with its own color context. For this addition, furthermore, we let \boxmaxdepth = \@maxdepth to keep the depth capping made in the box builder from nullified \frac{151}{5}.

Then if c=0, we fix the page number of the page p having the column-page and let $\pi^p(q)$ have page(p)+(q-p) usually but possibly page(p)+2(q-p) with non-paired parallel-paging, for

 $^{^{149}\}mathrm{Maybe}$ unnecessary because of <code>\@textbottom</code> inserted by <code>\pcol@makecol</code> but ...

¹⁵⁰Though not definitely in theoretical sense.

¹⁵¹Or to apply the capping dropped from pLATEX's \@makecol, or to do nothing for the box made by \@tryfcolumn and thus being 0 deep.

all $q \in [p+1, p_t]$ by \pcol@setpageno. After that, we invoke \pcol@nextpage to let p = p' for the next column-page of c, where p' = p+1 usually but can be p+k+1 if we have consecutive k float pages from p+1.

Next, we check if the oldest page p_b is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out by the participation of the completed column-page by \c is made ready to be shipped out \c in the complete columns giving argument 0 to ship out \c is made ready to be shipped out by the participation of the complete columns giving argument 0 to ship out \c is made ready to be shipped out by the participation of the complete columns giving argument 0 to ship out \c is made ready to be shipped out by the participation of the complete columns giving argument 0 to ship out \c is made ready to be shipped out by the participation of the complete columns giving argument 0 to ship out \c is made ready to be shipped out by the participation of the complete columns giving argument 0 to ship out \c is made ready to be shipped out \c in the complete columns given by the columns give

Finally we set up the next page p by $\pol@startpage$ if $p > p_t$ meaning it is new one, or by $\pol@startpage$ otherwise, and reinitialize parameters for floats by $\pol@startpage$ floatplacement before returning to the invoker.

```
230 \def\pcol@opcol{%
     \pcol@Fb
231
     \@next\@currbox\@freelist{\global\setbox\@currbox\vbox to\@colht{%
232
         \boxmaxdepth\@maxdepth
233
         \pcol@clearcst@unvbox\@outputbox}}\pcol@ovf
234
235
     \pcol@Fe{opcol}%
     \expandafter\@cons\csname pcol@shipped\number\pcol@currcol\endcsname\@currbox
236
     \ifnum\pcol@currcol=\z@ \pcol@setpageno \fi
237
     \pcol@nextpage
238
     \pcol@checkshipped
239
     \if@tempswa \pcol@outputcolumns\z@ \fi
240
     \ifnum\pcol@page>\pcol@toppage \pcol@startpage
241
                                      \pcol@getcurrpage
242
     \fi
243
244
     \pcol@floatplacement}
245
```

\pcol@setpageno \pcol@setpnoelt

The macro \pcol@setpageno is invoked from \pcol@opcol when it proceeses the column-page of the first column c=0 to fix the page number $page(p) \leftarrow page = \colonormalcolonorma$

Since we possibly have to update $\pi(q)$ such that $q \geq p$, at first we temporarily let $\Pi^+ = (\Pi, \pi(p_t)) = \polenges \polenge empty after copying its original value into <math>\Pi' = \polenge empty$. Then we scan $\pi'(q) \in \Pi'$ for all $q \in [p_b, p_t]$ by applying \polenge empty applying \polenge empty each $\pi'(q)$ giving its five components to the macro, so that the macro updates $\pi(q)$ by \polenge defcurrpage letting $\pi^p(q) = page'(q)$ if $q \geq p$, or equivalently $p - q \leq 0$. Note that we let \copage have page'(q), but this assignment is temporary and \copage will regain the value page(p) after \polenge colone polenge in inshes.

```
246 \def\pcol@setpageno{\begingroup
    \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
247
    \let\@elt\relax \edef\reserved@a{\pcol@pages\pcol@currpage}%
248
    \global\let\pcol@pages\@empty \global\let\pcol@currpage\@empty
249
250
    \let\@elt\pcol@setpnoelt \reserved@a
251
    \endgroup}
252 \def\pcol@setpnoelt#1#2#3#4#5{%
    {\let\@elt\relax \xdef\pcol@pages{\pcol@pages\pcol@currpage}}%
    \else \pcol@defcurrpage{\number\c@page}{#2}{#3}{#4}{#5}%
255
256
      \advance\c@page\@ne
      \ifpcol@paired\else \advance\c@page\@ne \fi
257
    \fi
258
```

259 \advance\@tempcnta\m@ne}

\pcol@defcurrpage

The macro \pcol@defcurrpage{ $\pi^p(p)$ } $\langle \pi^i(p) \rangle \langle \pi^f(p) \rangle \{\pi^s(p)\} \{\pi^m(p)\}$ is invoked from \pcol@ makecol to update $\pi^s(p_t)$, \pcol@setpnoelt to update $\pi^p(p)$, \pcol@startpage to initialize a newly created page, \pcol@output@start to initialize a starting page, \pcol@output@switch to update $\pi^s(p_t)$ and/or $\pi^f(p_t)$, and \pcol@setmpbelt to update $\pi^m(p)$. The macro \xdefines \pcol@currpage letting it have the page context $\pi(p)$ given by the arguments.

260 \def\pcol@defcurrpage#1#2#3#4#5{{%

261 \let\Celt\relax \xdef\pcol0currpage{\Celt{#1}#2#3{#4}{#5}}}}

262

\pcol@nextpage \pcol@nextpelt

The macro \pcol@nextpage is invoked solely in \pcol@opcol to let p be p+k+1 where k is the number of float pages directly following p, i.e., $k=|\{q>p\,|\,p<\forall q'\leq q:\pi(q')^h<0\}|$. For this update, the macro scans $\pi(q)\in \Pi$ for all $q\in [p_b,p_t)$ applying \pcol@nextpelt to $\pi(q)$, to perform the following where p_0 is p before update and f=\if@tempswa being true at initial, to let $p\leftarrow p+k$, and then increments p to have p+k+1.

$$\langle p, f \rangle \leftarrow \begin{cases} \langle p, f \rangle & q \leq p_0 \\ \langle p+1, f \rangle & q > p_0 \land f \land \pi^i(q) \neq \bot \land \pi^h(q) < 0 \\ \langle p, false \rangle & \text{otherwise} \end{cases}$$

263 \def\pcol@nextpage{\begingroup

 ${\tt 264} \qquad \verb|\dtempcnta|pcol@page \advance|@tempcnta-\pcol@basepage|\\$

265 \@tempswatrue

266 \let\@elt\pcol@nextpelt \pcol@pages

267 \global\advance\pcol@page\@ne

268 \endgroup}

269 \def\pcol@nextpelt#1#2#3#4#5{%

270 \ifnum\@tempcnta<\z@

271 \ifvoid#2\@tempswafalse

272 \else\ifdim\dimen#2<\z@

273 \if@tempswa \global\advance\pcol@page\@ne \fi

274 \else \@tempswafalse

275 \fi\fi

276 \fi

277 \advance\@tempcnta\m@ne}

278

\pcol@checkshipped

The macro \pcol@checkshipped is invoked solely in \pcol@opcol to let \if@tempswa be true iff $S_c = \pcol@shipped c \neq \emptyset$ for all $c \in [0, C)$ to mean the oldest page p_b is ready to be shipped out.

 $279 \verb|\def|\pcol@checkshipped{| Qtempswatrue|}$

280 \@tempcnta\z@ \@whilenum\@tempcnta<\pcol@ncol\do{%

 $\verb| \expandafter\ifx\csname pcol@shipped\number\@tempcnta\endcsname\@empty| \\$

282 \@tempswafalse \fi

283 \advance\@tempcnta\@ne}}

284

\pcol@getcurrpage
 \pcol@getpelt
 \pcol@getpinfo
\pcol@getcurrpinfo

The macro \pcol@getcurrpage is invoked in \pcol@opcol, \pcol@restartcolumn, \pcol@addmarginpar, \pcol@flushcolumn and \pcol@freshpage to let;

```
\label{eq:condition} $\operatorname{\colong} = \pi^p(p) \ \operatorname{\colong} = \pi^i(p) \ \operatorname{\colong} = \pi^i(p)
```

for $p = \text{pcol@page} \in [p_b, p_t]$. To do that, the macro scans all $\pi(q) \in \Pi^+ = (\Pi, \pi(p_t))$ applying pcol@getpelt to $\pi(q) = \{\pi^p(q)\} \langle \pi^i(q) \rangle \langle \pi^f(q) \rangle \{\pi^s(q)\} \{\pi^m(q)\}$ to invoke

$$\verb|\pcol@getpinfo|{|\pi||} |\pi^i(q)| |\pi^i(q)| |\pi^s(q)| |\pi^m(q)| |\pi^m(q)| |\pi^m(q)| |\pi^i(q)| |\pi^i$$

with the following arguments for \global assignments, if q = p.

```
\langle pg \rangle = \global \colht \ \langle ts \rangle = \global \topskip
```

Then the macro \pcol@getpinfo do the obvious assignments to \pcol@spanning, \pcol@footins, \pcol@sptextlist, \pcol@mparbottom and $\langle pg \rangle$, and the following condintional assignments.

$$\langle\langle ch\rangle, \langle ts\rangle, \texttt{\ \, lifpcol@nospan}\rangle = \left\{ \begin{array}{ll} \langle \texttt{\ \, leight}, & \texttt{\ \, logl@topskip}, & true\rangle & \pi^i(q) = \bot \\ \langle \pi^h(q), & \pi^t(q), & false\rangle & \pi^i(q) \neq \bot \end{array} \right.$$

The other macro \pcol@getcurrpinfo $\langle pg\rangle\langle ch\rangle\langle ts\rangle$ is invoked in \pcol@makecol, \pcol@ startpage, \pcol@output@switch, \pcol@sync, \pcol@flushcolumn and \pcol@make flushedpage do the similar assignments using \pcol@getpinfo, but it is not for $\pi(p)$ but for $\pi(p_t) = \pcol@currpage$. The macro \pcol@getpinfo also has a direct invoker \pcol@ outputelt.

```
285 \def\pcol@getcurrpage{\begingroup
     \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
     \let\@elt\pcol@getpelt \pcol@pages\pcol@currpage
     \endgroup}
289 \def\pcol@getpelt#1#2#3#4#5{%
    \ifnum\@tempcnta=\z@
       \pcol@getpinfo{#1}#2#3{#4}{#5}%
291
                     {\global\c@page}{\global\@colht}{\global\topskip}%
292
293
     \advance\@tempcnta\m@ne}
294
295 \def\pcol@getpinfo#1#2#3#4#5#6#7#8{\pcol@nospantrue
     \gdef\pcol@spanning{#2}\gdef\pcol@footins{#3}\gdef\pcol@sptextlist{#4}%
     \gdef\pcol@mparbottom{#5}%
     #6#1\relax
298
     \ifvoid#2\relax #7\textheight #8\pcol@topskip
299
300
     \else #7\dimen#2\relax #8\skip#2\relax \pcol@nospanfalse
301
     \fi}
302 \def\pcol@getcurrpinfo{%
     \edef\reserved@a{\expandafter\@cdr\pcol@currpage\@nil}%
303
     \expandafter\pcol@getpinfo\reserved@a}
304
305
```

\pcol@floatplacement

The macro <page-header> column, $\$ and $\$ column-wise float placement at the beginning of a column-page or that of post-environment stuff. The macro lets $\$ cotath addition, the macro lets $\$ described be $\$ and then invokes $\$ maxdimen to mean the new column-page does not have synchronization point at initial.

```
306 \def\pcol@floatplacement{%
307 \global\@textfloatsheight\z@ \global\pcol@textfloatsep\maxdimen
308 \@floatplacement}
309
```

¹⁵²But \mathcal{Q}mparbottom = 0 is not done because it is meaningless now.

7 Starting New Page

\pcol@startpage

The macro \pcol@startpage is invoked from \pcol@opcol with \pcol@currpage = $\pi(p-1)$ to start a new page $p = \pcol@page$, or from \pcol@output@start with a too large preenvironment stuff or \pcol@freshpage with \pcol@currpage = {} and \c@page = page(p) to start a new page p = 0.

First, we let \pcol@firstprevdepth = \relax to mean we have (had) left from the starting page so that \pcol@output@end will be informed of that. Next we let $p_t = p$ and then, if invoked from \pcol@opcol, obtain $\pi^p(p-1)$ by \pcol@getcurrpinfo to have page(p-1) in \c@page, and let $\Pi \leftarrow \Pi^+ = (\Pi, \pi(p-1))$ with $\pi^f(p-1) = \text{pcol@currfoot}$ into which \pcol@makecol saved page-wise footnotes if any. Next we lets \c@page = page(p-1) + 1 unless non-paired parallel-paging is in effect or in other words if \ifpcol@paired = true, or \c@page = page(p-1) + 2 otherwise, by \stepcounter. Then we let \@colht = \textheight as the base value without spanning stuff, and \topskip = \pcol@topskip because the new page is the second or succeeding one built in paracol environment.

```
310 %% Starting New Page
311
312 \def\pcol@startpage{%
     \global\let\pcol@firstprevdepth\relax
     \global\pcol@toppage\pcol@page
     \ifx\pcol@currpage\@empty\else
315
       \pcol@getcurrpinfo{\global\c@page}\@tempdima\@tempskipa
316
317
       \@cons\pcol@pages
318
         {{\number\c@page}\pcol@spanning\pcol@currfoot
319
          {\pcol@sptextlist}{\pcol@mparbottom}}%
       \stepcounter{page}\ifpcol@paired\else \stepcounter{page}\fi
320
321
     \fi
     \global\@colht\textheight
322
     \global\topskip\pcol@topskip
```

Then, we build float pages if any as follows. First we invoke \d oblfloatplacement to reinitialize the parameters for page-wise float placement. In addition, we let \f odepth = 0 to nullify the setting \f odepth = 1sp possibly done by \d odblfloatplacement as discussed in the item-(2) of §1.8. Then we repeat \d otryfcolumn giving it \d odbldeferlist having page-wise floats not contributed to previous pages yet, while \f offcolmade = true meaning it builds float pages in \d outputbox. For each float page, we acquire an \f insert from \d offreelist by \d onext for $\pi^i(p_t)$ to let it have the followings to represent the float page.

$$\pi^p(p_t) = \texttt{\colored} \quad \pi^b(p_t) = \texttt{\colored} \quad \pi^h(p_t) = -\texttt{\colored} \quad \pi^t(p_t) = \texttt{\colored} \quad \pi^t(p_t) = \texttt{\colo$$

We also increment p and p_t , and also \copage by one or two according to \ifpcolopaired by \stepcounter, to let them have the values for the page following the float pages.

```
\@dblfloatplacement \let\f@depth\z@
324
325
     \@tryfcolumn\@dbldeferlist
     \@whilesw\if@fcolmade\fi{%
326
327
       \pcol@Fb
328
       \@next\@currbox\@freelist{%
329
         \global\setbox\@currbox\box\@outputbox}\pcol@ovf
330
       \pcol@Fe{startpage(fcol)}%
331
       \global\dimen\@currbox-\maxdimen
       \global\skip\@currbox\pcol@topskip
332
```

```
333 \@cons\pcol@pages{{\number\c@page}\@currbox\voidb@x{}{}}%
334 \stepcounter{page}\ifpcol@paired\else \stepcounter{page}\fi
335 \global\advance\pcol@page\@ne \global\pcol@toppage\pcol@page
336 \@tryfcolumn\@dbldeferlist}%
```

Next, we copy \@dbldeferlist containing page-wise floats which could not be included in float pages to \reserved@b, clear the list, and then scan the copied list by applying \@sdblcolelt to each list element to invoke \@addtodblcol for adding the element to \@dbltoplist or keeping it in \@dbldeferlist or \@deferlist depending on LATEX's version, as LATEX's \@startdblcolumn does. In addition, as discussed in item-(3) of §1.8, we also clear \@deferlist after saving it in \reserved@c prior to the scan, and then after the scan we concatenate \@dbldeferlist and \@deferlist to let the former have the result and restore \@deferlist from \reserved@c.

Then If this scan results in empty \@dbltoplist to mean the new page does not have any spanning stuff, we invoke \pcol@defcurrpage with $\pi^i(p_t) = \pi^f(p_t) = \bot$ and $\pi^s(p_t) = \pi^m(p_t) = \emptyset$ so that $\pi(p_t)$ represents a page perfectly empty.

```
337
     \begingroup
338
       \let\reserved@b\@dbldeferlist \let\reserved@c\@deferlist
339
       \global\let\@dbldeferlist\@empty \global\let\@deferlist\@empty
340
       \let\@elt\@sdblcolelt
341
       \reserved@b
       \let\@elt\relax \xdef\@dbldeferlist{\@dbldeferlist\@deferlist}%
342
       \global\let\@deferlist\reserved@c
343
     \endgroup
344
     \ifx\@dbltoplist\@empty
345
       \pcol@defcurrpage{\number\c@page}\voidb@x\voidb@x{}{}%
346
```

Otherwise, i.e., \d to have all page-wise floats in \d tempboxa. Then, after returning all elements to \d tempboxa in \d to be $\pi^i(p_t)$ by \d to the contents of \d tempboxa in $\pi^b(p_t)$ after removing the last vertical skip \d then adding \d then adding \d the vertical skip \d then the removing the last vertical skip \d after removing the last vertical skip \d and then adding \d then represent the page with spanning stuff which makes the height of each column \d colht shrunk from its initial value \t the series of \d addtodblcol.

$$\pi^p(p_t) = \texttt{\colored} \quad \pi^h(p_t) = \texttt{\colored} \quad \pi^t(p_t) = \texttt{\colored} \quad \pi^f(p_t) = \bot \\ \pi^s(p_t) = \emptyset \quad \pi^m(p_t) = \emptyset$$

Finally, regardless of the existence of the page-wise floats, we let \polinimes to mean the top page does not have any page-wise footnotes, so far if footnote typesetting is page-wise, or never otherwise.

```
347
     \else
       \setbox\@tempboxa\vbox{}%
348
       \begingroup
349
         \let\@elt\@comdblflelt
350
351
         \@dbltoplist
352
         \let\@elt\relax
         \pcol@Fb
353
         \xdef\@freelist{\@freelist\@dbltoplist}%
354
         \pcol@Fe{startpage(dbltop)}%
355
356
         \global\let\@dbltoplist\@empty
357
         \pcol@Fb
         \Onext\Ocurrbox\Ofreelist{\global\setbox\Ocurrbox\vbox{%
358
```

```
\unvbox\@tempboxa \vskip-\dblfloatsep \dblfigrule
359
           \vskip\dbltextfloatsep}}\pcol@ovf
360
         \pcol@Fe{startpage(spanning)}%
361
         \global\dimen\@currbox\@colht
362
363
         \global\skip\@currbox\pcol@topskip
         \pcol@defcurrpage{\number\c@page}\@currbox\voidb@x{}{}%
364
365
       \endgroup
     \fi
366
     \gdef\pcol@footins{\voidb@x}}
367
368
```

8 Shipping Page Out

\pcol@outputcolumns

The macro \pcol@outputcolumns $\langle all \rangle$ is invoked from \pcol@opcol with $\langle all \rangle = 0$ to ship out the page p_b and float pages following it if any, or \pcol@sync with $\langle all \rangle = 1$ to ship out all pages in Π . It copies $\Pi = \pcol@pages$ into $\Pi' = \pcol@pages$ and clear Π once to remove pages shipped out from it. Then, after initializing $f_o = \pcol@pages$ are true to ship out (the first) ordinary page and $f_f = \pcol@outputflt = true$ to ship out float pages (following the first page), it scans all $\pi(q) \in \Pi'$ applying \pcol@outputelt $\langle all \rangle$ to $\pi(q)$ to ship it out or keep it in Π .

```
369 %% Shipping Page Out
370
371 \def\pcol@outputcolumns#1{\begingroup
372 \def\@elt{\pcol@outputelt#1}\@tempswatrue \pcol@outputflttrue
373 \let\reserved@b\pcol@pages \gdef\pcol@pages{}%
374 \reserved@b
375 \endgroup}
```

\pcol@outputelt

 $376 \ensuremath{ \mbox{def\pcol@outputelt#1#2#3#4#5#6{\%} }$

377 \setbox\@outputbox\box\voidb@x

 $378 \pcol@getpinfo{#2}#3#4{#5}{#6}\c@page\@tempdima\@tempskipa$

Then, we do one of the followings according to h and f_o .

• *h* < 0

On the other hand if $f_f = false$, we simply return $\pi(q)$ back to Π .

```
379
     \ifdim\@tempdima<\z@
       \ifpcol@outputflt
380
         \def\pcol@bg@floatheight{\pcol@bg@textheight}%
381
         \setbox\@outputbox\vbox to\textheight{%
382
           \pcol@bg@paintbox{Ff}\unvbox\pcol@spanning}%
383
384
         \pcol@Fb
         \@cons\@freelist\pcol@spanning
385
         \pcol@Fe{outputelt(spanning)}%
386
387
         \ifnum\pcol@ncolleft<\pcol@ncol
           \setbox\pcol@rightpage\vbox to\textheight{%
388
              \ifpcol@paired\else \advance\c@page\@ne \fi
389
              \pcol@bg@paintbox{Ff}\vfil}%
390
         \fi
391
       \else
392
         \@cons\pcol@pages{{#2}#3#4{#5}{#6}}%
393
394
```

• $h \ge 0 \land f_o = true$

It means q is a non-float page to be shipped out. If $\langle all \rangle = 0$, we let $f_o = false$ to keep succeeding non-float pages from being shipped out. Then we build the ship-out image of the right parallel-page q in \pcol@rightpage by \pcol@ioutputelt giving it the box and the column range $[C_L,C)$ if $C_L < C$ to mean parallel-paging, and then that of the left parallel-page in \@outputbox by \pcol@ioutputelt again but giving it $[0,C_L)$ and \@outputbox. Note that the right-first left-second order is essential, because in the process to build right parallel-page we have to examine the existence of $\pi^i(q)$ and $\pi^f(q)$ and then refer to their height and depth to make the region corresponding to them blank, while the boxes of these \inserts are made void in the building process of the left parallel-page obviously.

Then after the ship-out image building, we $\$ lobally let $\$ ifpcol@firstpage = false to tell $\$ col@ioutputelt and $\$ pcol@makeflushedpage that the pages they build are no longer first of a paracol environment and thus $\pi^i(q)$ should have page-wise floats rather than pre-environment stuff hereafter.

```
395
     \else\if@tempswa
396
       \ifnum#1=\z@ \@tempswafalse \fi
397
       \ifnum\pcol@ncolleft<\pcol@ncol
          \pcol@Logstart{\pcol@outputelt{right}}%
398
         \pcol@ioutputelt\pcol@ncolleft\pcol@ncol\pcol@rightpage
399
         \pcol@Logend{\pcol@outputelt{right}}%
400
401
       \pcol@Logstart{\pcol@outputelt{left}}%
402
       \pcol@ioutputelt\z@\pcol@ncolleft\@outputbox
403
       \pcol@Logend{\pcol@outputelt{left}}%
404
405
       \global\pcol@firstpagefalse
    • h \ge 0 \land f_o = false
```

It means q is a non-float page to be kept. Therefore, we let $f_f = false$ to keep float pages following it from being shipped out. Then we return $\pi(q)$ to Π by \Qcons.

```
406 \else

407 \pcol@outputfltfalse

408 \@cons\pcol@pages{{#2}#3#4{#5}{#6}}%

409 \fi\fi
```

Finally, if \emptyset outputbox $\neq \bot$ to mean $\pi(q)$ is to be shipped out, we invoke \emptyset outputpage to do it and increment p_b to let it has q+1. Note that since we have let \emptyset and indirect references to it in \emptyset outputpage are correctly done. Also note that the \emptyset lobal increment of it by ∞ if \emptyset or \emptyset in \emptyset invoked from \emptyset invoked from \emptyset or \emptyset or by \emptyset or by \emptyset or by \emptyset invoked from \emptyset otherwise.

```
410 \ifvoid\@outputbox\else
411 \global\advance\pcol@basepage\@ne \@outputpage
412 \fi}
413
```

\pcol@ioutputelt

The macro $\polenoise \polenoise \polenoise$

After opening a $\begin{subarray}{l} \begin{subarray}{l} \begin{s$

Next, we put materials to be shipped out in the box b as follows. First, if $\pi^f(q) \neq \bot$ to mean the page q has page-wise footnote, we paint their background with $B_{\{N,n\}}$ by \pcol@bg@paintbox letting the basic height \pcol@bg@footnoteheight of the paining region $R_{\{N,n\}}$ be the height-plus-depth of $\pi^f(q)$. We do the painting at this earliest stage of the image building in order to use the left-top corner of the text area where we are now at as the origin for painting, and to let the region may be overlaid by those of columns and column-separating gaps. We also let $h = \pi^h(q) = \texttt{Qtempdima}$ shrunk by the height-plus-depth by \pcol@shrinkcolbyfn.

```
414 \def\pcol@ioutputelt#1#2#3{\setbox#3\vbox to\textheight{%
415 \ifpcol@paired\else\ifnum#1=\z@\else \advance\c@page\@ne \fi\fi
416 \ifvoid\pcol@footins\else
417 \def\pcol@bg@footnoteheight{\@elt{\ht\pcol@footins}\@elt{\dp\pcol@footins}}%
418 \pcol@bg@paintbox{\n}%
419 \pcol@shrinkcolbyfn\@tempdima\pcol@footins\relax
420 \fi
```

Second, if $f_{ns} = false$ to mean $\pi(q)$ has spanning stuff in $\pi^b(q)$, we do one of the followings.

- If $C^0=0$ to mean the target is the left parallel-page, $\pi^b(q)$ is put by \unvbox, painting its background with $B_{\{F,f\}}$ by \pcol@bg@paintbox letting the basic height \pcol@bg@floatheight of the paining region $R_{\{F,f\}}$ be the height-plus-depth of $\pi^b(q)$ if q is not the first page and thus $\pi^b(q)$ has page-wise floats. We also return the \insert $\pi^i(q)$ to \@freelist by \@cons.
- If $C^0 \neq 0$ to mean right parallel-page and q is the first page, \pcol@rightpage has pre-environment stuff in the right parallel-page. Therefore, we simply put the box but making its height and depth equal to those of $\pi^b(q)$, without painting because the box has already been painted, and with \nointerlineskip to prevent baseline-skip insertion below the box.
- Otherwise, i.e., $C^0 \neq 0$ and q is not the first page, we put an empty box whose height and depth equal to those of $\pi^b(q)$ by \pcol@phantom, with painting as done for floats in the left parallel-page and with \nointerlineskip.

Note that after putting spanning stuff and/or painting the background, we temporarily increment \text{topmargin} by the height-plus-depth of $\pi^b(q)$, so that painting macros for columns,

column-separating gaps and spanning texts assume the top edge of column area as that of text area when they extend the top edges of their regions upward to the page top.

```
\ifpcol@nospan\else
421
       \def\pcol@bg@floatheight{%
422
         \@elt{\ht\pcol@spanning}\@elt{\dp\pcol@spanning}}%
423
       \@tempdimb\ht\pcol@spanning \advance\@tempdimb\dp\pcol@spanning
424
       \int \frac{1}{z} dx
425
         \ifpcol@firstpage\else \pcol@bg@paintbox{Ff}\fi
426
427
         \pcol@Fb
428
         \@cons\@freelist\pcol@spanning \unvbox\pcol@spanning
429
         \pcol@Fe{ioutputelt(spanning)}%
430
       \else\ifpcol@firstpage
431
         \ht\pcol@rightpage\ht\pcol@spanning
432
         \dp\pcol@rightpage\dp\pcol@spanning
         \box\pcol@rightpage \nointerlineskip
433
434
         \pcol@bg@paintbox{Ff}\pcol@phantom\pcol@spanning \nointerlineskip
435
       \fi\fi
436
437
       \advance\topmargin\@tempdimb
438
```

Third, we invoke $\col@buildcolseprule$ giving it h being $\pi^h(q)$ but possibly shrunk by page-wise footnotes, the column range $[C^0,C^1)$, and $\colorebrack{Qmaxdepth}$ to mean q is non-last page, to draw a column-separating rule possibly broken by the speces for spanning texts in the box $\colorebrack{pcol@tempboxa}$ and to paint the backgrounds of columns, column-separating gaps and spanning text in the box $\colorebrack{Qtempboxa}$ which we put into b immediately.

Fourth, we put a \hbox of \textwidth wide having \hboxes of $w_c = \coloredge column width c$ wide containing σ_c followed by \hss for all $c \in [C^0, C^1)$, where $\sigma_c = \box \cdot s_c(q)$ being the first element removed from S_c by \@next and then returned to \@freelist by \@cons if it is not \bot , or \voidb@x otherwise. We separate \hboxes of σ_c by making each \hbox preceded by \pcol@@hfil being \relax for the first one and the macro \pcol@hfil for others giving it an argument $c^g = \pcol@colsepid \in \{c, c-1\}$ which we discuss shortly to put a gap of $g_{cg} = \pcol@columnsep \cdot c^g$ wide optionally having a column-separating rule and being painted.

Note that the scanning order of $c \in [C^0, C^1)$ is usually ascending of course, but is descending if column-swapping is specified and $page(q) \mod 2 = 0$. For this ordering, we invoke $\colored{\colore$

```
439
     \pcol@buildcolseprule\@tempdima#1#2\@maxdepth \unvbox\@tempboxa
     \hb@xt@\textwidth{%
440
       \let\pcol@@hfil\relax
441
       \@tempcnta#1\relax \@whilenum\@tempcnta<#2\do{%
442
443
         \pcol@swapcolumn\@tempcnta\@tempcntb#1#2\relax
444
         \expandafter\@next\expandafter\@currbox
           \csname pcol@shipped\number\@tempcntb\endcsname
445
           \relax{\let\@currbox\voidb@x}%
446
         \ifvoid\@currbox\else
447
448
           \pcol@Fb
           \@cons\@freelist\@currbox
449
           \pcol@Fe{ioutputelt(page)}%
450
451
452
         \expandafter\@tempdima
```

```
453 \csname pcol@columnwidth\number\@tempcntb \endcsname
454 \pcol@@hfil \hb@xt@\@tempdima{\box\@currbox\hss}%
455 \edef\pcol@@hfil{\noexpand\pcol@hfil{\pcol@colsepid}}%
456 \advance\@tempcnta\@ne}}%
```

Fifth, if $\pi^f(q) \neq \bot$ to mean the page q has page-wise footnotes, we put them at the bottom of \@outputbox by \pcol@putfootins, and return $\pi^f(q)$ to \@freelist, if $C^0=0$ meaning left parallel-page. Otherwise for the right parallel-page, we simply put an empty box whose height and depth equal to those of $\pi^f(q)$ by \pcol@phantom, preceded by a vertical skip of \skip· $\pi^f(q)$ and then \nointerlineskip to inhibit baseline skip insertion above the box, and followed by null \vskip as done in \pcol@putfootins.

Sixth and finally 153 , we let \boxmaxdepth = \@maxdepth to cap the depth of b which we are now closing, as done for each column-page and as expected to be applied to page-wise footnotes.

```
\ifvoid\pcol@footins\else
457
       \int \frac{1}{z} dx
458
          \pcol@Log\pcol@outputelt{output}\pcol@footins
459
         \pcol@putfootins\pcol@footins
460
         \pcol@Fb
461
         \@cons\@freelist\pcol@footins
462
         \pcol@Fe{ioutputelt(footins)}%
463
464
          \vskip\skip\pcol@footins \nointerlineskip
465
466
         \pcol@phantom\pcol@footins \vskip\z@
       \fi
467
468
     \fi
     \boxmaxdepth\@maxdepth}}
```

\pcol@phantom

The macro $\polenoise{colored}$ is used in $\polenoise{colored}$ in the argument box b being a kind of page-wise stuff, into $\polenoise{colored}$ for the right parallel-page whose left counterpart has b in it. That is, the macro is used to make a region corresponding to b blank. To put the empty box, we locally let $\polenoise{colored}$ have it setting its height and depth to those of b and then put it.

```
470 \def\pcol@phantom#1{{% 471 \setbox\@tempboxa\ht\@tempboxa\ht#1\dp\@tempboxa\dp#1\box\@tempboxa}}
472
```

\pcol@buildcolseprule \pcol@buildcselt@S \pcol@buildcselt The macro \pcol@buildcolseprule $\langle H_{n+1}\rangle\langle C^0\rangle\langle C^1\rangle\langle d\rangle$ is used in \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to build a box containing column-separating rule possibly broken by spanning texts and to paint backgrounds of columns and column-separating gaps for $c \in [C^0, C^1)$ and spanning texts in the last page (d = 0) or non-last page (d = 0) p having column-pages of H_{n+1} tall where $n = |\pi^s(p)|$.

For initializing the drawing and painting process, we let $\mathbb{Q} = H_0 + h_0 = 0$, $\polegofrom, \polegofole = (C_b^0, C_b^1) = (C^0, C^1)$, and make boxes $b_r = \polegofole = 0$ for the rule and $b_b = \mathbb{Q} = \mathbb$

¹⁵³Not necessary to be finally, but we placed this assignment at the end of the box to make it clear the depth capping is only for the box.

 h_i if $H_i + h_i < H_{n+1}$ to mean the spanning text is non-last, or $(H_{n+1} - H_i) + d$ if last to fill the narrow strip of $d = \mathbb{Q}$ and $d = \mathbb{Q}$ tall below the text for non-last pages.

Then we scan $\pi^s(p)$ again but applying \pcol@buildcselt $\langle H_i \rangle \langle h_i \rangle$ to each element $span(H_i, h_i)$ to do the followings.

- 1. To b_r , add a vertical rule whose height is $H'_i = H_i (H_{i-1} + h_{i-1})$ and width is \columnseprule if $H'_i > 0$, and then a vertical skip of h_i , as the rule segment between (i-1)-th and i-th spanning texts. Note that H_i and h_i are represented in the form of integers and thus we need sp to use them as dimensions.
- 2. To b_b , add painted backgrounds for all columns $c \in [C^0, C^1)$ and column-separating gaps $c \in [C^0, C^1-1)$ by $\polebg@paintcolumns$ defining their regions $R^c_{\{c,g\}}(i)$ by letting common top edge position $y_0 = \polebg@columntop = H_{i-1} + h_{i-1}$ and common height $y_1 y_0 = \polebg@columnheight = H'_i$, if $H'_i > 0$. Also add painted background for the i-th spanning text by $\polebg@paintbox$ as we did for under-painting but this time the region is $R_s(i)$.
- 3. Let $\ensuremath{\texttt{Qtempdimb}} = H_i + h_i$ for the next element $span(H_{i+1}, h_{i+1})$.

Then if $H'_{n+1} > 0$, we add the last rule segment of H'_{n+1} tall to b_r , and add painted backgrounds for columns and column-separating gaps as done in the step 2 above but letting $y_1 - y_0 = H'_{n+1} + d$ to let the common bottom edge of the their regions reach the bottom of text area for non-last pages.

```
473 \def\pcol@buildcolseprule#1#2#3#4{%
474
     \@tempdima#1\relax \dimen@#4\relax
     \let\pcol@bg@from#2\relax \let\pcol@bg@to#3\relax
475
     \setbox\pcol@tempboxa\vbox{}\setbox\@tempboxa\vbox{}%
476
     \let\@elt\pcol@buildcselt@S \pcol@sptextlist
478
     \@tempdimb\z@ \let\@elt\pcol@buildcselt \pcol@sptextlist
479
     \let\@elt\relax \advance\@tempdima-\@tempdimb
     \ifdim\@tempdima>\z@
480
481
       \setbox\pcol@tempboxa\vbox{\unvbox\pcol@tempboxa
         \hrule\@height\@tempdima\@width\columnseprule}%
482
       \setbox\@tempboxa\vbox{\unvbox\@tempboxa
483
         \let\@elt\relax
484
         \edef\pcol@bg@columntop{\number\@tempdimb sp}%
485
486
         \edef\pcol@bg@columnheight{%
487
           \Qelt{\number\Qtempdima sp}\Qelt{\number\dimenQ sp}}%
488
         \pcol@bg@paintcolumns}%
489
     fi
   \def\pcol@buildcselt@S#1#2{%
490
491
     \setbox\@tempboxa\vbox{\unvbox\@tempboxa
       \let\@elt\relax
492
       \def\pcol@bg@spanningtop{\@elt{#1sp}}%
493
       \advance\@tempdima-#1sp\relax \advance\@tempdima-#2sp\relax
494
495
       \advance\dimen@\@tempdima
       \edef\pcol@bg@spanningheight{\@elt{#2sp}%
496
         \ifdim\@tempdima>\z@\else \@elt{\number\dimen@ sp}\fi}%
497
       \pcol@bg@paintbox{S}}}
499
   \def\pcol@buildcselt#1#2{%
500
     \@tempdimc#1sp \advance\@tempdimc-\@tempdimb
501
     \setbox\pcol@tempboxa\vbox{\unvbox\pcol@tempboxa
       \ifdim\@tempdimc>\z@ \hrule\@height\@tempdimc\@width\columnseprule \fi
502
```

```
503
       \vskip#2sp}%
     \setbox\@tempboxa\vbox{\unvbox\@tempboxa
504
       \let\@elt\relax
505
       \edef\pcol@bg@columntop{\number\@tempdimb sp}%
506
507
       \edef\pcol@bg@columnheight{\@elt{\number\@tempdimc sp}}%
       \ifdim\@tempdimc>\z@ \pcol@bg@paintcolumns \fi
508
       \def\pcol@bg@spanningtop{\@elt{#1sp}}%
509
       \advance\@tempdima-#1sp\relax \advance\@tempdima-#2sp\relax
510
       \advance\dimen@\@tempdima
511
       \edef\pcol@bg@spanningheight{\@elt{#2sp}%
512
         \ifdim\@tempdima>\z@\else \@elt{\number\dimen@ sp}\fi}%
513
       \pcol@bg@paintbox{s}}%
514
     \@tempdimb#1sp \advance\@tempdimb#2sp\relax}
515
516
```

\pcol@hfil

The macro \pcol@hfil\langle c\rangle is used in \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to separate column c+1 and c or c and c+1 according as the columns are swapped or not in the page the caller macros are building. If \columnseprule = r > 0, the macro puts the followings; a horizontal space of $g_c/2 = \text{pcol@columnsep} \cdot c/2$ followed by a skip -r/2 to nullify the width of the rule; the rule in \pcol@colseprulecolor according as the former is defined or not, i.e., \colseprulecolor[mode] \{color\}[c]\$ is declared or not; and $g_c/2$ again but preceded by -r/2. On the other hand if r=0, we simply put a space of g_c . Note that the skips of $g_c/2$ and g_c are accompanied by 1 fil inifinit stretch to avoid underfull when $\sum_{c=C^0}^{C^1-2}(w_c+g_c)+w_{C^1-1}< W_T$ where $(C^0,C^1)=\{(0,C_L),(C_L,C)\}$, due to arithmetic errors in calculations of w_c and g_c^{154} .

```
517 \def\pcol@hfil#1{{%}}
     \@tempdima\csname pcol@columnsep#1\endcsname\relax
518
519
     \ifdim\columnseprule>\z@
       \hskip.5\@tempdima\@plus1fil\relax
520
       \hskip-.5\columnseprule
521
       \@ifundefined{pcol@colseprulecolor#1}%
522
         {\pcol@colseprulecolor}{\@nameuse{pcol@colseprulecolor#1}}%
523
       \copy\pcol@tempboxa \hskip-.5\columnseprule
524
       \hskip.5\@tempdima\@plus1fil\relax
525
     \else \hskip\@tempdima\@plus1fil\relax
526
     fi}
527
```

\pcol@@outputpage \@outputpage The macro \@outputpage, being our own version of LATEX's one kept in \pcol@outputpage, ships out a page p or parallel-page pair in p. The reason why we redefine this macro is that we need a few special operations for parallel-paging and background painting outside of paracol environments. Therefore, the macro is not only used in our own macros \pcol@outputelt, \pcol@output@start, \pcol@output@flush, \pcol@output@clear, \pcol@flushfloats and \pcol@output@end, but also in LATEX's \@opcol and \@doclearpage^{155} invoked from our own or LATEX's \output routine.

First we calculate $H_M' = \text{topmargin} + \text{headheight} + \text{headsep}$ to place the origin of background painting at the top edge of text area in what LATEX assumes as a page, i.e., shifted 1 inch down from the real page. Then if \ifpcol@output = true to mean this macro is used

 $^{^{154}}$ It is assured the sum of w_c and g_c cannot exceed W_T even with arithmetic errors and thus overfull never occurs.

¹⁵⁵And possibly in \@outputdblcol if double-column typesetting is done outside paracol.

in a paracol environment, we build the painted backgrounds of left and right parallel-pages in $\colored{pcolored}$ and $\colored{pcolored}$ and $\colored{pcolored}$ and $\colored{pcolored}$ by putting a vertical skip of H'_M , and invoking $\colored{pcolored}$ pcolored paintpage with the setting ($\colored{pcolored}$ pcolored pcolored paints backgrounds of regions $R_a^{[c]}$ for all $a \in \{T, B, L, R, C, S, t, b, l, r\}$ and $c \in [C_b^0, C_b^1)$, and for b_r we temporarily increment page(p) by one if non-paired parallel-paging is in effect.

Otherwise, i.e., if \ifpcol@output = false indicating outside use, we build the painted backgrounds in b_l and b_r similarly but with the following differences; background painting is done if \ifpcol@havelastpage = true to mean the page to be shipped has the last page of closed paracol as its part and \set@color \neq \relax to mean some coloring package is loaded; page background painting is done by \pcol@bg@Qpaintpage because \pcol@bg@paintpage is not available outside paracol environments; the background of post-environment stuff is painted by \pcol@bg@Qpaintbox for the region $R_{\{P,p\}} = [(0,W_T)(H_B,H_T)]$ where $H_B = \text{pcol@bg@preposttop} \in \{\text{pcol@bg@preposttop@left}, \text{pcol@bg@preposttop@right}\}$ having the bottom edge of the last paracol environment (having right parallel-page for b_r). In addition, we examine if \pcol@rightpage $\neq \bot$ to mean the right parallel-page was built by \pcol@output@end when the last paracol environment was closed and, if so, make the box \textheight tall adding \vfil to its bottom.

Then regardless of \ifpcol@output, we do the followings; let the height and depth of b_l and b_r be 0 because they cannot occupy any real spaces in the ship-out image; temporarily let \ifpcol@swapcolumn = false if page(p) is odd, $C_L = C$ to mean parallel-paging is not in effect¹⁵⁶, parallel-paging is done in non-paired mode¹⁵⁷, or we are outside paracol environments and the page does not have anything produced in environments. That is, we let \ifpcol@swapcolumn = true if the page has something produced by a paracol environment, column-swapping and parallel-paging are specified for the (last) environment¹⁵⁸, and the page number is even. Note that a page may have two or more (last pages of) paracol environments whose parallel-paging style can be inconsistent including the case some of them are not parallel-paged. If this inconsistency happens the page is shipped out following the style of the last environment. Also note that even if the last environment is not parallel-paged, the right parallel-page kept in \pcol@rightpage is assuredly shipped out.

Then if column-swapping is in effect, we ship out the right parallel-page at first by \pcol@ outputpage@r and then the left one by \pcol@outputpage@l to swap the left and right. Otherwise, the ship-out order is normal and thus the invocation order is \pcol@outputpage@l then \pcol@outputpage@r. Note that if non-paired parallel-paging is in effect, the page number to given to \pcol@outputpage@r as its argument is page(p) + 1 if it is the second one, i.e., not swapped, while the argument in other cases and of \pcol@outputpage@l are always page(p). Then finally, we \globally let \ifpcol@havelastpage = false because so far the next page does not have paracol's last page especially when we are outside it, let \pcol@bg@preposttop@left and \pcol@bg@preposttop@right have 0 because, if we are outside, the next pre-environment stuff should start from the top of a page, and let $\mathcal{M} = \pcol@mparbottom@out$ be $\mathcal{M}_0 = \pcol@mparbottom@zero$ because so far we have no marginal notes given in paracol environments¹⁵⁹.

529 \let\pcol@@outputpage\@outputpage

 $^{^{156}}$ Since the assignments of C_L and C in \pcol@zparacol are \global and they are not nodified anywhere else, examining their equality outside paracol environments is safe and meaningful.

 $^{^{157}}$ We need this examination because $\ifpcol@swapcolumn = false$ for non-paired parallel-paging is made locally by $\col@sparacol$.

¹⁵⁸Column-swapping may be enabled *after* the last paracol environment was closed but we consider the enablement is effective for the page having the environment.

 $^{^{159}}$ This assignment in a paracol environment is meaningless because \mathcal{M} is meaningless too, but not harmful.

```
530 \def\@outputpage{\begingroup
     \@tempdima\topmargin \advance\@tempdima\headheight \advance\@tempdima\headsep
     \ifpcol@output
532
       \setbox\pcol@tempboxa\vtop{\vskip\@tempdima \global\pcol@bg@paintedfalse
533
        \let\pcol@bg@from\z@ \let\pcol@bg@to\pcol@ncolleft
534
        \pcol@bg@paintpage}%
535
       \ifpcol@bg@painted \@tempswatrue \else \@tempswafalse \fi
536
       \setbox\@tempboxa\vtop{\vskip\@tempdima \global\pcol@bg@paintedfalse
537
538
         \ifpcol@paired\else \advance\c@page\@ne \fi
         \let\pcol@bg@from\pcol@ncolleft \let\pcol@bg@to\pcol@ncol
539
         \pcol@bg@paintpage}%
540
541
     \else
       \def\reserved@a{\vskip\@tempdima \global\pcol@bg@paintedfalse
542
         \ifpcol@havelastpage \ifx\set@color\relax\else
543
           \pcol@bg@@paintpage \pcol@bg@@paintbox{Pp}%
544
         fi\fi}%
545
       \setbox\pcol@tempboxa\vbox{%
546
         \let\pcol@bg@preposttop\pcol@bg@preposttop@left
547
         \let\pcol@bg@from\z@ \let\pcol@bg@to\pcol@ncolleft \reserved@a}%
548
       \ifpcol@bg@painted \@tempswatrue \else \@tempswafalse \fi
549
       \setbox\@tempboxa\vbox{\ifpcol@paired\else \advance\c@page\@ne \fi
550
         \let\pcol@bg@preposttop\pcol@bg@preposttop@right
551
         \let\pcol@bg@from\pcol@ncolleft \let\pcol@bg@to\pcol@ncol
552
         \reserved@a}%
553
       \ifvoid\pcol@rightpage\else
554
         \pcol@Logstart{\@outputpage{rightset}}%
555
         \setbox\pcol@rightpage\vbox to\textheight{\unvbox\pcol@rightpage \vfil}%
556
         \pcol@Logend{\@outputpage{rightset}}%
557
       \fi
558
559
     \fi
     \ht\pcol@tempboxa\z@ \dp\pcol@tempboxa\z@
560
     \ht\@tempboxa\z@ \dp\@tempboxa\z@
561
     \ifodd\c@page
562
                                                     \pcol@swapcolumnfalse \fi
     \ifnum\pcol@ncolleft<\pcol@ncol\else
                                                     \pcol@swapcolumnfalse \fi
563
     \ifpcol@output\else \ifpcol@havelastpage\else \pcol@swapcolumnfalse \fi\fi
564
     \@tempcnta\c@page
565
     \ifpcol@paired\else \advance\@tempcnta\@ne
                                                     \pcol@swapcolumnfalse \fi
566
567
     \ifpcol@swapcolumn \pcol@outputpage@r\c@page \pcol@outputpage@l\@tempcnta
568
                         \pcol@outputpage@1\c@page \pcol@outputpage@r\@tempcnta
569
     \fi
     \global\pcol@havelastpagefalse \gdef\pcol@bg@preposttop@left{0pt}%
570
571
     \global\let\pcol@bg@preposttop@right\pcol@bg@preposttop@left
     \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
572
     \endgroup}
573
574
```

\pcol@outputpage@l \pcol@outputpage@r \pcol@outputpage@ev The macro \pcol@outputpage@1 $\langle page \rangle$, used solely in our own version of \@outputpage, at first lets \c@page have $\langle page \rangle$ which definitely has the value that \c@page had when we start \@outputpage. That is, even when this macro is invoked after \pcol@outputpage@r due to swapped parallel-paging, this assignment cancels the increment of \c@page done in IATEX's \@outputpage or in other word \pcol@outputpage because in this case parallel-pages are paired. Then we make \@themargin \let-equal to \evensidemargin if two-side typesetting is in effect and \c@page is even, or to \oddsidemargin otherwise for the reference in \pcol@outputpage@ev as shown shortly.

Next, if background painting took place in \lozenge outputpage, we let \trianglerighteq everyvbox have the macro invocation \LaTeX col@outputpage@ev $\lozenge b_l \lozenge$ to be expanded to the following sequence so that they are the leading materials in the \backprime box to be \thickspace shipout; examination if the document is processed by a Japanese \LaTeX named platex and then, if so, a control sequence \thickspace yoko to put materials naturally; the painted background b_l shifted right by \thickspace @themargin; \thickspace nointerlineskip to inhibit \thickspace baselineskip insertion after b_l ; emptying \thickspace everyvbox to ensure nothing will be inserted into internal \thickspace vboxes; and the assignment of \thickspace yoko to \thickspace let it be \thickspace relax if necessary. This trick with \thickspace everyvbox is necessaryូ160 because b_l should be put \thickspace before \thickspace pcol@@outputpage puts the page header, or the header would be overlaid by regions, e.g., \thickspace R $_{\{t,T\}}$ in natural cases.

The tricky elements to handle \yoko in the sequence is necessary for pIATEX whose \@outputpage has \yoko as the first element of the \vbox to be \shipout, because \yoko must be the first element of a box but our \everyvbox to put background would make it nonfirst. That is by the tricky elements, the \vbox should have \yoko as the first element from \everyvbox and then that put by pIATEX's \@outputpage is nullified by \let\yoko\relax in the \everyvbox just for the \vbox to be shipped out. On the other hand in ordinary IATEX, \yoko does not appear in the \vbox or is modified. The examination of the use of pIATEX is also trickily done by comparing the expansion results of \meaning\yoko and \string\yoko. Since the former results in the tokens "\yoko" which \string\yoko gives us iff \yoko is a primitive of underlying TEX being pTEX if so, the comparison should give us equality iff pIATEX is in use¹⁶¹.

Then we invoke \pcol@Coutputpage being (p)IATEX's original version of \Coutputpage to ship out \Coutputbox finally.

The macro \pcol@outputpage@r $\langle page \rangle$ performs similar operations but it does them only when \pcol@rightpage $\neq \bot$ to mean we are in an paracol environment with parallel-paging or outside it but in the page in which it resides. Other differences are as follows; $\langle page \rangle$ can be page(p)+1 for non-paired right parallel-pages; \@outputbox is locally made \let-equal to \pcol@rightpage prior to the invocation of \pcol@outputpage; and b_r is given to \pcol@outputpage@ev as its argument.

```
575 \def\pcol@outputpage@l#1{%
     \pcol@Logstart{\@outputpage{left}}%
     \global\c@page#1\relax
577
     \let\@themargin\oddsidemargin
578
     \if@twoside\ifodd\c@page\else \let\@themargin\evensidemargin \fi\fi
     \if@tempswa \everyvbox{\pcol@outputpage@ev\pcol@tempboxa}\fi
580
     \pcol@@outputpage
     \pcol@Logend{\@outputpage{left}}}
583 \def\pcol@outputpage@r#1{%
     \begingroup
584
585
     \ifvoid\pcol@rightpage\else
586
       \global\c@page#1\relax
       \let\@outputbox\pcol@rightpage
587
       \pcol@Logstart{\@outputpage{right}}%
588
       \let\@themargin\oddsidemargin
589
       \if@twoside\ifodd\c@page\else \let\@themargin\evensidemargin \fi\fi
590
       \ifpcol@bg@painted \everyvbox{\pcol@outputpage@ev\@tempboxa}\fi
591
       \pcol@@outputpage
       \pcol@Logend{\@outputpage{right}}%
593
594
     \fi
```

 $^{^{160} \}mathrm{Unless}$ we rewrite **\@outputpage**.

¹⁶¹Unless some other TEX has a primitive named \yoko. This examination is more strict than that with \pfmtname for \ifpcol@bfbottom.

```
595 \endgroup}
596 \def\pcol@outputpage@ev#1{%
597 \edef\reserved@a\meaning\yoko}\edef\reserved@b\\string\yoko}%
598 \ifx\reserved@a\reserved@b \yoko\fi
599 \moveright\@themargin\box#1\nointerlineskip \everyvbox{}%
600 \ifx\reserved@a\reserved@b \let\yoko\relax \fi}
601
```

9 Starting New Column-Page

\pcol@startcolumn

The macro \polesize{loss} is invoked from \polesize{loss} with f=1 and \polesize{loss} freshpage with f=0 to start a new column-page. This macro has two additional functions to \polesize{loss} loss to $\polesize{l$

First, if the page p in which the new column-page resides has page-wise footnotes in $\pi^f(p)$ = \pcol@footins because the column is not the leading one, we temporarily shrink \@colht and \@colroom by the space required to put $\pi^f(p)$ by \pcol@shrinkcolbyfn during the trial of deferred float placement, remembering the existence of the footnotes by letting \@tempdimb = -\skip\pcol@footins which should be 0 otherwise. This shrinkage is essentially required when $p < p_t$ because $\pi^f(p)$ has been fixed to be a part of p and thus deferred floats cannot push footnotes down to succeeding pages. In the case of $p = p_t$, the shrinkage is also desirable to avoid unnecessary pushing down of footnotes which TFX has decided to be in p.

Then after trying put deferred floats in the column-page by \mathfrak{T}_p and \mathfrak{T}_p trynextcolumn as done in LaTeX's \mathfrak{T}_p to \mathfrak{T}_p . If it is has some footnoes, by letting \mathfrak{T}_p to the page break of the column-page. That is, if $p < p_t$ the \mathfrak{T}_p the \insertion is to keep the vertical space for $\pi^f(p)$ in the building process of the column-page in p because any page-wise footnotes cannot be added to p any more, and thus $\pi^f(p)$ is preserved until the page p is shipped out. On the other hand if $p = p_t$, page-wise footnotes in p can grow further and thus \mathfrak{T}_p inserted footnotes will be captured again by \mathfrak{T}_p to \mathfrak{T}_p . Therefore, if $p = p_t$, we release $\pi^f(p)$ to \mathfrak{T}_p to \mathfrak{T}_p .

Then if $p=p_t$, we also \insert deferred footnotes in Φ until their total height reaches \@colht by \pcol@deferredfootins if f=1 to mean this macro is invoked from \pcol@output^{162}. Note that the deferred footnote \insertion in the case of f=0 will be done afterward when \pcol@freshpage does \pcol@restartcolumn at its tail. Also note that \pcol@deferredfootins examines if \@tempdimb = 0 to mean $\pi^f(p) = \bot$ and thus \skip\footins should be taken into account in its extraction of the footnotes from Φ .

Then after restoring \colonormal{Qcolht} and canceling the temporary shrinkage of $\colonormal{Qcolroom}$, we invoke \colorstack to save column-page's color context into Γ_s so that coloring $\colonormal{Qcolloon}$ specials to reestablish Γ_s will be put at its top if it has something when we leave it.

```
602 %% Starting New Column Page
603
604 \def\pcol@startcolumn#1{%
605 \@tempdima\@colht \@tempdimb\z@
606 \ifvoid\pcol@footins\else
607 \pcol@shrinkcolbyfn\@colht\pcol@footins\@tempdimb
608 \fi
609 \global\@colroom\@colht
610 \@tryfcolumn\@deferlist
```

¹⁶² The \insertion of $\pi^f(p)$ also requires f=1 but this examination is redundant because $\pi^f(p)=\bot$ definately if f=0.

```
\if@fcolmade\else
611
       \pcol@trynextcolumn
612
       \ifpcol@scfnote \ifnum#1>\z@
613
         \ifvoid\pcol@footins\else
614
           \edef\pcol@currfoot{\pcol@footins}%
615
           \pcol@getcurrfoot\copy
616
           \pcol@Log\pcol@startcolumn{insert}\footins
617
           \insert\footins{\unvbox\footins}%
618
619
           \ifnum\pcol@page=\pcol@toppage
620
              \pcol@Fb
              \@cons\@freelist\pcol@footins
621
              \pcol@Fe{startcolumn(pagefn)}%
622
           \fi
623
         \fi
624
         \ifnum\pcol@page=\pcol@toppage
625
           \pcol@deferredfootins\pcol@startcolumn \fi
626
627
     \fi
628
629
     \advance\@tempdima-\@colht
630
     \global\advance\@colroom\@tempdima
631
     \global\advance\@colht\@tempdima
     \pcol@savecolorstack}
632
```

\pcol@trynextcolumn

The macro \pcol@trynextcolumn is invoked from \pcol@startcolumn and \pcol@flush column to try to move deferred floats in \@deferlist into \@toplist or \@botlist. The body of this macro is perfectly equivalent to the \else part of \if@fcolmade in IATEX's \@startcolumn.

```
633 \def\pcol@trynextcolumn{\begingroup
634 \let\reserved@b\@deferlist
635 \global\let\@deferlist\@empty
636 \let\@elt\@scolelt
637 \reserved@b
638 \endgroup}
639
```

10 Background Painting

\pcol@bg@from \pcol@bg@to

The control sequence pair (\pcol@bg@from, \pcol@bg@to) = (C_b^0, C_b^1) are made \let-equal to $(0, C_L)$ or (C_L, C) by \pcol@buildcolseprule and \@outputpage for background painting of columns and column-separating gaps, and referred to by column scanning loops in \pcol@bg@paint@ii and \pcol@bg@columnleft. The control sequence \pcol@bg@to is also referred to by \pcol@bg@paint@ii to decrement it by one temporarily so that the loop in \pcol@bg@paint@ii scans $c \in [C_b^0, C_b^1-1)$ rather than $[C_b^0, C_b^1)$. Since this decrement is done whenever a painting macro is used regardless some setting of C_b^1 , \pcol@bg@to has default setting with C to avoid unbound reference at the decrement. Note that since this decrement is done in a \vbox and an appropriate setting must have been done if C_b^1 is referred in \pcol@bg@paint@ii, this decrement and default setting are safe.

```
640 %% Background Painting
641
642 \let\pcol@bg@to\pcol@ncol
```

\pcol@bg@paintpage \pcol@bg@gaintcolumns \pcol@bg@gaintcolumns \pcol@bg@paintbox \pcol@bg@gaintbox The macros \pcol@bg@@paintpage, \pcol@bg@@paintcolumns and \pcol@bg@@paintbox{A} are made \let-equal to their interface counterparts \pcol@bg@paintpage, \pcol@bg@paint columns and \pcol@bg@paintbox by \pcol@zparacol if some coloring package has been loaded. Otherwise, these interface macros are \let-equal to \relax for first two and \@gobble for the last, so that macros in \output routine freely use them unaware of coloring capability. One exception is in \@outputpage which uses \pcol@bg@@paintpage and \pcol@bg@@paintbox explicitly when it is outside paracol environments, examining the availability of coloring.

The macro \pcol@bg@paintpage and \pcol@bg@paintpage are used in \@outputpage to paint backgrounds of regions $R_a^{[c]}$ for all $a \in \{T, B, L, R, G, C, t, b, l, r\}$ and $c \in [C_b^0, C_b^1)$ for a = C while $c \in [C_b^0, C_b^1 - 1)$ for a = G. Therefore, the macro invokes \pcol@bg@paint@ii(ab){A_g}{A_g}, letting $A_b = \text{TBLR}$, $A_g = \text{G}$ and $A_c = \text{C}$ in the first invocation and then $A_b = \text{tblr}$ and $A_g = A_c = \emptyset$ in the second.

The macro \pcol@bg@paintcolumns is used in \pcol@buildcolseprule and \pcol@buildcselt to paint backgrounds of regions $R_g^c(i)$ for $c \in [C_b^0, C_b^1 - 1)$ and $R_c^c(i)$ for $c \in [C_b^0, C_b^1)$. Therefore, the macro invokes \pcol@bg@paint@i with \pcol@bg@paint@ii giving it $A_b = \emptyset$, $A_g = g$ and $A_c = c$.

The macro \pcol@bg@paintbox{A} is used in the following macros with A shown in the parantheses to paint the backgrounds of regions $R_{\{a_1,a_2\}}$ where $(a_1,a_2) \in \{(S,s),(F,f),(N,n),(P,p)\}$.

The macro \@outputpage also uses the function but \pcol@bg@@paintbox explicitly with A = Pp. Therefore \pcol@bg@@paintbox invokes \pcol@bg@paint@i with \pcol@bg@paint@i giving it $A_b = A$ and $A_g = A_c = \emptyset$.

```
643 \def\pcol@bg@@paintpage{%
644 \pcol@bg@paint@ii{%
645 \pcol@bg@paint@ii{TBLR}{G}{C}\pcol@bg@paint@ii{tblr}{}{}}}
646 \def\pcol@bg@@paintcolumns{\pcol@bg@paint@ii{\pcol@bg@paint@ii{}{g}{c}}}
647 \def\pcol@bg@@paintbox#1{\pcol@bg@paint@ii{\pcol@bg@paint@ii{#1}{}{}}}
```

\pcol@bg@paint@i

The macro \pcol@bg@paint@i{body} is used in \pcol@bg@paintpage, \pcol@bg@paint columns and \pcol@bg@paintbox to paint backgrounds by a sequence of \pcol@bg@paint@ii specified in $\langle body \rangle$. The painted background is built in \@tempboxa being a \vtop having a null \vskip as its first element so that everything put in the box is below its reference point at its top. Then, before invoking \pcol@bg@paint@ii in $\langle body \rangle$, we do the followings; \globally let \ifpcol@bg@painted = false to indicate so far any painted background are produced; make \pcol@bg@leftmargin \let-equal to \pcol@lrmargin to use this \dimen register locally with the more appropriate alias; negate \pagerim locally to calculate H_T easily; decrement C_b^1 by one locally for the column scanning loop for $c \in [C_b^0, C_b^1-1)$ in \pcol@bg@paint@ii; and \offinterlineskip to inhbit inter-line \baselineskip insertion in the box. Then after the invocation of the sequence of \pcol@bg@paint@ii in $\langle body \rangle$ and closing the box, we let the height, depth and width of the box be 0 so that it does not occupy any real space in the outer box in which the box is put. Finally, if \ifpcol@bg@painted = true meaning that some painted backgrounds are built in the box, we put the box into the outer box surrounding it by \nointerlineskip to inhibit inter-line \baselineskip insertion before and after it.

649 \def\pcol@bg@paint@i#1{%

```
\lambda \setbox\@tempboxa\vtop{\vskip\z@
\lambda \global\pcol@bg@paintedfalse
\let\pcol@bg@leftmargin\pcol@lrmargin
\lambda \pagerim-\pagerim \advance\pcol@bg@to\m@ne
\lambda \offinterlineskip #1}%
\ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa\z@
\ifpcol@bg@painted \nointerlineskip \fi}
```

\pcol@bg@paint@ii

The macro \pcol@bg@paint@ii{ A_b }{ A_g }{ A_c } appears only in the argument of \pcol@bg@paint@i used in \pcol@bg@@paintpage, \pcol@bg@@paintcolumns and \pcol@bg@@paintbox to paint backgrounds of regions R_a for $a \in A_b \subseteq \{T, B, L, R, S, F, N, P, t, b, l, r, s, f, n, p\}$, R_a^c for $a \in A_g \subseteq \{G, g\}$ and $c \in [C_b^0, C^1 - 1)$, and R_a^c for $a \in A_c \subseteq \{C, c\}$ and $c \in [C_b^0, C_b^1)$.

First we invoke \pcol@bg@swappage with \ifpcol@bg@swap to let \pcol@bg@leftmargin and \ifpcol@bg@swap have values accorging to \ifpcol@bg@swap, \if@twoside and the parity of page(p). Then we invoke \pcol@bg@paintregion $\langle a \rangle \langle c \rangle$ for all $a \in A_b$ and c = -1 to paint the background of R_a . Second, we invoke \pcol@bg@swappage again but with \ifpcol@swapcolumn instead of \ifpcol@bg@swap, and \pcol@bg@paintregion as well but for $a \in \{A_g, A_c\}$ and $c \in [C_b^0, C_b^1 - 1)$. Third and finally, we make yet another invocation of \pcol@bg@paintregion for $a \in A_c$ and $c = C_b^1 - 1$.

```
657 \def\pcol@bg@paint@ii#1#2#3{%
    \pcol@bg@swappage\ifpcol@bg@swap\fi
658
659
    \Otfor\reservedOb:=#1\do{\pcolObgOpaintregion\reservedOb\mOne}%
660
    \pcol@bg@swappage\ifpcol@swapcolumn\fi
    661
       \pcol@currcol\pcol@bg@from \@whilenum\pcol@currcol<\pcol@bg@to\do{%
662
663
        \pcol@bg@paintregion\reserved@b\pcol@currcol
664
        \advance\pcol@currcol\@ne}}%
    \@tfor\reserved@b:=#3\do{\pcol@bg@paintregion\reserved@b\pcol@currcol}}
```

\pcol@bg@swappage

The macro \pcol@bg@swappage $\langle if \rangle$ \fi is used solely in \pcol@bg@paint@ii but twice with $\langle if \rangle = \ensuremath{\mbox{\mbox{olifpcol@bg@swap}}}$ and then with $\langle if \rangle = \ensuremath{\mbox{\mbox{olipcol@bg@swap}}}$ corrections according to the truth values of $\langle if \rangle$ and \iffthereorder{\mbox{olifotwoside}} and the parity of page(p) of the page p for which background painting is taking place. That is, they are let have the values as follows.

```
\begin{split} W &= \begin{cases} \texttt{\ \ } \texttt{\ } \texttt{\ \ } \texttt{\ } \texttt{\
```

Note that $W_P - (W + W_T + 2 in)$ means the right margin width minus 1 in with given left margin width W, and thus $W_M = \pcol@bg@leftmargin + 1$ in gives us the right margin width we need in mirrored background painting.

```
666 \def\pcol@bg@swappage#1#2{%
667 \pcol@bg@leftmargin\oddsidemargin \pcol@bg@@swapfalse
668 \ifodd\c@page\else
669 \if@twoside \pcol@bg@leftmargin\evensidemargin \fi
670 #1% \ifpcol@{bg@swap,swapcolumn}
671 \pcol@bg@@swaptrue
672 \advance\pcol@bg@leftmargin\textwidth \advance\pcol@bg@leftmargin2in
673 \advance\pcol@bg@leftmargin-\paperwidth
```

```
674 \pcol@bg@leftmargin-\pcol@bg@leftmargin
675 #2% \fi
676 \fi}
677
```

\pcol@bg@paintregion \pcol@bg@paintregion@i The macro $\color=0$ by $\color=0$ but as many times as $|A_b| + |A_g|(C_b^1 - C_b^0 - 1) + |A_c|(C_b^1 - C_b^0)$ to paint background region $R_a^{[c]}$ specified by $\color=0$ with color $B_a^c = \color=0$ by $\color=0$ and $\color=0$ by $\color=0$ by

If R_a^c or R_a is defined, the painted background is built in $\mathbf{etempboxa}$ with \mathbf{vtop} having null vertical skip at its top and by $\mathbf{pcol@bg@paintregion@i}\{F_x\}\{F_y\}\{F_w\}\{F_h\}$ where the arguments are defined in the body of the macro $\mathbf{pcol@bg@@}\cdot a$ and thus we need triple $\mathbf{expandafter}$ to give them to the macro. Prior to the invocation of the macro, we let $\mathbf{expandafter}$ have $a\cdot \mathbf{e}\cdot c$ if B_a^c is defined for $a\in \{G,C,g,c\}$, or a otherwise definitely for $a\notin \{G,C,g,c\}$.

Then \pcol@bg@paintregion@i calculates $x_0 = \text{Qtempdima}, y_0 = \text{Qtempdimb}, x_1 = \text{Qtempdimc}$ and $y_1 = \text{dimen@ of the region } R_a^{[c]}$ by \pcol@bg@calculate $\langle z \rangle \langle z_0 \rangle \{F\}$ giving it $(z,z_0,F) \in \{(x_0,0,F_x),(y_0,0,F_y),(x_1,x_0,F_w),(y_1,y_0,F_h)\}$, where (x_0,y_0) and (x_1,y_1) is the left-top and right-bottom corner of the painting region in the text-area coordinate, i.e., left-right and top-down coordinate whose origin is at the left-top corner of the left-most column. Next we modify $\{x,y\}_{\{0,1\}}$ for extension by \pcol@bg@addext $\langle z \rangle \{s\} \{d\}$ with $(z,s,d) \in \{(x_0,`-`,1),(y_0,`-`,t),(x_1,\emptyset,r),(y_1,\emptyset,b)\}$.

Now we have $[(x_0,y_0)(x_1,y_1)]$ and thus, if not mirrored, we place $R_a^{[c]}$ at (x_0,y_0) by a vertical skip of y_0 and shifting a \hbox for the region right by x_0 by \moveright, and paint the box putting a \vrule of (x_1-x_0) wide and (y_1-y_0) tall, letting \current@color have $B_r^{[c]} = \poolebg@colr\cdot a'$ and then invoking \pooleget@color being the orinigal definition of \set@color. On the other hand if mirroring is to be done, the region should be $[(W_T-x_1,y_0)(W_T-x_0,y_1)]$ and thus the shift amount for \moveright of the \hbox is (W_T-x_1) .

Then after \pcol@bg@paintregion@i finshes its work, \pcol@bg@paintregion lets the switch \ifpcol@bg@painted = true because we painted $R_a^{[c]}$, lets the height, depth and width of \@tempboxa be 0 to make it a phantom, and then put it into the outside box opened by \pcol@bg@paint@i. On the other hand, if neither B_r^c nor B_r defined to mean the background painting of the region is not specified, we do nothing.

```
678 \def\pcol@bg@paintregion#1#2{%
    \@ifundefined{pcol@bg@color@#1@\number#2}%
679
       {\def\reserved@a{\#1}}{\edef\reserved@a{\#1@\number\#2}}\%
680
     \@ifundefined{pcol@bg@color@\reserved@a}\relax
681
682
       {\setbox\@tempboxa\vtop{\vskip\z@
683
         \expandafter\expandafter\expandafter
           \pcol@bg@paintregion@i\csname pcol@bg@@#1\endcsname}%
684
685
        \global\pcol@bg@paintedtrue
       \ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa\z@ \box\@tempboxa}}
686
  \def\pcol@bg@paintregion@i#1#2#3#4{%
687
     \pcol@bg@calculate\@tempdima\z@{#1}%
     \pcol@bg@calculate\@tempdimb\z@{#2}%
689
     \pcol@bg@calculate\@tempdimc\@tempdima{#3}%
690
     \pcol@bg@calculate\dimen@\@tempdimb{#4}%
691
     692
     \pcol@bg@addext\@tempdimb{-}{t}\pcol@bg@addext\dimen@{}{b}%
693
694
     \vskip\@tempdimb
695
    \ifpcol@bg@@swap
      \advance\@tempdima-\@tempdimc \@tempdima-\@tempdima
696
```

```
\advance\@tempdimc-\textwidth \@tempdimc-\@tempdimc
697
       \moveright\@tempdimc\hbox{%
698
         \advance\dimen@-\@tempdimb
699
         \edef\current@color{\@nameuse{pcol@bg@color@\reserved@a}}\pcol@set@color
700
         \vrule\@width\@tempdima\@height\dimen@}%
701
702
     \else
       \moveright\@tempdima\hbox{%
703
         \advance\@tempdimc-\@tempdima \advance\dimen@-\@tempdimb
704
         \edef\current@color{\@nameuse{pcol@bg@color@\reserved@a}}\pcol@set@color
705
         \vrule\@width\@tempdimc\@height\dimen@}%
706
     fi
707
708
```

\pcol@bg@calculate \pcol@bg@advance \pcol@bg@negative \pcol@bg@nadvance \pcol@bg@dimen The macro $\colorspace{10cm} colorspace{10cm} colorspace$

The macro makes \pcol@bg@dimen \let-equal to z and \@elt to \pcol@bg@advance, lets $z=z_0$, and then does what is specified in F. Therefore, \@elt\(f\) appearing directly or indirectly in F does \advance\(z\)\(z\)\(f\) for the accumulation. On the other hand, \pcol@bg@negative makes \@elt \let-equal to \pcol@bg@nadvance to let \@elt\(f\) do \advance\(z\)\(z\)\-\(f\) for subtraction, does F^- , and then remake \@elt = \pcol@bg@advance. Note that f may be expanded to a negative amount having '-' its beginning to results in \@elt\(f\) expanded to \advance\(z\)\(-\(f'\)\) with some positive amount f', but this double negation is legitimate in TEX and is equivalent to \advance\(z\)\(z'\)\(f'\)\). The macro \pcol@bg@negative is used in the following macros.

\pcol@bg@ext@inf@1, \pcol@bg@ext@inf@r, \pcol@bg@ext@inf@t, \pcol@bg@@t, \pcol@bg@@D, \pcol@bg@@P.

```
709 \def\pcol@bg@calculate#1#2#3{\let\pcol@bg@dimen#1\relax
710 \let\Qelt\pcol@bg@advance \pcol@bg@dimen#2\relax #3}
711 \def\pcol@bg@negative#1{\let\Qelt\pcol@bg@nadvance #1\relax
712 \let\Qelt\pcol@bg@advance}
713 \def\pcol@bg@advance#1{\advance\pcol@bg@dimen#1\relax}
714 \def\pcol@bg@nadvance#1{\advance\pcol@bg@dimen-#1\relax}
```

\pcol@bg@addext
\pcol@bg@ext@inf@l
\pcol@bg@ext@inf@r
\pcol@bg@ext@inf@t
\pcol@bg@ext@inf@b

The macro $\pcol@bg@addext\langle z\rangle\{s\}\{d\}$ is used only in $\pcol@bg@paintregion@i$ but four times with $(z,s,d) \in \{(x_0,`-',1),(y_0,`-',t),(x_1,\emptyset,r),(y_1,\emptyset,b)\}$, to perform extension on a $\dimen \ register \ z$.

First the macro gets $e = \pcol@bg@ext@\cdot d\cdot @\cdot a' \in e_a^{[c]}(\{x,y\}^{\{+,-\}})$ where $a' = \pcol@bg@ext@\cdot d\cdot @\cdot a' \in e_a^{[c]}(\{x,y\}^{\{+,-\}})$ where $a' = \pcol@bg@ext@inite extension, we let <math>z \leftarrow z \pm e$ according to s, i.e. + if $s = \emptyset$ while - if s = `-`. Otherwise, i.e., $e \geq 9000$ pt for a infinite extension, let e' be the value shown below by invoking $\pcol@bg@ext@inf@\cdot d$

$$e' = \begin{cases} -(W_M - W_R) & d = \mathbf{1} \\ W_P - (W_M - W_R) & d = \mathbf{r} \\ -(H_M - H_R) & d = \mathbf{t} \\ H_P - (H_M - H_R) & d = \mathbf{b} \end{cases}$$

where $W_M - W_R$ is specified by \pcol@bg@pageleft and $H_M - H_R$ by \pcol@bg@pagetop. Then we let $z = e' \pm (e - 10000 \,\text{pt})$ according to s again, i.e., move z inside by $(10000 \,\text{pt} - e)$ from e'.

```
716 \def\pcol@bg@addext#1#2#3{%
     \dimen@ii\@nameuse{pcol@bg@ext@#3@\reserved@a}\relax
     \ifdim\dimen@ii<9000\p@\relax \advance#1#2\dimen@ii
718
719
     \else
       \pcol@bg@calculate#1\z@{\@nameuse{pcol@bg@ext@inf@#3}}%
720
       \advance\dimen@ii-\@M\p@ \advance#1#2\dimen@ii
721
723 \def\pcol@bg@ext@inf@l{\pcol@bg@negative\pcol@bg@pageleft}
724 \def\pcol@bg@ext@inf@r{\pcol@bg@negative\pcol@bg@pageleft
     \pcol@bg@paperwidth}
725
726 \def\pcol@bg@ext@inf@t{\pcol@bg@negative\pcol@bg@pagetop}
727 \def\pcol@bg@ext@inf@b{\pcol@bg@negative\pcol@bg@pagetop
     \pcol@bg@paperheight}
729
```

\pcol@bg@paperwidth \pcol@bg@paperheight \pcol@bg@pageleft \pcol@bg@textheight \pcol@bg@columnleft \pcol@bg@columnright \pcol@bg@columnwidth \pcol@bg@columnsep The following macros specify the whole or a part of $F \in \{F_x, F_y, F_w, F_h\}$ being the body of \pcol@bg@@·a for background painting regions $R_a^{[c]}$.

```
\label{eq:pol_paper_width} \begin{split} & | pcol@bg@paperwidth = W_P - 2W_R = paperwidth - 2pagerim \quad (t,T,b,B,r,R) \\ & | pcol@bg@paperheight = H_P - 2H_R = paperheight - 2pagerim \quad (b,B) \\ & | pcol@bg@pageleft = W_M - W_R = (pcol@bg@leftmargin + 1in) - pagerim \quad (t,T,b,B,l,L,r,R) \\ & | pcol@bg@pagetop = H_M - W_R \\ & = (pcol@bg@pagetop + pcol@bg@pagetop + pcol@pagetop + pcol
```

Note that $\pagerim\ in\ F$ means $-\pagerim\ because its sign is reversed by <math>\pagerim\ in\ F$ means $-\pagerim\ because its sign is reversed by <math>\pagerim\ in\ F$ means $-\pagerim\ because its sign is reversed by <math>\pagerim\ in\ pool@bg@paint@in\ pool@bg@evainf@in\ pool@output@clear\ while it is temporarily redefined in <math>\pagerim\ pool@output@end$.

```
730 \def\pcol@bg@paperwidth{\@elt\paperwidth \@elt{2\pagerim}}
731 \def\pcol@bg@paperheight{\@elt\paperheight \@elt{2\pagerim}}
732 \def\pcol@bg@pageleft{\@elt{1in}\@elt\pcol@bg@leftmargin \@elt\pagerim}
733 \def\pcol@bg@pagetop{\@elt{1in}\@elt\topmargin \@elt\headheight \@elt\headsep
734 \@elt\pagerim}
735 \def\pcol@bg@textheight{\@elt\textheight \@elt\@maxdepth}
736 \def\pcol@bg@columnleft{%
```

```
737 \@tempcnta\pcol@bg@from \@whilenum\@tempcnta<\pcol@currcol\do{%
738 \@elt{\@nameuse{pcol@columnwidth\number\@tempcnta}}%
739 \@elt{\@nameuse{pcol@columnsep\number\@tempcnta}}%
740 \advance\@tempcnta\@ne}}
741 \def\pcol@bg@columnright{\pcol@bg@columnleft \pcol@bg@columnwidth}
742 \def\pcol@bg@columnwidth{\@elt{\@nameuse{pcol@columnwidth\number\pcol@currcol}}}
743 \def\pcol@bg@columnsep{\@elt{\@nameuse{pcol@columnsep\number\pcol@currcol}}}
```

\pcol@bg@preposttop
\pcol@bg@preposttop@left
\pcol@bg@preposttop@right
 \pcol@bg@columntop
 \pcol@bg@columnheight
 \pcol@bg@floatheight
 \pcol@bg@footnoteheight
 \pcol@bg@spanningtop
 \pcol@bg@spanningtop

Besides the macros shown above, $\pcol@bg@e.a$ uses the following macros defined by macros using $\pcol@bg@paintpage$, $\pcol@bg@paintcolumns$ or $\pcol@bg@paintbox$.

- \pcol@bg@preposttop being \pcol@bg@preposttop@left or \pcol@bg@preposttop@ right for $a \in \{p, P\}$ by \@outputpage and \pcol@output@end, the latter of which may define only the left one if the closing environment is not parallel-paged. That is, both of left and right macros are usually equivalent, but the right one can be smaller than the left if we have two or more (last pages of) paracol environments in a page and the closing environment is not parallel-paged while some others are. In such case, \@outputpage or \pcol@output@start, another macro referring to them, must paint the region below \pcol@bg@preposttop@right in the right page as a part of pre-environment stuff or post-environment stuff by \letting \pcol@bg@preposttop@ left and \pcol@bg@preposttop@right for the left and right parallel-pages respectively. Both macros have common initial value 0.
- \pcol@bg@columntop and \pcol@bg@columnheight for $a \in \{c,g\}$ by \pcol@build colseprule and \pcol@buildcselt.
- \bullet \pcol@bg@spanningtop and \pcol@bg@spanningheight for $a \in \{s,S\}$ by \pcol@buildcselt.
- \pcol@bg@floatheight for $a \in \{f,F\}$ by \pcol@outputelt, \pcol@ioutputelt, \pcol@output@clear and \pcol@makeflushedpage
- \pcol@bg@footnoteheight for $a \in \{n, N\}$ by \pcol@ioutputelt, \pcol@imakeflushed page and \pcol@output@end.

```
744 \def\pcol@bg@preposttop@left{Opt}
745 \let\pcol@bg@preposttop@right\pcol@bg@preposttop@left
746
```

```
The macros \pcol@bg@c·a define arguments F_x, F_y, F_w and F_h to be passed to \pcol@
\pcol@bg@@c
\pcol@bg@@C
                          bg@paintregion@i in their bodies to calculate (x_0, y_0) and (x_1-x_0, y_1-y_0) for regions R_a^{[c]}
\pcol@bg@@g
                          as shown below in the form of (x_0, y_0) + (x_1 - x_0, y_1 - y_0) (to have (x_1, y_1)), where H^c
\pcol@bg@@G
                          \pcol@bg@columntop, h^c = \pcol@bg@columnheight, H^s = \pcol@bg@spanningtop, h^s = \
\pcol@bg@@s
                          \verb|\pcol@bg@spanningheight|, $h^f = \pcol@bg@floatheight|, $h^n = \pcol@bg@footnoteheight|
\pcol@bg@@S
                          and H^p = \pcol@bg@preposttop calculated by macros which invoke background painting
\pcol@bg@@t
                          macros, while s^n = \ jobins.
\pcol@bg@@T
                                        R_c^c : (W_c, H^c) + (w_c, h^c)
\pcol@bg@@b
                                       R_C^c : (W_c , 0) + (w_c , H_T)
\pcol@bg@@B
\pcol@bg@@l
                                        R_q^c : ((W_c + w_c), H^c) + (g_c, h^c)
\pcol@bg@@L
                                       R_G^c : ((W_c + w_c), 0) + (g_c, H_T)
\pcol@bg@@r
                                 R_{\{s,S\}}: (0, H^s) + (W_T, h^s)
\pcol@bg@@R
                                 R_{\{t,T\}}: (-(W_M - W_R), -(H_M - H_R)) + ((W_P - 2W_R), H_M - H_R)
\pcol@bg@@f
\pcol@bg@@F
                                R_{\{b,B\}}: (-(W_M - W_R), H_T) + ((W_P - 2W_R), (H_P - 2H_R) - ((H_M - H_R) + H_T))
\pcol@bg@@n
                                 R_{\{l,L\}} : (-(W_M - W_R), 0) + ((W_M - W_R), H_T)
\pcol@bg@@N
                                R_{\{r,R\}}: (W_T, 0) + ((W_P - 2W_R) - ((W_M - W_R) + W_T), H_T)
\pcol@bg@@p
\pcol@bg@@P
                                R_{\{f,F\}}: (0,0) + (W_T, h^f)
                                R_{\{n,N\}}: (0, H_T - (h^n + s^n)) + (W_T, h^n + s^n)
                                R_{\{p,P\}}: (0, H^p) + (W_T, H_T - H^p)
                         747 \def\pcol@bg@@c{%
                                   {\pcol@bg@columnleft}%
                         749
                                   {\@elt\pcol@bg@columntop}%
                         750
                                   {\pcol@bg@columnwidth}%
                         751
                                   {\pcol@bg@columnheight}}
                         752 \def\pcol@bg@@C{%
                                   {\pcol@bg@columnleft}%
                         753
                         754
                                   {}%
                                   {\pcol@bg@columnwidth}%
                         755
                                   {\pcol@bg@textheight}}
                         756
                         757 \def\pcol@bg@@g{%
                                   {\pcol@bg@columnright}%
                         759
                                   {\@elt\pcol@bg@columntop}%
                                   {\pcol@bg@columnsep}%
                         760
                                   {\pcol@bg@columnheight}}
                         762 \def\pcol@bg@@G{%
                                   {\pcol@bg@columnright}%
                         763
                         764
                                   {\pcol@bg@columnsep}%
                         765
                                   {\pcol@bg@textheight}}
                         766
                         767 \def\pcol@bg@@s{%
                                   {\pcol@bg@spanningtop}%
                         769
                         770
                                   {\@elt\textwidth}%
                                   {\pcol@bg@spanningheight}}
                         771
                         772 \def\pcol@bg@@t{%
                                   {\pcol@bg@negative\pcol@bg@pageleft}%
                         773
                                   {\pcol@bg@negative\pcol@bg@pagetop}%
                         774
                                   {\pcol@bg@paperwidth}%
```

```
{\pcol@bg@pagetop}}
777 \def\pcol@bg@@b{%
    {\pcol@bg@negative\pcol@bg@pageleft}%
     {\pcol@bg@textheight}%
     {\pcol@bg@paperwidth}%
780
     {\pcol@bg@paperheight
781
       \pcol@bg@negative{\pcol@bg@pagetop \pcol@bg@textheight}}}
782
783 \def\pcol@bg@@1{%
    {\pcol@bg@negative\pcol@bg@pageleft}%
784
785
     {}%
    {\pcol@bg@pageleft}%
786
     {\pcol@bg@textheight}}
787
788 \def\pcol@bg@@r{%
     {\@elt\textwidth}%
789
790
     {}%
791
     {\pcol@bg@paperwidth
       \pcol@bg@negative{\pcol@bg@pageleft \@elt\textwidth}}%
792
     {\pcol@bg@textheight}}
794 \def\pcol@bg@@f{%
795
    {}%
     {}%
796
     {\@elt\textwidth}%
797
     {\pcol@bg@floatheight}}
798
799 \def\pcol@bg@@n{%
800
801
     {\pcol@bg@textheight
       \pcol@bg@negative{\pcol@bg@footnoteheight \@elt{\skip\footins}}}%
     {\@elt\textwidth}%
     {\pcol@bg@footnoteheight \@elt{\skip\footins}}}
805 \def\pcol@bg@@p{%}
806
    {}%
     {\@elt\pcol@bg@preposttop}%
807
808
     {\@elt\textwidth}%
     {\pcol@bg@textheight \pcol@bg@negative{\@elt\pcol@bg@preposttop}}}
810 \let\pcol@bg@@S\pcol@bg@@s
811 \let\pcol@bg@@T\pcol@bg@@t
812 \let\pcol@bg@@B\pcol@bg@@b
813 \let\pcol@bg@@L\pcol@bg@@l
814 \let\pcol@bg@@R\pcol@bg@@r
815 \let\pcol@bg@@F\pcol@bg@@f
816 \let\pcol@bg@@N\pcol@bg@@n
817 \let\pcol@bg@@P\pcol@bg@@p
818
```

Special Output Routines 11

11.1 Dispatcher

\pcol@op@start \pcol@op@switch \pcol@op@flush \pcol@op@clear

The macro $\polenoise{1pt} \operatorname{pcol@op@-}f$ where $f \in F = \{ ptart, ptart$ \outputpenalty code less than -10000 to invoke the corresponding macro \pcol@output@·f. The code macros are given to \pcol@invokeoutput as its argument by \pcol@zparacol (f = start), \pcol@switchcol (f = switch), \pcol@visitallcols (f = switch), \pcol@ $\protect\pro$

switch), and \endownarrownar

```
819 %% Special Output Routines: Dispatcher 820
821 \def\pcol@op@start{-10010}
822 \def\pcol@op@switch{-10011}
823 \def\pcol@op@flush{-10012}
824 \def\pcol@op@clear{-10013}
825 \def\pcol@op@end{-10014}
```

\pcol@specialoutput

The macro \pcol@specialoutput is invoked solely in \pcol@output to invoke our own or IATEX's special output routine. It examines if $P = \text{outputpenalty} \in \{\text{pcol@op@} \cdot f \mid f \in F\}$ and then, if so, before invoking \pcol@output@ \cdot f, we rebuild \@holdpg removing \lastbox and the last vertical skip as done in IATEX's \@specialoutput. We also let \outputpenalty = -10000^{163} so that \vsize is correctly set to \@colroom in the second half of \pcol@output after this macro finishes.

Otherwise, i.e., if $P \notin \{\text{pcol@op@} f \mid f \in F\}$, we simply invokes LATEX's \@specialoutput 164 .

```
827 \def\pcol@specialoutput{%
     \ifnum\outputpenalty=\pcol@op@start\relax
828
       \let\reserved@a\pcol@output@start
829
     \else\ifnum\outputpenalty=\pcol@op@switch\relax
830
       \let\reserved@a\pcol@output@switch
831
832
     \else\ifnum\outputpenalty=\pcol@op@flush\relax
833
       \let\reserved@a\pcol@output@flush
     \else\ifnum\outputpenalty=\pcol@op@clear\relax
834
       \let\reserved@a\pcol@output@clear
835
     \else\ifnum\outputpenalty=\pcol@op@end\relax
836
       \let\reserved@a\pcol@output@end
837
     \else \let\reserved@a\@specialoutput
838
     \fi\fi\fi\fi\fi
839
840
     \ifnum\outputpenalty=-\@Miv\relax
       \ifvoid\footins\else \pcol@Log\dummy{dummy}\footins \fi
842
     \ifx\reserved@a\@specialoutput\else
843
       \global\setbox\@holdpg\vbox{\unvbox\@holdpg \unvbox\@cclv
844
         \setbox\@tempboxa\lastbox \unskip}%
845
       \verb|\outputpenalty-\@M|
846
     \fi
847
     \reserved@a}
848
849
```

11.2 Building Starting Page

\pcol@output@start

 $^{^{163}}$ It can be any value larger than -10004.

 $^{^{164}}$ With footnote logging if \outputpenalty = -10004.

 $p_t = 0$ and $\Pi = \emptyset$ because we have nothing for $q < p_t = 0$. We also move \@deferlist to \@dbldeferlist and then let \@deferlist be empty because all column-wise dererred floats become page-wise. In this float importation, as discussed in item-(4) of §1.8, we force all floats in the list have depth 0 to ensure no one has 1sp to conform our own and old-fashioned pagewise float placement mechanism¹⁶⁵. We then and let $\Phi = \bot$ because we don't have any deferred footnotes.

Next we caculate $H = H_r - (H_m + H_f + H_b)$ where $H_r = \colroom$; H_m is the height-plus-depth of the main vertical list in $\colonomath{\mathbb{Choldpg}}$; H_f is the sum of \schlash footins, the height-plus-depth of $\colonomathbb{\mathbb{Choldpg}}$ is the sum of \schlash is not $\colonomalh{\mathbb{L}}$ or 0 otherwise; and $H_b = \colonomalh{\mathbb{Choldpg}}$ the pre-environment stuff has bottom floats or 0 otherwise. That is, H is the room for each of column-page in the starting page. Then we examine if $H < 1.5 \times \colonomalh{\mathbb{Choldpg}}$ to mean $\colonomalh{\mathbb{Choldpg}}$ to ship out pre-environment stuff to avoid the warning. Therefore, we invoke $\colonomalh{\mathbb{Choldpg}}$ to ship out pre-environment stuff to avoid the ship-out image in $\colonomalh{\mathbb{Choldpg}}$. Then the box is passed to $\colonomalh{\mathbb{Choldpg}}$ through $\colonomalh{\mathbb{Choldpg}}$ to be outside the paracol environment having just started.

After that we invoke \pcol@startpage to let it produce $\pi(p_t)$ for the starting page $p_t = 0$ letting \pcol@currpage be empty so that the macro will not refer to it. The page $\pi(0)$ is usually empty but can have non-empty $\pi^i(0)$ with imported deferred floats which are now page-wise. Moreover, we can have two or more pages if deferred page-wise floats produce float pages. However, we can be unaware of these effects of floats because the resulting Π^+ with them is correct of course.

Then let $\topskip = \poletopskip$ being the value at $\poletopskip paracol$, and $\poletopskip paracol$, and $\poletopskip paracol$, and $\poletopskip paracol$, and thus the first item of each column will be at its top.

```
850 %% Special Output Routines: Building First Page
851
852 \def\pcol@output@start{%
853
     \global\pcol@outputtrue
     \global\pcol@page\z@ \global\pcol@toppage\z@ \global\pcol@basepage\z@
854
855
     \global\let\pcol@pages\@empty
     \global\let\@dbldeferlist\@deferlist \global\let\@deferlist\@empty
856
     {\def\@elt##1{\global\dp##1\z@}\@dbldeferlist}%
857
     \setbox\z@\box\pcol@topfnotes
858
     \@tempdima\@colroom
859
     \advance\@tempdima-\ht\@holdpg \advance\@tempdima-\dp\@holdpg
860
     \ifvoid\footins\else
861
       \advance\@tempdima-\skip\footins
862
863
       \advance\@tempdima-\ht\footins \advance\@tempdima-\dp\footins
       \advance\@tempdima-\belowfootnoteskip
864
     \fi
865
     \ifx\@botlist\@empty\else \advance\@tempdima-\textfloatsep \fi
866
     \ifdim\@tempdima<1.5\baselineskip
867
       \setbox\@cclv\box\@holdpg \@makecol
868
       \pcol@outputfalse \@outputpage \pcol@outputtrue
869
       \global\let\pcol@currpage\@empty \pcol@startpage
870
       \global\topskip\pcol@topskip \global\pcol@firstpagefalse
871
```

¹⁶⁵Though having 1sp is almost imposiible.

¹⁶⁶ We can be unaware of our customization for synchronization in $\pcol@combinefloats$ because $\pcol@ctextfloatsep$ is made ∞ by $\pcol@cparacol$.

Otherwise, i.e., if $H \ge 1.5 \times \text{baselineskip}$, we invoke \pcol@makenormalcol to make the pre-environment stuff as the spanning stuff of the starting page. The macro is different from \@makecol as follows; the height of resulting \@outputbox is natural rather than \textheight; merged footnotes is excluded if any; and the skip of \textfloatsep is added below the bottom floats also if any,

Then we let h be the height-plus-depth of $\oldsymbol{\col}$ being the spanning stuff and shrink $\oldsymbol{\col}$ by h. Next if $h > H_B = \poll{\col}$ by $\oldsymbol{\col}$ prol $\oldsymbol{\col}$ being the bottom of the previous paracol environment (having right parallel-page) or 0 if the curret page does not have it, to mean we have ordinary single-columned stuff in pre-environment stuff, we paint its background by $\coldsymbol{\col}$ by $\coldsymbol{\col}$ temporarily letting $\coldsymbol{\col}$ be $\coldsymbol{\col}$ by $\coldsymbol{\coldsym$

We also let $\pi^h(0)$ be the shrunk \@colht, and $\pi^t(0)$ be \topskip if h=0 assuming that the page does not have any spanning stuff¹⁶⁷ to typeset column-pages from the top of the page, or otherwise be 0 together with \topskip to inhibit the ordinary \topskip insertion.

As for $\pi^m(0)$, we define it as follows, referring to $\mathcal{M} = \text{pcol@mparbottom@out} = \{M_L^l, M_L^r, M_R^l, M_R^r\}$, where M_X^x has exactly one element mpar(h,t) which may be the position of last marginal notes in the last paracol environment in the page we are working on, or $M_X^x = \{mpar(0,0)\}$ if such marginal note or the environment itself does not exist in the page. On the other hand, B = Qmparbottom may have non-zero for the bottom edge of the last marginal note in pre-environment stuff including the last paracol environment if any. Therefore, what we need to do is to let $M_L^x = \{mpar(0,B)\}$ to reflect the marginal node whose bottom is at B and which can be different from what M_L^x had, where x is the target margin in the pre-environment stuff determined by \if@mparswitch, the parity of page(0) and \if@reversemargin.

The replacement is done by \pcol@do@mpbout which invokes \pcol@do@mpbout@whole $\langle m_L^l \rangle \langle M_R^l \rangle \langle M_R^r \rangle$ where $m_L^x \in \{M_L^x, \text{pcol@do@mpbout@elem}\langle M_L^x \rangle\}$ whose choice is made according that $x \in \{l,r\}$ is the target margin (latter) or not (former). Therefore, prior to the invocation of \pcol@do@mpbout, we \deffine \pcol@do@mpbout@whole so that it \xdefines $\mathcal{M} = \text{pcol@mparbottom@out}$ with its four arguments, and \pcol@do@mpbout@elem to let it be expanded to \@elt{0}{B} = mpar(0,B). After that, we also invoke \pcol@bias@mpbout giving it -h to replace mpar(t,b) being the sole element of each $M_{\{L,R\}}^{\{l,r\}}$ in the resulting \mathcal{M} with mpar(t-h,b-h) to have what we give to $\pi^m(0)$. This replacement transforms the coordinates for text area to that for columns, and makes it possible for the first marginal note in each margin in the paracol environment we now start to exploit the space for pre-environment stuff even if it is tall extraordinarily.

Then we let $\pi(0)$ have $\pi^i(0)$ and $\pi^m(0)$ shown above, and $\pi^p(0) = \texttt{c@page}$, $\pi^f(0) = \bot$ and $\pi^s(0) = \emptyset$ by pcol@defcurrpage, and let lifpcol@firstpage = true because $\pi^b(0)$ has pre-environment stuff.

```
872 \else
873 \pcol@makenormalcol
874 \@tempdima\ht\@outputbox \advance\@tempdima\dp\@outputbox
875 \global\advance\@colht-\@tempdima
876 \def\reserved@a{%
877 \ifdim\pcol@bg@preposttop=\@tempdima\else
```

¹⁶⁷Checking the emptiness by \pcol@ifempty does not work well for the very first page of a document because it has a \write as the very first item.

```
878
           \edef\pcol@bg@textheight{\@elt{\number\@tempdima sp}}%
           \pcol@bg@paintbox{Pp}%
879
         \fi}
880
       \ifnum\pcol@ncolleft<\pcol@ncol
881
          \global\setbox\pcol@rightpage\vbox{%
882
           \ifpcol@paired\else \advance\c@page\@ne \fi
883
           \let\pcol@bg@preposttop\pcol@bg@preposttop@right
884
           \reserved@a \unvbox\pcol@rightpage}%
885
       \fi
886
       \pcol@Fb
887
       \Onext\Ocurrbox\Ofreelist{\global\setbox\Ocurrbox\vbox{%
888
         \let\pcol@bg@preposttop\pcol@bg@preposttop@left
889
         \reserved@a \unvbox\@outputbox}}\pcol@ovf
890
       \pcol@Fe{output@start(preenv)}%
891
       \global\dimen\@currbox\@colht
892
       \ifdim\@tempdima=\z@ \@tempskipa\topskip \else \@tempskipa\z@ \fi
893
       \global\skip\@currbox\@tempskipa \global\topskip\@tempskipa
894
       \def\pcol@do@mpbout@whole##1##2##3##4{%
         \ensuremath{\mbox{wdef\pcol@mparbottom@out}{\#1}{\#2}{\#3}{\#4}}}
896
       \def\pcol@do@mpbout@elem\@elt##1##2{\@elt{0}{\number\@mparbottom}}%
897
898
       \pcol@do@mpbout
       \pcol@bias@mpbout{-\@tempdima}%
899
       \pcol@defcurrpage{\number\c@page}\@currbox\voidb@x{}{\pcol@mparbottom@out}%
900
901
       \global\pcol@firstpagetrue
902
```

Then regardless of H, we do the followings for all columns $c \in [0, C)$ to build κ_c , after initializing \@colroom to be \@colht, and invoking \pcol@floatplacement to reinitialize the parameters of column-wise float placement.

First, if we have let \topskip = 0 with the pre-environment stuff, we let $\kappa_c(\beta^b)$ have an invisible \hrule whose height and depth are 0 as the very first vertical item of the column-page. When we visit the column c for the first time afterward, we will \unvbox the box to let T_FX 's page builder have topskip = 0 and the invisible rule. Then the first vertical item of the column-page is added but it is recognized as non-first by TFX's page builder and thus it inserts \baselineskip referring to \prevdepth as the depth of the last item. The important issue is that the \prevdepth to be referred is assured having its value at \begin{paracol}, which is usually the depth of the last item of spanning stuff, by the following mechanism: (1) \pcol@ invokeoutput invoked in \pcol@zparacol saves \prevdepth in \pcol@prevdepth before the \output request for \pcol@output@start; (2) \pcol@prevdepth is saved in $\kappa_c(\delta)$ by \pcol@ setcurrcolnf invoked from \pcol@output@start as discussed afterward; (3) when the column c is visited for the first time, the special output routine $\pcol@output@start$ itself (c=0) or \pcol@output@switch (c>0) restores \pcol@prevdepth from $\kappa_c(\delta)$ by \pcol@getcurrcol; (4) \pcol@invokeoutput which made the \output request for (3) lets \prevdepth have the value of \pcol@prevdepth after the request. Therefore, the baseline progress from the last line of the spanning stuff to the first line of each column-page should be very natural as we see in the third and fourth lines of §6 of Part I.

Then we invoke \pcol@setcurrcolnf to save the following values for $\kappa_c(e)$ ($e \neq \beta$); $\kappa_c(\tau) = \text{voidb@x}$ because c does not have column-wise footnotes so far; $\kappa_c(\delta) = \text{prevdepth}$ as discussed above; $\kappa_c(\lambda_t) = \kappa_c(\lambda_m) = \kappa_c(\lambda_b) = \emptyset$ because \pcol@makenormalcol and \@combinefloats invoked from it emptied them; $\kappa_c(\lambda_d) = \emptyset$ as discussed above; $\kappa_c(\nu_t) = \text{c@topnumber}$, $\kappa_c(\nu_b) = \text{c@botnumber}$ and $\kappa_c(\nu_t) = \text{c@totalnumber}$ as initialized by \@floatplacement invoked from \pcol@floatplacement; $\kappa_c(\rho_t) = \text{topfraction} \times \text{@colht}$

and $\kappa_c(\rho_b) = \text{bottomfraction} \times \text{@colht}$ as initialized by \@floatplacement; $\kappa_c(\sigma)$ is defined by \if@nobreak and \if@afterindent at the time of \begin{paracol}; and $\kappa_c(\varepsilon) = \text{verypar}$ at the time of \begin{paracol}. We also let $\kappa_c(\beta^p) = 0$ because p = 0 and $\kappa_c(\beta^r) = \text{@colroom}$ defined above. In addition, we let $S_c = \emptyset$ because we don't have any column-page having been completed.

We also examine if $\hat{\gamma}_0^c = \ \text{col@columncolor} \cdot c$ is defined and, if so, acquire an \insert from \@freelist to let $\gamma_0^c = \ \text{col@columncolor@box} \cdot c$ have the coloring \special for the color defined in $\hat{\gamma}_0^c$ by invoking \pcol@set@color being the origina \set@color with nullification of \aftergroup. Otherwise, we let $\gamma_0^c = \bot$.

```
\global\@colroom\@colht \pcol@floatplacement
903
     \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
904
905
       \pcol@Fb
       \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{%
906
         \ifdim\topskip=\z@ \hrule\@height\z@\@width\z@ \fi}}\pcol@ovf
907
       \pcol@Fe{output@start(col)}%
908
       \pcol@setcurrcolnf
909
       \global\count\@currbox\z@
910
       \global\dimen\@currbox\@colroom
911
912
       \expandafter\gdef\csname pcol@shipped\number\pcol@currcol\endcsname{}%
913
       \pcol@ifccdefined
         {\@next\@currbox\@freelist{\global\setbox\@currbox\vbox{%
914
           \def\current@color{\pcol@ccuse{}}\let\aftergroup\@gobble
915
           \pcol@set@color}}\pcol@ovf}%
916
917
         {\def\@currbox{\voidb@x}}%
918
       \pcol@ccxdef{\@currbox}%
919
      \advance\pcol@currcol\@ne}%
```

Finally, we let $c = \pcolecurrcol = 0$ for the first column, and regain the parameters in κ_0 by \pcolegetcurrcol . Then before putting $\kappa_0(\beta^b)$ to the main vertical list by \pcolegetcurrol returning $\kappa_0(\beta)$ to \pcolegetcurrol to \pcolegetcurrol because it has become useless so far, we save the color context just with γ_0^c into Γ_s by \pcolegetcurrol strough itself to the main vertical list if it is not \prought and thus has footnotes to be merged. This \pcoleget insertion is different from other footnote \pcoleget insertion because \pcoleget footins is not \pcoleget but is put as a whole and is followed by \pcoleget pervent the reconnection of a broken footnotes will not be broken by \pcoleget page builder to prevent the reconnection of a broken footnote with innapropriate glue discarding, which we will discuss in §18. We also add a penalty 10000 or \pcoleget page when its first item is taller than the room in the starting page.

```
\global\pcol@currcol\z@
920
921
     \pcol@getcurrcol
922
     \pcol@savecolorstack
923
     \@cons\@freelist\@currbox \unvbox\@currbox
924
925
     \pcol@Fe{output@start(col)}%
926
     \ifvoid\footins\else
       \pcol@Log\pcol@output@start{insert}\footins
927
       \insert\footins{\box\footins\penalty\interlinepenalty}%
928
929
     \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi}
930
931
```

\pcol@makenormalcol

The macro \pcol@makenormalcol is invoked solely from \pcol@output@start to let \@output box have the pre-environment stuff as spanning stuff of the starting page. The operations this macro performs are very similar to those of \@makecol, which in fact is used in this macro itself, but has the following differences.

- (1) If \ifpcol@mgfnote = true, we exclude footnotes in \footins from \@outputbox, because they are merged with page-wise footnotes given in columns, by saving it into \@tempboxa during the building process and restoring it from the box register.
- (2) If pre-environment stuff does not have bottom floats, we build \@outputbox by ourselves without relying on \@makecol because the skips put into the bottom (or near it) by the macro is harmful to making pre-environment stuff and parallel columns naturally connected. Therfore, we move \@holdpg to \@outputbox adding \footins to its tail if any by \pcol@combinefootins, and then combine top floats if any by \pcol@combinefloats \footins to \@freelist as \@makecol does.

 In addition, we clear \@midlist and returns its contents to \@freelist as \@makecol does.
- (3) If pre-environment stuff has bottom floats, on the other hand, we use \@makecol to build pre-environment stuff in \@outputbox moving \@holdpg into \box255 prior to the invocation 169. Also before invocation in addition, we temporarily let \ifpcol@lastpage = true to let \@combinefloats = \pcol@combinefloats used in \@makecol put a vertical skip of \textfloatsep below the bottom floats so that the floats are well seperated from the top of multi-column stuff in the starting page. We also nullify \@textbottom by making it \let-equal to \relax because it is unnessary to put an infinitely stretchable skip at the bottom 170, and let \vbadness = 10000 to avoid an inevitable underfull message because \@makecol lets \@outputbox as tall as \textheight.
- (4) In both cases but especially that with bottom floats, resulting \contents outputbox is decapsulated by \unvbox to make its height natural.

Note that the special function for synchronized column-page in \colern used directly or indirectly in this macro, on the other hand, is not active in the invocation because \colern pcol@zparacol initialized \colern pcol@textfloatsep = \colern to mean we have no synchronization points. Also note that bottom floats and non-merged footnotes are put in \colern und thus they will not appear at the bottom of the page but above the column-pages in the page \colern 171.

```
932 \def\pcol@makenormalcol{%
```

```
\ifpcol@mgfnote \setbox\@tempboxa\box\footins \fi
933
934
     \begingroup
935
     \ifx\@botlist\@empty
       \ifvoid\footins \setbox\@outputbox\box\@holdpg
936
       \else
                        \pcol@combinefootins\@holdpg\footins
937
       \fi
938
       \pcol@Fb
939
       \let\@elt\relax \xdef\@freelist{\@freelist\@midlist}%
940
941
       \pcol@Fe{makenormalcol}%
       \global\let\@midlist\@empty
942
```

¹⁶⁸Since we do not have bottom floats, the order of materials in the resulting \@outputbox being top floats, main text and footnotes should be consistent with other pages with any IATEX including pIATEX.

 $^{^{169}}$ Therefore the order of footnotes and bottom floats is consistent with other pages and columns, i.e., footnote-first in the native IATEX while float-first in pIATEX, for example.

 $^{^{170}\}mathrm{Even}$ if unharmful.

 $^{^{171}}$ We could put them at the bottom by keeping them somewhere and insert them in \pcol@outputcolumns, but it will cause another problem that the numbers of the figures and footnotes are smaller than those in column-pages which are above them.

```
943
       \pcol@combinefloats
944
     \else
       \pcol@lastpagetrue
945
       \setbox\@cclv\box\@holdpg \let\@textbottom\relax \vbadness\@M
946
947
948
     \global\setbox\@outputbox\vbox{\unvbox\@outputbox}%
949
950
951
     \ifpcol@mgfnote \setbox\footins\box\@tempboxa \fi}
952
```

11.3 Column-Switching

\pcol@output@switch

The macro \pcol@output@switch is invoked from \pcol@specialoutput to process the special \output request made in \pcol@switchcol, \pcol@visitallcols and \pcol@flushclear, for a column-switching from $c = \pcol@currcol$ to $d = \pcol@nextcol$ which can be c. The macro is also invoked from \pcol@makeflushedpage to synchronize and to flush all current column-pages but staying in c.

First, we examine if the column-switching is to close a spanning text, i.e., \ifpcol@sptext = true and c=0, and if so we do the following; let h_p be the height of \pcol@prespan having pre-spanning-text stuff if it is not \bot , or 0 if \bot to mean we have had a page break in the spanning text; add h_p to \@colroom which we temporarily shrank when the spanning text starts; add an elemnent span(H,h) to the tail of $\pi^s(p_t) = \pcol@sptextlist$ by \pcol@getcurrpage and \pcol@defcurrpage, where H is h_p plus the total height of top floats measured by \pcol@addflhd, and h is the height-plus-depth of \@holdpg having (a part of) spanning text, represented in the form of integers and thus expanded with \number; shift \@holdpg left by \pcol@shiftspanning if the column-0 is not the leftmost due to column-swapping; and then put prespanning-text stuff and (maybe shifted) \@holdpg into \@holdpg itself so as to let \@holdpg have everything in the column-page 0 as usual.

Note that it can be $\poolegrespan = \bot$ if spanning text had a page break (or multiple ones) in it as shown above. This empty pre-spanning-text stuff, however, does not always means that we have no top floats because the page break in the spanning text can produce a column-page with top floats which are deferred from the previous page(s), or though unlikely the spanning text itself has float environments. Therefore, the measurement of the total height of top floats are always necessary. Also note that we perform these operations at the first column-switching for column-scaning from c = 0 with $\pooledge prevent produce <math>prevent prevent prevent$

Then regardless of the operations above, we acquire an \insert from \Offreelist by \Onext for $\kappa_c(\beta)$ to store the current column-page in (maybe modified) \Oholdpg by \pcolOclearcstOunvbox to add uncoloring \specials to rewind the color stack Γ^c at the bottom and possibly coloring ones to establish that saved in Γ_s at the top as the color context for the column-page when it has the first item.

Then if \footins $\neq \perp$, we perform one of the followings.

- If page-wise footnote typesetting is in effect and $p = p_t$, we save \footins into $\pi^f(p)$ by the sequence of \pcol@getcurrpinfo to get $\pi(p)$, \pcol@savefootins to move it in $\pi^f(p)$, and \pcol@defcurrpage to update $\pi(p)$ with $\pi^f(p)$.
- If page-wise footnote typesetting is in effect but $p < p_t$, we simply discard the contents of \footins by making it \bot , because \footins should have $\pi^f(p)$ which has been already fixed.

• If column-wise footnote typesettinng is in effect, by $\cline{colored}$ we save $\cline{colored}$ into $\cline{colored}$ which should be \cline{lem} in other cases, so that it will be saved into $\kappa_c(\tau)$ by $\cline{colored}$ by $\cline{colored}$ afterward.

Then if c=0, we invoke \pcol@setpageno to reflect the jump of \c@page made in the building process of the column-page to $\pi(q)$ for all $q \in [p, p_t]$. After that, we save c's column-context into κ_c by \pcol@setcurrcol and let $\kappa_c(\beta^p) = p$ and $\kappa_c(\beta^r) = \text{Qcolroom}$.

```
953 %% Special Output Routines: Column-Switching
955 \def\pcol@output@switch{%
     \ifpcol@sptext\ifnum\pcol@currcol=\z@
       957
958
       \global\advance\@colroom\dimen@
959
       \pcol@addflhd\@toplist\pcol@textfloatsep
960
       \pcol@getcurrpinfo\@tempcnta\@tempdima\@tempskipa
       \@tempdimb\ht\@holdpg \advance\@tempdimb\dp\@holdpg
961
       \@cons\pcol@sptextlist{{\number\dimen@}{\number\@tempdimb}}%
962
963
       \pcol@defcurrpage{\number\@tempcnta}\pcol@spanning\pcol@footins
964
                        {\pcol@sptextlist}{\pcol@mparbottom}%
       \pcol@shiftspanning\@holdpg
965
966
       \setbox\@holdpg\vbox{\unvbox\pcol@prespan \unvbox\@holdpg}%
967
     \fi\fi
968
     \pcol@Fb
969
     \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{
970
       \pcol@clearcst@unvbox\@holdpg}}\pcol@ovf
971
     \pcol@Fe{output@switch}%
972
     \def\pcol@currfoot{\voidb@x}%
973
     \ifvoid\footins\else
974
       \ifpcol@scfnote
975
         \ifnum\pcol@page=\pcol@toppage
976
           \pcol@getcurrpinfo\@tempcnta\@tempdima\@tempskipa
977
           \pcol@Log\pcol@output@switch{save}\footins
978
           \pcol@Fb
979
           \pcol@savefootins\pcol@footins
           \verb|\pcol@Fe{output@switch(pagefn)}||%
980
           \pcol@defcurrpage{\number\@tempcnta}\pcol@spanning\pcol@footins
981
                            {\pcol@sptextlist}{\pcol@mparbottom}%
982
983
984
           \pcol@Log\pcol@output@switch{discard}\footins
985
           \setbox\@tempboxa\box\footins
986
       \else
987
         \pcol@Log\pcol@output@switch{save}\footins
988
         \pcol@Fb
989
         \pcol@savefootins\pcol@currfoot
990
         \pcol@Fe{output@switch(colfn)}%
991
       \fi
992
     \fi
993
     \ifnum\pcol@currcol=\z@ \pcol@setpageno \fi
994
     \pcol@setcurrcol
995
     \global\count\@currbox\pcol@page
     \global\dimen\@currbox\@colroom
```

Next, we examine if \ifpcol@sptext = true and c = 0 again, and if so we broadcast \if@nobreak and \if@afterindent, or in other words $\kappa_c(\sigma)$, and tokens in \everypar = $\kappa_c(\varepsilon)$,

to pretend all columns follow the spanning text. That is, for each column e, we restore its column-context from κ_e by \pcol@getcurrcol, let \if@nobreak and \if@afterindent have the values for $c \in \{0, C-1\}$ and \everypar = $\kappa_c(\varepsilon)$, and then save the context to κ_e by \pcol@setcurrcol so that $\kappa_e(\sigma) = \kappa_c(\sigma)$ and $\kappa_e(\varepsilon) = \kappa_c(\varepsilon)$. After that, we \globally turn \ifpcol@sptext = false to give it the default state.

Note that this broadcast is essential when the spanning text has sectioning commands to have consistent settings of the page break inhibition, the skip above the another sectioning command following them, and the indentation of the first paragraph, for all columns. On the other hand, broadcasting of \everypar is natural even when it does not have sectioning commands because all columns may be considered following the spanning text. Also note that, as mentioned in the explanation of the first examination at the beginning of this macro, we perform these operations at the first column-switching for column-scanning from c=0 with \ifpcol@sptext = true prior to the synchronization following the spanning text. This means, if \if@nobreak = true, \penalty = 10000 is inserted at the top and bottom end of the space for spanning text in the columns such that $c \neq 0$, the former by this column-scan and the latter by the column-switching to c made after the synchronization. Therefore, if our synchronization mechanism and TeX's page builder once agreed both end can be in a page, both end will not chosen as page break points¹⁷².

```
\let\reserved@a\@nobreakfalse \let\reserved@b\@afterindentfalse
      \ifpcol@sptext\ifnum\pcol@currcol=\z@
999
1000
        \if@nobreak \let\reserved@a\@nobreaktrue \fi
        \if@afterindent \let\reserved@b\@afterindenttrue \fi
1001
        \@temptokena\everypar
1002
        \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
1003
          \pcol@getcurrcol \reserved@a \reserved@b \everypar\@temptokena
1004
          \pcol@setcurrcol
1005
1006
         \advance\pcol@currcol\@ne}%
1007
        \global\pcol@sptextfalse
```

Finally we invoke $\colongraphical problem of the synchronization if <math>\colongraphical problem or \colongraphical problem or the current column-page <math>d$ if $\colongraphical problem or \colongraphical problem or$

```
1009 \@tempswafalse \ifpcol@sync \@tempswatrue \fi \ifpcol@clear \@tempswatrue \fi
1010 \iff@tempswa \pcol@sync \fi
1011 \@tempswatrue
1012 \ifpcol@clear \ifpcol@sync\else \@tempswafalse \fi\fi
1013 \iff@tempswa \pcol@restartcolumn \fi
1014 \global\pcol@syncfalse}
1015
```

\pcol@shiftspanning

The macro $\pol@shiftspanning\langle b\rangle$ is used in $\pol@makecol$ and $\pol@output@switch$ to let box register b have itself but shifted left by $W_T-w_0=\textwidth-\columnwidth$ so that the left edge of its contents spanning text is aligned to the left edge of the leftmost column being different from column-0 due to column-swapping, i.e., if $\textsize{ \poleskip if poleskip in the left edge}$

 $^{^{172}}$ As for c=0, its top end of spanning text is a feasible break point to make the penalty insertion asymmetric. Therefore, we need to reinvestigate if the condition of the broadcast is really appropriate, and, if inappropriate, have to go back to the old implementation in which \ifpcol@sync is included in the condition. Otherwise, if proved appropriate, we will have to consider to make the penalty insertion symmetric by adding \nobreak at the top of spanning text in c=0.

and \copage mod 2 = 0. Note that \copage is not obtained from $\pi^p(p)$ by the invokers but have the value when the \output request is made to let invokers work, and thus have the correct value even when a jump occurs prior to the request.

```
1016 \def\pcol@shiftspanning#1{%
1017 \ifpcol@swapcolumn\ifodd\c@page\else
1018 \setbox#1\vbox{\@tempdima\textwidth \advance\@tempdima-\columnwidth
1019 \moveleft\@tempdima\box#1}
1020 \fi\fi}
1021
```

\pcol@restartcolumn

The macro \pcol@restartcolumn is invoked from \pcol@output@switch or \pcol@freshpage to restart the current column-page $d = \pcol@nextcol$ which becomes $c = \pcol@currcol$ by the very first assignment in this macro. Then we restore the column-context in κ_c by \pcol@getcurrcol and let $p = \kappa_c(\beta^p)$ and \@colroom = $\kappa_c(\beta^r)$ before returning $\kappa_c(\beta)$ to \@freelist by \@cons because it has become useless so far. We also restore the page context of p by \pcol@getcurrpage.

```
1022 \def\pcol@restartcolumn{%
1023
      \global\pcol@currcol\pcol@nextcol
1024
      \pcol@getcurrcol
1025
      \global\pcol@page\count\@currbox
      \global\@colroom\dimen\@currbox
      \pcol@Fb
1027
      \cons\cons\cons
1028
1029
      \pcol@Fe{restartcolumn(col)}%
      \pcol@getcurrpage
1030
```

Then we perform footnote \insertion as follows.

- (1) If footnote typesetting is page-wise and $p = p_t$, we do the followings.
 - (a) Put the contents of $\kappa_c(\beta^b)$ by \pcol@putbackmvl to make the color context in .dvi consistent with the current .tex's one, and to save pre-spanning-text stuff into \pcol@prespan if we are opening a spanning text.
 - (b) Put \penalty = 10000 by \nobreak if \if@nobreak = true or \interlinepenalty by \addpenalty¹⁷³ otherwise, as the page break penalty at the returning point. Note that adding the \penalty will be nullified by TeX if $\kappa_c(\beta^b)$ has nothing and thus, if the column-page is still empty when we leave from it, its emptiness without any items is assured. Also note that the penalty insertion here looks essential to keep TeX's page builder from confusing with page-wise footnotes which it has not seen in a column-page¹⁷⁴.
 - (c) If $\pi^f(p) \neq \bot$, let \pcol@currfoot and then \footins have the footnotes in it by an \edef and \pcol@getcurrfoot, return the \insert for them to \@freelist, invoke \pcol@shrinkcolbyfn to shrink \@colht temporarily by their total height and to remember the exsistence of them with \@tempdimb = -\skip\footins, and then \insert the footnotes so that it contributes to the building process of the column-page to be restarted. Otherwise, i.e. if $\pi^f(p) = \bot$, \@colht is unchanged and \@tempdimb = 0.
 - (d) Invoke $\protect\operatorname{pcol@deferredfootins}$ to $\protect\operatorname{linsert}$ deferred footnotes in Φ until their total height reaches (possibly shrunk) $\protect\operatorname{linsert}$ deferred footnotes in Φ until their total height reaches (possibly shrunk) $\protect\operatorname{linsert}$ deferred footnotes in Φ until their total

¹⁷³As done in \@specialoutput but \penalty\interlinepenalty should be sufficient.

 $^{^{174}\}mathrm{At}$ least a test with tall page-wise footnotes gave us a confusing result.

builder from holding too large number of footnotes unprocessed causing confused ordering on presenting them to **\output** routine.

- (2) If footnote typesetting is page-wise but $p < p_t$, we do the followings.
 - (a) If $\pi^f(p) \neq \bot$, get it into \footins as done in (1c) but giving \copy to \pcol@ getcurrfoot because $\pi^f(p)$ has been fixed and thus will be kept until it is shipped out, and then \insert it.
 - (b) Put $\kappa_c(\beta^b)$ and the penalty as done in (1a) and (1b).

Thes order of footnotes, main vertical list and then penalty is essential to ensure that the column-page in $p < p_t$ has room for footnotes whose residence in p has already been fixed.

- (3) If footnote typesetting is column-wise, we do the followings.
 - (a) Put $\kappa_c(\beta^b)$ as done in (1a).
 - (b) If $\kappa_c(ft) \neq \bot$, get it by \pcol@getcurrfoot returning the \insert to \@freelist, and then \insert it.
 - (c) Put a penalty as done in (1b).

The order of main vertical list, footnotes and then penalty is appropriate for column-wise footnotes because they definitely have space in the column-page and TeX will break the page below the insertion, possibly just below thanks to the penalty, to keep the footnotes and references to them in a page.

```
\ifpcol@scfnote
1031
        \edef\pcol@currfoot{\pcol@footins}%
1032
1033
        \ifnum\pcol@page=\pcol@toppage
          \@tempdima\@colht \@tempdimb\z@
1034
          \pcol@putbackmvl
1035
          \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi
1036
          \ifvoid\pcol@footins\else
1037
            \pcol@Fb
1038
            \pcol@getcurrfoot\box \@cons\@freelist\pcol@currfoot
1039
            \pcol@Fe{restartcolumn(pagefn)}%
1040
            \pcol@Log\pcol@restartcolumn{insert}\footins
1041
            \pcol@shrinkcolbyfn\@colht\footins\@tempdimb
1042
1043
            \insert\footins{\unvbox\footins}%
1044
          \pcol@deferredfootins\pcol@restartcolumn
1045
          1046
        \else
1047
          \ifvoid\pcol@footins\else
1048
            \pcol@getcurrfoot\copy
1049
1050
            \pcol@Log\pcol@restartcolumn{insdmy}\footins
            \insert\footins{\unvbox\footins}%
1051
1052
          \pcol@putbackmvl
1053
          \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi
1054
        \fi
1055
1056
      \else
        \pcol@putbackmvl
1057
```

```
\ifvoid\pcol@currfoot\else
1058
          \pcol@Fb
1059
          \pcol@getcurrfoot\box \@cons\@freelist\pcol@currfoot
1060
          \pcol@Fe{restartcolumn(colfn)}%
1061
          \pcol@Log\pcol@restartcolumn{insert}\footins
1062
          \insert\footins{\unvbox\footins}%
1063
1064
        \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi
1065
1066
      fi
1067
```

\pcol@getcurrcol \pcol@igetcurrcol \pcol@iigetcurrcol The macro \pcol@getcurrcol is invoked from the following macros to restore the typesetting parameters of the column $c = \pcol@currcol$ from κ_c , and to let \columnwidth have $w_c = \pcol@columnwidth \cdot c^{175}$.

```
\pcol@output@start \pcol@output@switch \pcol@restartcolumn \pcol@flushcolumn \pcol@measurecolumn \pcol@synccolumn \pcol@makeflushedpage \pcol@iflushfloats \pcol@freshpage \pcol@output@end
```

Since we represent κ_c as;

$$\{\kappa_c(\beta)\}\{\kappa_c(\tau)\}\{\kappa_c(\delta)\}\{\kappa_c(\lambda_t)\}\{\kappa_c(\lambda_m)\}\{\kappa_c(\lambda_b)\}\{\kappa_c(\lambda_d)\}\{\kappa_c(\xi)\}\}$$

$$\{\{\kappa_c(\eta)\}\{\kappa_c(\nu_t)\}\{\kappa_c(\rho_t)\}\{\kappa_c(\nu_b)\}\{\kappa_c(\rho_b)\}\{\kappa_c(\nu_c)\}\{\kappa_c(\sigma)\}\{\kappa_c(\varepsilon)\}\}$$

in the body of \c we restore first eight by \c giving everything above as its arguments by the expansion of

\csname pcol@col\number\pcol@currcol\endcsname

and then of the resulting control sequence. Then this macro gives its nineth argument to \pcol@ijgetcurrcol which restores the last eight. We also do

$\verb|\global| column width \verb|\pcol@column width| \cdot c$

by a pair of \expandafter for the first two control sequences.

Note that the restore operations are $\S lobal$, except for $\kappa_c(\beta)$ and $\kappa_d(\tau)$ because they are referred to only in $\S lobal$ including $\S lobal$ for which $\S lobal$ are defined $\S lobal$ by Lagrange and $\S lobal$ are defined $\S lobal$ by Lagrange and thus restoring them needs to specify the unit sp.

```
1068 \def\pcol@getcurrcol{%
      \expandafter\expandafter\expandafter\pcol@igetcurrcol
1070
        \csname pcol@col\number\pcol@currcol\endcsname
1071
      \expandafter\global\expandafter\columnwidth
1072
        \csname pcol@columnwidth\number\pcol@currcol\endcsname}
1073 \def\pcol@igetcurrcol#1#2#3#4#5#6#7#8#9{%
      \def\@currbox{#1}\def\pcol@currfoot{#2}\global\pcol@prevdepth#3sp\relax
1074
      \gdef\@toplist{#4}\gdef\@midlist{#5}\gdef\@botlist{#6}\gdef\@deferlist{#7}%
1075
      \global\pcol@textfloatsep#8sp\pcol@iigetcurrcol#9}
1076
1077 \def\pcol@iigetcurrcol#1#2#3#4#5#6#7#8{%
1078
      \global\@textfloatsheight#1sp\relax
      \global\@topnum#2\relax \global\@toproom#3sp\relax
```

¹⁷⁵\hsize and \linewidth are let have w_c and $w_c - \mu$ respectively in \pcol@invokeoutput.

```
\label{lobal_Qbotnum#4} $$ \global\\@botnom#5sp\relax $$
1080
      \global\@colnum#6\relax
1081
      \global\@afterindentfalse \@nobreaktrue
1082
      \ifcase#7
1083
        \@nobreakfalse \or
1084
        \global\@afterindenttrue \else
1085
1086
        \relax
      \fi
1087
      \global\everypar{#8}}
1088
```

\pcol@getcurrfoot

The macro \pcol@getcurrfoot\\(com \) is invoked from \pcol@startcolumn (\copy, $\pi^f(p)$), \pcol@restartcolumn (\copy/\box, $\pi^f(p)/\kappa_c(\tau)$), \pcol@flushcolumn (\box, $\kappa_c(\tau)$) and \pcol@imakeflushedpage (\box, $\kappa_c(\tau)$) to put everything in \pcol@currfoot, having the second element in the parens following macro names, into \footins using \langle com \rangle shown as the first element in parens for the \box component. That is, if the source $\pi^f(p)$ or $\kappa_c(\tau^b)$ is void, we let \box\footins be so. Otherwise, we move \box, \count, \dimen and \skip of the source into those of \footins^{176}.

```
1089 \def\pcol@getcurrfoot#1{%
1090 \ifvoid\pcol@currfoot \global\setbox\footins\box\voidb@x
1091 \else
1092 \global\setbox\footins#1\pcol@currfoot
1093 \global\count\footins\count\pcol@currfoot
1094 \global\dimen\footins\dimen\pcol@currfoot
1095 \global\skip\footins\skip\pcol@currfoot
1096 \fi}
```

\pcol@setcurrcol
\pcol@setcurrcolnf

The macro \pcol@setcurrcol is invoked from \pcol@output@switch, \pcol@measurecolumn and \pcol@synccolumn to save column-context of $c = \pcol@currcol$ in κ_c . It is also used in \pcol@setcurrcolnf invoked from \pcol@output@start, \pcol@flushcolumn, \pcol@imakeflushedpage, \pcol@iflushfloats and \pcol@freshpage for the saving when the column-page is known to have no footnotes.

The macro \pcol@setcurrcol at first calculates the combined code for \if@nobreak and \if@afterindent, and then saves parameters into κ_c by \xdef to have the sequence shown in the description of \pcol@getcurrcol. Note that \dimen-type parameters are saved by expansions with \number and thus as decimal integers.

The macro \pcol@setcurrcolnf \defines $\kappa_c(\tau) = \pcol@currfoot$ as \voidb@x, and then invoke \pcol@setcurrcol for saving.

```
1097 \def\pcol@setcurrcol{{\let\@elt\relax
     \@tempcnta\if@nobreak\if@afterindent\@ne\else\tw@\fi\else\z@\fi
     \expandafter\xdef\csname pcol@col\number\pcol@currcol\endcsname{%
1099
       {\@currbox}{\pcol@currfoot}{\number\pcol@prevdepth}%
1100
        {\@toplist}{\@midlist}{\@botlist}{\@deferlist}{\number\pcol@textfloatsep}%
1101
1102
        {{\number\@textfloatsheight}%
        {\number\@topnum}{\number\@botnum}{\number\@botroom}%
1103
        {\number\@colnum}{\number\@tempcnta}{\the\everypar}}}}
1104
1105 \def\pcol@setcurrcolnf{\def\pcol@currfoot{\voidb@x}\pcol@setcurrcol}
1106
```

¹⁷⁶Moving \count, \dimen and \skip is redundant almost always because it is very unlikely that these footnote parameters are modified dynamically. Moreover, dynamic modification of them is hardly consistent with repetitive self-\insertion of \footins in \pcol@restartcolumn and \@reinserts of LaTeX. However, we dare to move them in order to, for example, allow each column has its own footnote parameters.

\pcol@putbackmvl

The macro \pcol@putbackmvl, solely used in \pcol@restartcolumn, has two functions; color stack restoration and pre-spanning-text stuff preservation. It examines the emptiness of the column-page of the column c to be restarted in $\kappa_c(\beta) = \text{Qcurrbox}$. If so, the color stack Γ^c is saved into $\Gamma_s = \text{pcol@colorstack@saved}$ by \pcol@savecolorstack as the opening color context of the column-page, and \pcol@prespan for pre-spanning-text stuff is made \bot .

Otherwise, Γ_s is let \bot because the opening color context has already been put when we left from the column-page. Then if $\ifthightharpoonup \ifthightharpoonup \ifthightharpoonup$

Note that $\footnote{\footnote{\colorestart}}$ is temporarily made false by this macro if the \colorestartcolumn did not make synchronized column-switching, i.e., if $\footnote{\footnote{\colorestart}}$ to mean the page is flushed before the synchronization, or $\footnote{\footnote{\colorestart}}$ for column-scanning prior to the synchronization.

```
1107 \def\pcol@putbackmvl{%
      \ifpcol@flush \pcol@sptextstartfalse \fi
1108
1109
      \ifpcol@sync\else \pcol@sptextstartfalse \fi
1110
      \pcol@ifempty\@currbox
1111
       {\pcol@savecolorstack
        \ifpcol@sptextstart \global\setbox\pcol@prespan\box\voidb@x \fi}%
1112
       {\global\setbox\pcol@colorstack@saved\box\voidb@x
1113
1114
        \ifpcol@sptextstart
          \global\setbox\pcol@prespan\vbox{%
1115
            \unvbox\@currbox \pcol@restorecolorstack}%
1116
1117
          \global\advance\@colroom-\ht\pcol@prespan
          \global\topskip\z@ \hrule\@height\z@\@width\z@
1118
1119
          \unvbox\@currbox \pcol@restorecolorstack
1120
        fi}
1121
1122
```

11.4 Color Management

\pcol@magicpenalty \pcol@ifempty

The macro \pcol@ifempty\langle box\langle (then)\langle else\rangle is used in \pcol@putbackmvl, \pcol@clearcst@ unvbox and \pcol@measurecolumn to examine if \langle box\rangle is empty, and to perform \langle then\rangle if so or \langle else\rangle otherwise. Since TeX does not provide any convenient way for the examination unfortunately, we perform a series of tricky operations to put the followings into \@tempboxa; a penalty of \pcol@magicpenalty = 12345 whose existence in the \langle box\rangle is (almost) impossible; contents of \langle box\rangle put by \unvcopy; and then a \global \definition of \@gtempa to let it have the decimal representation of \lastpenalty. Since \lastpenalty has \langle pen\rangle if the last item is \penalty \langle pen\rangle, or 0 otherwise, \@gtempa = \pcol@magicpenalty iff \langle box\rangle is empty.

¹⁷⁷ If \pcol@prespan is connected to (the first part of) the spanning text, the reestablishment of the color stack here correctly places coloring \specials in .dvi. On the other hand, if the spanning text is slown away to the next page as a whole, the reestablishment here is essential for the correct paring of the pushes and pops, the latter of which are at the bottom of the column-page whose tail is \pcol@prespan.

```
1123 %% Special Output Routines: Color Management
1124
1125 \def\pcol@magicpenalty{12345}
1126 \def\pcol@ifempty#1#2#3{%
1127 \setbox\@tempboxa\vbox{\penalty\pcol@magicpenalty}
1128 \unvcopy#1\xdef\@gtempa{\number\lastpenalty}}%
1129 \ifnum\@gtempa=\pcol@magicpenalty\relax \def\reserved@a{#2}%
1130 \else \def\reserved@a{#3}%
1131 \fi
1132 \reserved@a}
```

\pcol@clearcst@unvbox \pcol@clearcolorstack

The macro \pcol@clearcst@unvbox $\langle box \rangle$, invoked from \pcol@opcol and \pcol@output@ switch, puts the following above and below $\langle box \rangle$ containing the main vertical list of a column-page from which we are now leaving, if \pcol@ifempty judges that $\langle box \rangle$ is not empty. Above the $\langle box \rangle$, we put coloring \specials to establish the color stack of .dvi saved in $\Gamma_s = \text{\col}$ colorstack@saved by \pcol@restorecst as the opening color context of the column-page. The stack Γ_s , however, can be \bot if $\langle box \rangle$ already has the \specials, i.e., when we visit the column-page it had already had some items. Below $\langle box \rangle$, on the other hand, we put uncoloring \specials by \pcol@clearcolorstack to rewind Γ_r^c to clear the color context of the column-page in .dvi temporarily so that afterward it is made consistent with that in .tex.

The macro \pcol@clearcolorstack, solely invoked from \pcol@clearcst@unvbox shown above \$^{178}\$, scans \$\Gamma_r^c = (\gamma_0^c, \Gamma_r)\$ by \pcol@scancst giving \$\Gamma_r = \pcol@colorins\$ to it as its argument. Since we gives \$\Gamma_r\$ to the macro, this scan includes removals of all \$\gamma_i^-\$ and \$\gamma_{i,m}^-\$, all \$\gamma_i\$ having matching \$\gamma_i^-\$, all \$\gamma_{i,m}\$ having matching \$\gamma_{i,m}^-\$, and all elements to update \$\gamma_0^c\$, from \$\Gamma_r\$ to let \pcol@colorins have \$\Gamma\$. Prior to this invocation, we \define \reserved@a(\gamma_i) and \reserved@b(\gamma_0^c)\$ to let them have \reset@color so that uncoloring \special will be put into the main vertical list for each \$\gamma_i \in \Gamma\$ and \$\gamma_0^c\$ before update if any, regardless of coloring \special they have. That is, we invoke \reset@color as many times as the appearance of \$\gamma_i \in \Gamma\$ and once if \$\gamma_0^c \neq \pm\$ before the invocation, ignoring the color information in each element and the order of elements, expecting \reset@color just pops printer's color stack to rewind it as we intend.

Note that in some printer .definition could \define \reset@color to let printer's text color be \current@color to make the stack rewinding resulting in the sequence of coloring operations with \current@color at the invocation of \output. This meaningless operations might cause a problem when a colored column-page of c_1 is physically followed by another column-page of the succeeding column c_2 without any coloring, because the column-page of c_2 will be colored with \current@color at the page break in c_1 . If this problem is serious, we could initialize γ_0^c with \current@color at \begin{paracol} for all c such that $\hat{\gamma}_0^c$ is undefined, in order to make sure that any column-page has at least one coloring \special with γ_0^c at its beginning so that, for example, coloring operations at the tail of the column-page of c_1 is overridden by that of the default color of c_2 placed at the head of its column-page.

```
1134 \def\pcol@clearcst@unvbox#1{%

1135 \pcol@ifempty#1\relax

1136 \{\pcol@restorecst\pcol@colorstack@saved \unvbox#1\pcol@clearcolorstack}\}

1137 \def\pcol@clearcolorstack{%

1138 \def\reserved@a##1{\reset@color}\def\reserved@b##1{\reset@color}\%

1139 \pcol@scancst\pcol@colorins}
```

¹⁷⁸But we have this macro to avoid the complication in \defining \reserved@a and \reserved@b with an argument if we did it in the argument of \pcol@ifempty in \pcol@clearcst@unvbox.

\pcol@restorecolorstack \pcol@restorecst

The macro \pcol@restorecolorstack, used in \pcol@putbackmvl and \pcol@output@end, makes color context in .dvi consistent with that in .tex by giving $\Gamma = \pcol@colorins$ to \pcol@restorecst to let it scan $\Gamma^c = (\gamma_0^c, \Gamma)$. The callee macro \pcol@restorecst $\langle box \rangle$, also used in \pcol@clearcst@unvbox with $\langle box \rangle = \Gamma_s = \pcol@colorstack@saved$, invokes \pcol@scancst after \defining \reserved@a $\langle \gamma_i \rangle$ to apply \unvbox to γ_i in Γ or Γ_s and \reserved@b $\langle \gamma_0^c \rangle$ to apply \unvcopy to γ_0^c so that coloring \specials they have will be put into the main vertical list.

```
1141 \def\pcol@restorecolorstack{\pcol@restorecst\pcol@colorins}
1142 \def\pcol@restorecst{%
1143 \def\reserved@a##1{\unvbox##1}\def\reserved@b##1{\unvcopy##1}%
1144 \pcol@scancst}
1145
```

\pcol@scancst \pcol@iscancst The macro $\protect\operatorname{pcol@scancst}\langle box \rangle$ is invoked from $\protect\operatorname{pcol@scancst}\langle box \rangle$ restorecst. In the former invocation, we have $\langle box \rangle = \Gamma_r = \pcol@colorins$ to rewind $\Gamma_r = (\gamma_0^c, \Gamma_r)$ with \reserved@a $\langle \gamma_i \rangle$ and \reserved@b $\langle \gamma_0^c \rangle$ having \reset@color. In the latter one, we have $\langle box \rangle \in \{\Gamma = \pcol@colorins, \Gamma_s = \pcol@colorstack@saved\}\$ to reestablish $\Gamma^c = (\gamma_0^c, \Gamma) \text{ or } \Gamma_s \text{ with } \text{reserved@a} \langle \gamma_i \rangle \text{ to apply } \text{unvbox to } \gamma_i \text{ and } \text{reserved@b} \langle \gamma_0^c \rangle \text{ to apply}$ \unvcopy to γ_0^c . Therefore, if $\langle box \rangle = \text{\closelection}$ special for γ_0^c , unless it is \perp , to the main vertical list applying \reserved@b to it. This means the \special for γ_0^c is put first prior to those for elements in Γ_r or Γ consistently in reestablishing but not in rewinding. However as we discussed in the description of \pcol@clearcolorstack, the order of rewinding does not affect the result for almost all printers because only the number of pop operations is significant for them¹⁷⁹. Then if $\langle box \rangle \neq \bot$ we invoke \pcol@iscancst to examine the contents of $\langle box \rangle$ from its bottom to top. Prior to the invocation, we do the following; let Ω temphoxa have an empty ∇ as its initial value of reformed $\langle box \rangle$; let ∇ tempboxa have an empty \vbox as its initial value of the sequence of \specials to be put into the main vertical list; let $n_{pop} = \emptyset$ tempentb = 0; let $M = \mathbb{C}$ reserved \emptyset b = () as its initial value of the list of identifiers of math-mode pops; $\forall e = true$ to mean the first $\forall e = true$ to update γ_0^c found in the scan (i.e., the bottommost one) is effective.

In the macro \pcol@iscancst, we repeatedly examine the last \vbox in $\langle box \rangle$ taken by \lastbox into $\gamma = \pcol@tempboxb$ until γ becomes \bot , and perform one of the following for γ .

- (1) If $height(\gamma) = 0$ and $width(\gamma) = 0$ to mean $\gamma = \gamma_i^-$, increment n_{pop} .
- (2) If $height(\gamma) = 0$ and $width(\gamma) = m > 0$ to mean $\gamma = \gamma_{i,m}^-$, let M = (m, M).
- (3) If $height(\gamma) \neq 0$, $depth(\gamma) = 0$ and $width(\gamma) = 0$ to mean $\gamma = \gamma_i$, decrement n_{pop} if $n_{pop} > 0$, or otherwise add γ to the head of \Otherwise and apply \reserved@a $\langle \gamma \rangle$ to add its result to the head of \pcol@tempboxa.
- (4) If $height(\gamma) \neq 0$, $depth(\gamma) = 0$ and $width(\gamma) = m > 0$ to mean $\gamma = \gamma_{i,m}$, do nothing if $m \in M$, or otherwise add γ to the head of \Quad \Quad tempboxa and apply \reservedQa\(\gamma\gamma) to add its result to the head of \pcolQtempboxa.

 $^{^{179}}$ And even for the minority because multiple updates of printer's color with one particular color are independent of the order of them.

(5) If $height(\gamma) \neq 0$, $depth(\gamma) \neq 0$ to mean γ has a \special with which γ_0^c is updated. If \iff \text{tempswa} = true to mean γ is the first (bottommost) occurence, γ_0^c is updated acquiring an \insert from \Offreelist if it was \bot . In this case of \bot , we have to put an uncoloring \special by \reset Occurrence, because \pcol occurrence \text{did not do it but \columncolor or \normalcolumncolor pushed the corresponding color \special. Then we let \iff Otempswa = false.

Otherwise, i.e., if $\ightharpoonup if 0 tempswa = false$ for second or succeeding occurences, we do nothing because updates by them are overridden by the first one.

Note that the cases other than (3) and (4) happen only in rewinding, and thus in reestablishing we only have (3) and (4) with $n_{\text{pop}} = 0$ and M = () always so that every γ is kept into new $\langle box \rangle$ and a coloring \special for it will be put into the main vertical list.

Then we go back to \c contents of \c to let \c box, meaningless in reestablishing but not harmful, and put the contents of \c to the main vertical list.

```
1146 \def\pcol@scancst#1{%
1147
      \@tempcnta#1\relax
      \ifnum\@tempcnta=\pcol@colorins
1148
        \ifvoid\pcol@ccuse{@box}\else
1149
          \reserved@b{\pcol@ccuse{@box}}\fi
1150
      \fi
1151
      \ifvoid\@tempcnta\else
1152
        \setbox\@tempboxa\vbox{}\setbox\pcol@tempboxa\vbox{}\@tempcntb\z@
1153
1154
        \def\reserved@b{}\let\@elt\relax \@tempswatrue \pcol@iscancst
        \global\setbox\@tempcnta\box\@tempboxa \unvbox\pcol@tempboxa
1155
      \fi}
1156
1157 \def\pcol@iscancst{%
      \setbox\@tempcnta\vbox{%
1159
        \unvbox\@tempcnta \global\setbox\pcol@tempboxb\lastbox}%
1160
      \ifvoid\pcol@tempboxb \let\reserved@c\relax
1161
        \let\reserved@c\pcol@iscancst
1162
        \ifdim\ht\pcol@tempboxb=\z@
1163
1164
          \ifdim\wd\pcol@tempboxb=\z@ \advance\@tempcntb\@ne
1165
          \else \edef\reserved@b{\@elt{\number\wd\pcol@tempboxb}\reserved@b}%
1166
        \else\ifdim\dp\pcol@tempboxb=\z@
1167
          \ifdim\wd\pcol@tempboxb=\z@
1168
            \ifnum\@tempcntb>\z@ \advance\@tempcntb\m@ne
1169
            \else
1170
              \setbox\@tempboxa\vbox{\copy\pcol@tempboxb \unvbox\@tempboxa}%
1171
1172
              \setbox\pcol@tempboxa\vbox{%
                 \reserved@a\pcol@tempboxb \unvbox\pcol@tempboxa}%
1173
            \fi
1174
          \else
1175
            \count@\wd\pcol@tempboxb \chardef\reserved@d\z@
1176
            \def\@elt##1{\ifnum##1=\count@ \chardef\reserved@d\@ne \fi}%
1177
            \reserved@b \let\@elt\relax
1178
            \ifnum\reserved@d=\z@
1179
              \setbox\@tempboxa\vbox{\copy\pcol@tempboxb \unvbox\@tempboxa}%
1180
              \setbox\pcol@tempboxa\vbox{%
1181
                 \reserved@a\pcol@tempboxb \unvbox\pcol@tempboxa}%
1182
            \fi
1183
1184
          \fi
```

```
1185
        \else\if@tempswa
          \ifvoid\pcol@ccuse{@box}%
1186
            \Onext\Ocurrbox\Ofreelist{\global\setbox\Ocurrbox\vbox{}}\pcolOovf
1187
            \pcol@ccxdef{\@currbox}\reset@color
1188
1189
          \global\setbox\pcol@ccuse{@box}\vbox{\unvbox\pcol@tempboxb}%
1190
1191
          \@tempswafalse
        \fi\fi\fi
1192
      \fi
1193
1194
      \reserved@c}
1195
```

\pcol@savecolorstack

The macro \pcol@savecolorstack is used in \pcol@startcolumn, \pcol@output@start and \pcol@putbackmvl to save the opening color context in Γ^c of a current column-page c known to be or found empty into $\Gamma_s = \text{pcol@colorstack@saved}$. If both of $\gamma_0^c = \text{pcol@columncolor@box} \cdot c$ and $\Gamma = \text{pcol@colorins}$ are \bot , Γ_s is let be \bot . Otherwise, Γ_s is let be a \vbox having a \vbox for γ_0^c at the top if it is not \bot and then the contents of Γ if it is not \bot .

```
1196 \def\pcol@savecolorstack{%
      \ifvoid\pcol@colorins \@tempswafalse \else \@tempswatrue \fi
1198
      \ifvoid\pcol@ccuse{@box}%
1199
        \setbox\@tempboxa\box\voidb@x
1200
      \else
        \setbox\@tempboxa\vbox{\unvcopy\pcol@ccuse{@box}}%
1201
        \ht\@tempboxa1sp \dp\@tempboxa\z@ \wd\@tempboxa\z@
1202
        \@tempswatrue
1203
      \fi
1204
      \if@tempswa
1205
        \global\setbox\pcol@colorstack@saved\vbox{%
1206
          \ifvoid\@tempboxa\else \box\@tempboxa \fi
1207
          \ifvoid\pcol@colorins\else \unvcopy\pcol@colorins \fi}
1208
      \else \global\setbox\pcol@colorstack@saved\box\voidb@x
      fi
1210
1211
```

\pcol@ccuse \pcol@ifccdefined \pcol@ccxdef The macro \pcol@ccuse $\langle pfx \rangle$ is to expand a macro \pcol@columncolor $\cdot \langle pfx \rangle \cdot c$ for the current column c. It is used in \pcol@cutput@start and \pcol@scancst@shadow with $\langle pfx \rangle =$ '' to have $\hat{\gamma}_0^c$, and in \pcol@scancst, \pcol@iscancst, \pcol@savecolorstack, \pcol@output@end and \pcol@icolumncolor with $\langle pfx \rangle =$ @box to have γ_0^c .

The macro \pcol@ifccdefined $\langle then \rangle \langle else \rangle$ is used in \pcol@output@start and \pcol@scancst@shadow to examine whether $\hat{\gamma}_0^c = \text{\pcol\pcolumncolor} \cdot c$ is defined and to do $\langle then \rangle$ if so or $\langle else \rangle$ otherwise.

The macro $\protect\p$

```
1212 \def\pcol@ccuse#1{\@nameuse{pcol@columncolor#1\number\pcol@currcol}}
1213 \def\pcol@ifccdefined#1#2{%
1214 \expandafter\ifx\csname pcol@columncolor\number\pcol@currcol\endcsname\relax
1215 #2\else#1\fi}
1216 \def\pcol@ccxdef#1{%
1217 \expandafter\xdef
```

```
1218 \csname pcol@columncolor@box\number\pcol@currcol\endcsname{#1}}
```

11.5 Footnote Handling

\pcol@savefootins

The macro \pcol@savefootins $\langle cs \rangle$, invoked from \pcol@makecol for page-wise footnotes and from \pcol@output@switch for both column-wise and page-wise footnotes, saves \footins to an \insert register obtained by \@next from \@freelist, and \defines $\langle cs \rangle$ being \pcol@currfoot or \pcol@footins so that it has the register as its body and the register is then saved into $\pi^f(p)$ or $\kappa_c(\tau)$. We save not only \box component of \footins but also \count, \dimen and \skip^{180}.

```
1220 %% Special Output Routines: Footnote Handling
1221
1222 \def\pcol@savefootins#1{%
1223 \@next#1\@freelist{%
1224 \global\setbox#1\box\footins
1225 \global\count#1\count\footins
1226 \global\dimen#1\dimen\footins
1227 \global\skip#1\skip\footins}{\def#1{\voidb@x}\pcol@ovf}}
1228
```

\pcol@shrinkcolbyfn

The macro \pcol@shrinkcolbyfn $\langle height\rangle\langle ins\rangle\langle skip\rangle$, invoked from \pcol@makecol, \pcol@ioutputelt, \pcol@startcolumn, \pcol@restartcolumn, \pcol@flushcolumn and \pcol@makeflushedpage, shrinks $\langle height\rangle\in\{\ensuremath{\male}\mbox{\ma$

```
1229 \def\pcol@shrinkcolbyfn#1#2#3{%

1230 \ifx#3\relax\else #3-\skip#2\relax \fi

1231 \advance#1-\ht#2\advance#1-\dp#2\advance#1-\skip#2\relax}
```

\pcol@unvbox@cclv

The macro $\colonormal{pcol@unvbox@cclv}\langle ins\rangle$, invoked from $\colonormal{pcol@makecol}$ and $\colonormal{pcol@flushcolumn}$ when they work on a column-page with page-wise footnotes, adds the stretch and shrink components of $\colonormal{lskip}\langle ins\rangle$ at the end of $\colonormal{lbox255}$, where $\colonormal{lbox255}$ is non-void $\colonormal{lbox255}$ having page-wise footnotes. Before the addition, the macro goes back to the baseline of $\colonormal{lbox255}$ to nullify the baseline progress mechanism so as to make it sure the exact amount of the vertical skip is added. Then it adds the stretch and shrink by at first adding the skip itself and then the negative amount of its natural component.

```
1232 \def\pcol@unvbox@cclv#1{%
1233 \@tempdima\dp\@cclv \unvbox\@cclv
1234 \vskip \ifdim\@tempdima>\@maxdepth -\@maxdepth \else -\@tempdima \fi
1235 \vskip\skip#1\@tempdima\skip#1\vskip-\@tempdima}
```

 $^{^{180}\}mathrm{Knowing}$ these three components are virtually constants.

 $^{^{181}}$ The comparison of the depth of **\box255** and **\@maxdepth** and taking the latter if it is smaller is really just-in-case.

\pcol@deferredfootins

The macro $\pool@deferredfootins \langle macro \rangle$, invoked from $\pool@startcolumn$ and $\pool@restartcolumn$, tries to $\poole insert$ some of leading deferred footnotes in $\poole insert$. In order to avoid that $\poole insert$ some of leading deferred footnotes in $\poole insert$. In order to avoid that $\poole insert$ has footnotes across three or more pages to make confusion in the order of footnotes kept inside of $\poole insert$, we cap the total height of footnotes by $\poole insert$ has already shrunk by non-deferred footnotes in the page we are working on indicated by $\poole insert$ has already shrunk by non-deferred footnotes in the page does not have non-deferred footnotes indicated by $\poole insert$ had is, we extract leading elements of $\poole insert$ by $\poole insert$ them through $\poole insert$ had, if some elements are obtained in $\poole insert$ them through $\poole insert$ had a leading $\poole insert$ them through $\poole insert$ had a leading $\poole insert$ ha

Note that we temporarily let \splitmaxdepth = \@maxdepth, \splittopskip = 0 and \vbadness = ∞ at the \vsplit so that the depth of the split first half is \@maxdepth at deepest, the second half does not have any skip at its top, and TEX will not complain of (almost) inevitable underfull. Also note that the successful extraction of the leading elements is examined by checking \ht\@tempboxa and thus we need to \unvbox it in itself because \vsplit makes the height h regardless of its contents.

```
1237 \def\pcol@deferredfootins#1{%
1238
      \ifdim\@tempdimb=\z@ \@tempdimb\@colht \advance\@tempdimb-\skip\footins
1239
      \else \@tempdimb\@colht
1240
1241
      \ifvoid\pcol@topfnotes\else \ifdim\@tempdimb>\z@
1242
        \begingroup
          \splitmaxdepth\@maxdepth \splittopskip\z@ \vbadness\@M
1243
          \setbox\@tempboxa\vsplit\pcol@topfnotes to\@tempdimb
1244
          \ifvoid\pcol@topfnotes\else
1245
             \global\setbox\pcol@topfnotes\vbox{\penalty\interlinepenalty
1246
               \unvbox\pcol@topfnotes}%
1247
1248
          \setbox\@tempboxa\vbox{\unvbox\@tempboxa}%
1249
1250
          \ifdim\ht\@tempboxa>\z@
            \pcol@Log#1{add}\@tempboxa
1251
            \insert\footins{\unvbox\@tempboxa}%
1252
1253
          \fi
1254
        \endgroup
1255
      fi\fi
1256
```

\pcol@combinefootins \pcol@putfootins

The macro $\c occupied combine footins \langle b \rangle \langle f \rangle$, invoked solely from $\c occupied combined constructs the pre-environment stuff in <math>\c occupied combining$ the stuff in the box b and pre-environment footnotes in the $\c occupied combined co$

The null vertical skip is put for page-wise footnotes, for which the macro \pcol@putfootins is invoked from \pcol@ioutputelt and \pcol@makeflushedpage. Since we shrink the height

 $^{^{182} \}text{The argument} \ \langle macro \rangle$ has the invoker itself shown in debug messages.

¹⁸³And thus having the arguments $\langle b \rangle$ and $\langle f \rangle$ is unnecessary, but we keep this implementation to avoid unnecessary recoding from a development version.

¹⁸⁴We avoid null space insertion to minimize the difference from older versions in traced output.

of column-pages by the height-plus-depth of page-wise footnotes, the natural height of the box in which column-pages and page-wise footnotes are combined would be less than \textheight due to the depth of the last footnote line if we simply made the footnotes the last items of the box. Though this shortage at most \maxdepth is expected to be covered by the stretch factor of \skip\footins without too large badness causing an underfull message¹⁸⁵, someday we could face an underfull with some unusual settings of \maxdimen, \skip\footins and/or \vbadness. Therefore, we put a null vertical skip so that the real bottom of the footnotes, instead of the last baseline, is placed at the baseline of the box, to make the natural height of the box is \textheight exactly. Note that this shifting page-wise footnotes up will not make last baselines of footnotes among pages unaligned, because the last line have a strut.

```
1257 \def\pcol@combinefootins#1#2{%
      \setbox\@outputbox\vbox{%
1258
        \boxmaxdepth\@maxdepth
1259
        \unvbox#1\relax
1260
        \pcol@putfootins#2\unskip
1261
        \ifdim\belowfootnoteskip=\z@\else \vskip\belowfootnoteskip \fi}}
1262
1263 \def\pcol@putfootins#1{%
      \vskip\skip#1\relax
1264
      \color@begingroup
1265
1266
        \normalcolor
1267
        \footnoterule
        \unvbox#1\relax
1268
      \color@endgroup \vskip\z@}
1269
1270
```

11.6 Marginal Notes

\@addmarginpar \pcol@addmarginpar \pcol@@addmarginpar The macro \pcol@addmarginpar is our own version of \@addmarginpar, which \pcol@zparacol makes \let-equal to \pcol@addmarginpar keeping its original definition in \pcol@addmarginpar. Therefore, in an paracol environment, the \output request made by LATEX's \marginpar in the column c and page p is processed by \pcol@addmarginpar through our own \output routine being \pcol@output, \pcol@specialoutput and LATEX's \@specialoutput. What we do in this macro are as follows; determine the margin which a marginal note goes to; temporarily modify the parameter $m_w = \text{marginparwidth}$ or $m_s = \text{marginparsep}$ according to the margin and the column; determine the position to place the marginal note consulting $\pi^m(p) = \text{pcol@mparbottom}$ obtained by \pcol@getcurrpage: and update $\pi^m(p)$ according to the position.

First, there are the following parameters to determine the margin, and thus the value of \if@firstcolumn referred to in LATEX's \@addmarginpar and meaning left if true or right if false.

- (1) The macros \pcol@mpthreshold@1 and \pcol@mpthreshold@r defined by \marginpar threshold give us the threshold of the column number to let columns less than it go to the left margin while those equal to or greater than it to the right, according to the parallel-page the column belongs to. Therefore, we let \if@firstcolumn = true iff $c < \pcol@mpthreshold@1 \land c < C_L \text{ or } c < \pcol@mpthreshold@r \land c \ge C_L, \text{ as the fundamental setting.}$
- (2) If ∞ is given to \times was plicitly or implicitly, the decision in (1) is reversed if $page(p) \mod 2 = 0$, and then this

¹⁸⁵With default settings of \maxdimen = 5 pt and the stretch factor 4 pt of \skip\footins, the badness $100 \times (5/4)^3 \approx 195$ is significantly less than the default \vbadness = 1000.

decision is reversed again if $c \geq C_L$ and \ifpcol@paired = false to mean c is in a non-paired right parallel-page. The second reversal is done because page(p) is common to both left and right parallel-pages and is for the left page in usual cases without page number jumps. Therefore, $(page(p) \mod 2)$ is for left parallel-pages and thus for right counterparts the decision should be made by $((page(p) + 1) \mod 2)$ and thus the result should be reversed.

(3) If \if@reversemargin is made true by LATEX's \reversemarginpar, the decision made by (1) and then possibly reversed by (2) is finally reversed.

Second, we calculate

$$D = \texttt{\colored{Qtempdima}} = \sum_{d=C^0}^{swap(c)-1} \left(w_{swap(d)} + g_{swap'(d)} \right)$$

where x' = swap(x) is given by $pcol@swapcolumn\langle x\rangle\langle x'\rangle\langle C^0\rangle\langle C^1\rangle$ to let $x' = C^1 - (x - C^0) - 1$ if ifpcol@swapcolumn = true and $page(p) \mod 2 = 0$ or x' = x otherwise, $swap'(x) = pcol@colsepid \in \{swap(x)-1,x\}$ according to swapped or not, $(C^0,C^1) \in \{(0,C_L),(C_L,C)\}$ according to $c < C_L$ or not, and w_x and g_x are the width of x-th column and gap given by pcol@columnwidth x and pcol@columnsep x respectively. That is, D is the distance from the left edge of the column c to that of leftmost column in the (paralell-) page in which c resides. Then if if@firstcolumn = true to let the margial note go to the left margin, we add c to c to c to the marginal note at the point apart from the column's left edge by c the left edge of the marginal note at the point apart from the column's left edge of the leftmost column. On the other hand if if@firstcolumn = false, we add c to that of the rightmost column, to c to that of the rightmost column, to c to that of the rightmost column, to c to the point apart from the column's right edge by c to that of the rightmost column, to c to the point apart from the column's right edge by c to that of the rightmost column, to c to the point apart from the column's right edge by c to that of the rightmost column, to c to the point apart from the column's right edge by c to the rightmost column.

Third, we let \pcol@marbox be the first element of \@currlist obtained by \@xnext for the right marginal note if \if@firstcolumn = false, or \@currbox for the left marginal note otherwise. Then we let $t = \@def{marginal}$ be the distance from the top edge of the column to that of the marginal note, namely \@pageht minus the height of \pcol@marbox plus \dimen\@currbox being downward shift amount optionally given by \marginnote. We also let $h = \@def{marginal}$ be the height-plus-depth of the box \pcol@marbox plus \marginparpush, or in other words the vertical space the marginal note requires. Then we give t and t to \pcol@getmparbottom to let \@mparbottom have the bottom of the exisiting marginal text below which we put the margial text in \pcol@marbox, and to let \pcol@mpblist have the new list to be replaced with $M_{\{L,R\}}^{\{l,r\}}$ in $\pi^m(p)$.

Forth, we update $\pi^m(p)$ with the new list in \pcol@mpblist by a process similar to \pcol@ setpageno but with \pcol@setmpbelt to scan the list of pages Π^+ .

Fifth, we shift down \pcol@marbox by \dimen\@currbox and, if the shift amount is greater than the height of the box and thus the height of shifting result is zero, decrement \@mparbottom by the amount to deceive LATEX's \@addmarginpar into believing \@mparbottom is above the real one by the amount. In other words, by the decrement we let \@addmarginpar see the top edge of the shifted marginal note in the box, rather than that of the box itself, for the placement with \@mparbottom.

Finally, we invoke LATEX's original \@addmarginpar being \pcol@@addmarginpar to put the marginal note according to \if@firstcolumn, temporarily modified \marginparsep and

\marginparwidth, and \@mparbottom. Note that since \pcol@zparacol lets \if@twocolumn = true, \pcol@@addmarginpar determine the margin only by \if@firstcolumn. Also note that it can be \@mparbottom > t (before decrement with the positive shift amount) to mean the marginal note should be shifted down from its natural position, and if so \pcol@addmarginpar will give us a warning as the correct consequence of the placement.

```
1271 %% Special Output Routines: Marginal Notes
1272
1273 \def\pcol@addmarginpar{%
1274
      \pcol@getcurrpage \@firstcolumntrue
1275
      \ifnum\pcol@currcol<\pcol@ncolleft
        \let\reserved@a\z@ \let\reserved@b\pcol@ncolleft
        \ifnum\pcol@mpthreshold@l>\pcol@currcol\else \@firstcolumnfalse \fi
1277
1278
1279
        \let\reserved@a\pcol@ncolleft \let\reserved@b\pcol@ncol
        \ifnum\pcol@mpthreshold@r>\pcol@currcol\else \@firstcolumnfalse \fi
1280
1281
      \ifpcol@swapmarginpar
1282
        \ifodd\c@page\else
1283
          \ifOfirstcolumn \Ofirstcolumnfalse \else \Ofirstcolumntrue \fi
1284
1285
1286
        \ifpcol@paired\else \ifnum\pcol@currcol<\pcol@ncolleft\else
          \ifOfirstcolumn \Ofirstcolumnfalse \else \Ofirstcolumntrue \fi
1288
        \fi\fi
1289
      \fi
1290
      \if@reversemargin
        \ifOfirstcolumn \Ofirstcolumnfalse \else \Ofirstcolumntrue \fi
1291
1292
      \pcol@swapcolumn\pcol@currcol\count@\reserved@a\reserved@b
1293
      \@tempdima\z@
1294
      \@tempcnta\reserved@a \@whilenum\@tempcnta<\count@\do{%
1295
        \pcol@swapcolumn\@tempcnta\@tempcntb\reserved@a\reserved@b
1296
1297
        \advance\@tempdima\csname pcol@columnwidth\number\@tempcntb\endcsname\relax
        \advance\@tempdima\csname pcol@columnsep\pcol@colsepid\endcsname\relax
1298
       \advance\@tempcnta\@ne}%
1299
      \if@firstcolumn \advance\marginparwidth\@tempdima
1300
1301
      \else
1302
        \advance\marginparsep\textwidth \advance\marginparsep-\@tempdima
1303
        \advance\marginparsep-\columnwidth
1304
      \expandafter\@xnext\@currlist\@@\pcol@marbox\@gtempa
1305
      \if@firstcolumn\let\pcol@marbox\@currbox \fi
1306
      \@tempdima\@pageht \advance\@tempdima-\ht\pcol@marbox
1307
1308
      \advance\@tempdima\dimen\@currbox
      \@tempdimb\ht\pcol@marbox \advance\@tempdimb\dp\pcol@marbox
      \advance\@tempdimb\marginparpush
1310
1311
      \pcol@getmparbottom\@tempdima\@tempdimb
1312
      \begingroup
        \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
1313
1314
        \edef\reserved@a{\pcol@pages\pcol@currpage}%
        \global\let\pcol@pages\@empty \global\let\pcol@currpage\@empty
1315
        \let\@elt\pcol@setmpbelt \reserved@a
1316
1317
      \endgroup
      \ifdim\dimen\@currbox=\z@\else
```

```
1319 \ifdim\dimen\@currbox>\ht\pcol@marbox
1320 \advance\@mparbottom-\dimen\pcol@marbox
1321 \fi
1322 \setbox\pcol@marbox\hbox{\lower\dimen\@currbox\box\pcol@marbox}%
1323 \fi
1324 \pcol@@addmarginpar}
1325
```

\pcol@getmparbottom \pcol@getmparbottom@i \pcol@getmpbelt The macro \pcol@getmparbottom $\langle t \rangle \langle h \rangle$ is solely used in \pcol@addmarginpar¹⁸⁶ to let $B = \text{\col} = \text{\col}$

First we examine if $\pi^m(p) = \text{pcol@mparbottom}$ is empty and if so we simply let B = 0 and M' = (mpar(t, t + h)) because there are no marginal notes in the page p at all. Otherwise we obtain $M \in \{M_X^x \mid X \in \{L, R\}, \ x \in \{l, r\}\}$ in \reserved@a according to the side margin to which the new marginal note m goes to, i.e., according to \iff@firstcolumn and $c < C_L$ or not, by \pcol@getmparbottom@i giving it the body of $\pi^m(p)$ by \expandafter. Then we apply \pcol@getmpbelt to each $mpar(t_i, b_i) \in M$ to have $t_k = \min\{t_i \mid t_i \geq t, \ t_i - \max(t, b_{i-1}) \geq h\}$ and let $B = b_{k-1}$ and

```
M' = (mpar(t_1, b_1), \ldots, mpar(t_{k-1}, b_{k-1}), mpar(max(t, B), max(t, B) + h), mpar(t_k, b_k), \ldots, mpar(t_n, b_n))
```

where n=|M|, assuming $b_0=0$. That is, we try to find the first avilable gap between marginal notes below t to accommodate the marginal note m of h tall. Then if such t_k is not found because $t>t_n$ to mean m appears below the last marginal note as in natural cases, or $t_i-\max(t,b_{i-1})< h$ for all t_i s.t. $t_i>t$ to mean there are no available gaps, we let $B=t_n$ and $M'=(M,mpar(\max(t,B),\max(t,B)+h))$ to place m at the bottom.

```
1326 \def\pcol@getmparbottom#1#2{%
      \global\@mparbottom\z@
1327
      \ifx\pcol@mparbottom\@empty
1328
        \begingroup
1329
          \@tempdimc#2\relax \advance\@tempdimc#1\relax \let\@elt\relax
1330
          \xdef\pcol@mpblist{\@elt{\number#1}{\number\@tempdimc}}%
1331
        \endgroup
1332
1333
      \else
        \expandafter\pcol@getmparbottom@i\pcol@mparbottom
1334
1335
        \begingroup
          \@tempdima#1\relax \@tempdimb#2\relax \@tempswafalse
1336
          \let\@elt\pcol@getmpbelt \global\let\pcol@mpblist\@empty \reserved@a
1337
1338
          \if@tempswa\else
            \ifdim\@tempdima<\@mparbottom \@tempdima\@mparbottom \fi
1339
            \advance\@tempdimb\@tempdima
1340
            \@cons\pcol@mpblist{{\number\@tempdima}{\number\@tempdimb}}%
1341
1342
          \fi
1343
        \endgroup
1345 \def\pcol@getmparbottom@i#1#2#3#4{%
```

 $^{^{186}}$ Thus giving t and h as arguments is not necessary but we dare to do it.

```
1346
      \ifnum\pcol@currcol<\pcol@ncolleft
        \if@firstcolumn \def\reserved@a{#1}\else\def\reserved@a{#2}\fi
1347
1348
      \else
        \if@firstcolumn \def\reserved@a{#3}\else\def\reserved@a{#4}\fi
1349
      fi
1350
1351 \def\pcol@getmpbelt#1#2{%
      \ifdim#1sp<\@tempdima
1352
        \global\@mparbottom#2sp\relax \@cons\pcol@mpblist{{#1}{#2}}%
        \ifdim\@tempdima<#2sp\relax \@tempdima#2sp\relax \fi
1354
1355
      \else
1356
        \@tempdimc\@tempdima \advance\@tempdimc\@tempdimb
        \ifdim#1sp<\@tempdimc
1357
          \@tempdima#2sp\relax \global\@mparbottom#2sp\relax
1358
          \@cons\pcol@mpblist{{#1}{#2}}%
1359
1360
          \cons\pcol@mpblist{{\number\@tempdima}{\number\@tempdimc}\@elt{#1}{#2}}
1361
1362
          \def\pcol@getmpbelt##1##2{\@cons\pcol@mpblist{{##1}{##2}}}
1363
1364
        \fi
1365
      fi
1366
```

\pcol@setmpbelt \pcol@setmpbelt@i

The macro $\protect\operatorname{pcol@setmpbelt}\{\pi^p(q)\} \langle \pi^i(q) \rangle \langle \pi^f(q) \rangle \{\pi^s(q)\} \{\pi^m(q)\}\$ is used solely in $\protect\operatorname{pcol@setmpbelt}\{\pi^p(q)\} \langle \pi^i(q) \rangle \langle \pi^j(q) \rangle \langle$ addmarginpar and is applied to Π^+ to update an element $M \in \{M_X^x \mid X \in \{L, R\}, x \in l, r\}$ in $\pi^m(p)$ with M' = pcol@mpblist given by pcol@getmparbottom. The structure of the macro is similar to \pcol@setpnoelt to upadate $\pi^p(q)$ s.t. $q \geq p$, but in this macro the target of the update is only p. Then for q = p, we invoke \pcol@setmpbelt@i giving it the body of $\pi^m(p)$ being $\{M_L^l\}\{M_L^r\}\{M_R^r\}\{M_R^r\}$, or $\langle\emptyset\rangle\langle\emptyset\rangle\langle\emptyset\rangle\langle\emptyset\rangle$ if $\pi^m(p)=\emptyset$, to obtain what $\pi^m(p)$ should have in $\pi_{new}^m(p) = \mathbf{X} = \mathbf{X}$ is replaced with M', where X = L or X = R if $C < C_L$ or not respectively, and x = l or x = r if \iftheta if \iftheta if \iftheta it column = true or not respectively, and then update $\pi^m(p)$ by $\pcol@defcurrpage{\pi^p(p)}\langle \pi^i(p)\rangle\langle \pi^f(p)\rangle\{\pi^s(p)\}\{\pi^m_{new}(q)\}.$

```
1367 \def\pcol@setmpbelt#1#2#3#4#5{%
     {\let\@elt\relax \xdef\pcol@pages{\pcol@pages\pcol@currpage}}%
     \ifnum\@tempcnta=\z@
1369
       \def\reserved@a{#5}%
1370
1371
       \ifx\reserved@a\@empty \pcol@setmpbelt@i{}{}{}\else \pcol@setmpbelt@i#5\fi
1372
       \pcol@defcurrpage{#1}{#2}{#3}{#4}{\reserved@a}%
1373
     \else \gdef\pcol@currpage{\@elt{#1}#2#3{#4}{#5}}%
1374
     \advance\@tempcnta\m@ne}
1375
1376 \def\pcol@setmpbelt@i#1#2#3#4{%}
     \ifnum\pcol@currcol<\pcol@ncolleft
1377
       \if@firstcolumn \def\reserved@a{{\pcol@mpblist}{#2}{#3}{#4}}%
1378
                      1379
       \else
       \fi
1380
     \else
1381
       \ifOfirstcolumn \def\reservedOa{{#1}{#2}{\pcolOmpblist}{#4}}%
1382
                     1383
       \else
       \fi
1384
     \fi}
1385
```

\pcol@mparbottom@zero The macro $\mathcal{M}_0 = \text{pcol@mparbottom@zero is used in }\$ $\protect\pro$ mpar(0,0) for all elements $M \in \{M_X^x \mid X \in \{L,R\}, x = \{l,r\}\}$ to mean a page has no marginal notes carrying over from the preceding paracol environments.

As for \mathcal{M} , besides the top level initialization to make it \mathcal{M}_0 , it is updated in \pcol@ output@end through macros \pcol@getmparbottom@last and \pcol@bias@mpbout to have the last element of each $M \in \{M_X^x \mid X \in \{L,R\}, x = \{l,r\}\}$ in $\pi^m(p_t)$ with transformation from coordinates of columns to that of text area, or directly with \mathcal{M}_0 if the last page will not have post-environment stuff. The resulting \mathcal{M} is at first used in \pcol@output@end itself through \pcol@do@mpbout to let \@mparbottom have the value b of mpar(t,b) in M_L^t or M_L^t according to the side margin which marginal notes in post-environment stuff goes to.

Then \mathcal{M} is passed to the next paracol environment if it resides in the page where the previous environment also resides, to be referred to by \pcol@output@start which also performs \pcol@do@mpbout and \pcol@bias@mpbout to let $\pi^m(0)$ have the lists according to \mathcal{M} and \@mparbottom which can be modified in post-environment stuff of the previous environment or in other word in pre-environment stuff of starting envionment. By this setting of $\pi^m(0)$, marginal note placement in the starting page is aware of the marginal notes having been placed in previous environments and in pre-environment stuff and thus can correctly examines if a marginal note to be added in a margin collide the last one in the margin. On the other hand, if the post-environment stuff encounters a page break before a new environment starts, our own \@outputpage should be invoked at the page break to let $\mathcal{M} = \mathcal{M}_0$ because the marginal notes in previous environments do not afffect those in the new environment.

```
\label{local_condition} $$1387 \gdef\pcol@mparbottom@zero{\{\elt{0}{0}}{\elt{0}{0}}{\elt{0}{0}}{\elt{0}{0}}} $$1388 \global\et\pcol@mparbottom@out\pcol@mparbottom@zero} $$1389 $$
```

\pcol@do@mpbout@i \pcol@do@mpbout@whole \pcol@do@mpbout@elem The macro \pcol@do@mpbout is used in \pcol@output@start and \pcol@output@end to perform operations specified by \pcol@do@mpbout@whole and \pcol@do@mpbout@elem. The macro just invokes \pcol@do@mpbout@i giving it all $M \in \{M_X^x \mid X \in \{L,R\}, x \in \{l,r\}\}$ by \expandafter.

Then \pcol@do@mpbout@i determines the side margin $x \in \{l, r\}$ letting x = l iff \if@mparswitch = true, $page(p) \mod 2 = 0$ and \if@reversemargin = false, to invoke \pcol@do@mpbout@whole giving it all M but M_L^x whose sole element mpar(t, b) may be modified by \pcol@do@mpbout@elem\@elt{t}\}.

In $\c M$ with all M and $\c M$ docump bout elem is expanded to mpar(0,B), where $B=\c M$ marging other elements unchanged. In $\c M$ keeping other elements unchanged. In $\c M$ with all M away into a $\c M$ while $\c M$ bottom of the last marginal note in the side margin specified by M is passed to post-environment stuff through $\c M$ margin specified.

```
1390 \def\pcol@do@mpbout{\expandafter\pcol@do@mpbout@i\pcol@mparbottom@out}
1391 \def\pcol@do@mpbout@i#1#2#3#4{\@tempcnta\@ne
1392 \if@mparswitch \ifodd\c@page\else \@tempcnta\m@ne \fi\fi
1393 \if@reversemargin \@tempcnta-\@tempcnta \fi
1394 \ifnum\@tempcnta<\z@
1395 \pcol@do@mpbout@whole{\pcol@do@mpbout@elem#1}{#2}{#3}{#4}%
1396 \else
1397 \pcol@do@mpbout@whole{#1}{\pcol@do@mpbout@elem#2}{#3}{#4}%
1398 \fi}
```

\pcol@bias@mpbout \pcol@bias@mpbout@i The macro \pcol@bias@mpbout{y} is used in \pcol@output@start with -y being the heighplus-depth of pre-environment stuff, in \pcol@output@end with y being that of spanning stuff in the last page, and in \pcol@getmparbottom@last{y} with its argument y. The macro modifies mpar(t,b) in all $M \in \{M_X^x \mid X \in \{L,R\}, x \in \{l,r\}\}$ of \mathcal{M} so that they have mpar(t+y,b+y) for the transformation from text area coordinates to columns in the first and third, while for the reverse transformation in the second, by invoking \pcol@do@mpb@all giving it \mathcal{M} and letting \reserved@a have \pcol@bias@mpbout@i{y}. That is, \pcol@bias@mpbout@i{y}\@elt{t}{b}\@nil is then invoked in \pcol@do@mpb@all@ii with t and b from mpar(t,b) in each M, and then it \defines \reserved@b with mpar(t+y,b+y) so that updated M has it.

```
1400 \def\pcol@bias@mpbout#1{\def\reserved@a{\pcol@bias@mpbout@i{#1}}%
1401 \pcol@do@mpb@all\pcol@mparbottom@out}
1402 \def\pcol@bias@mpbout@i#1\@elt#2#3\@nil{%
1403 \dimen@#2sp\relax \advance\dimen@#1\relax
1404 \dimen@ii#3sp\relax \advance\dimen@ii#1\relax
1405 \def\reserved@b{\@elt{\number\dimen@}{\number\dimen@ii}}}
1406
```

\pcol@getmparbottom@last \pcol@getmparbottom@last@i

The macro \pcol@getmparbottom@last{y} is used solely in \pcol@output@end to let $\mathcal{M} = \{m_L^l\}\{m_R^r\}\{m_R^r\}$, where $m_X^x = mpar(t_n, b_n) \in M_X^x$, $n = |M_X^x|$ assuming $mpar(t_0, b_0) = mpar(y, y)$, and y is the negative counterpart of the height-plus-depth of the spanning stuff in the last page. Therefore, \mathcal{M} is let have the occupancy information of the last marginal note if any, or the top edge of text area otherwise, in each margin.

The macro at first examines if $\pi^m(p_t) = \emptyset$ and, if so, lets all elements in \mathcal{M} have (mpar(y,y)) by letting it \mathcal{M}_0 and then adding y to each t=b=0 by \pcol@bias@ mpbout giving it y. Otherwise, i.e., if $\pi^m(p_t) \neq \emptyset$, it invokes \pcol@do@mpb@all giving it $\pi^m(p_t)$ and letting \reserved@a have \pcol@getmparbottom@last@i{y}. That is, \pcol@getmparbottom@last@i{y}mpar(t_1,b_1) \cdots mpar(t_n,b_n)\@nil is then invoked in \pcol@do@mpb@all@ii for each M_X^x to let \reserved@b have mpar(y,y) at first and then to let it have $mpar(t_i,b_i)$ for all $i \in [1,n]$. Therefore, \reserved@b should finally have $mpar(t_n,b_n)$ assuming $t_0=b_0=y$, and then becomes m_X^x .

```
1407 \def\pcol@getmparbottom@last#1{%
      \ifx\pcol@mparbottom\@empty
1409
        \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
1410
        \pcol@bias@mpbout{#1}%
1411
      \else
        \def\reserved@a{\pcol@getmparbottom@last@i{#1}}%
1412
        \pcol@do@mpb@all\pcol@mparbottom
1413
1414
1415 \def\pcol@getmparbottom@last@i#1#2\@nil{%
      \edef\reserved@b{\@elt{\number#1}{\number#1}}%
1416
      \def\@elt##1##2{\def\reserved@b{\@elt{##1}{##2}}}%
1417
      #2\let\@elt\relax}
1418
1419
```

\pcol@do@mpb@all \pcol@do@mpb@all@i \pcol@do@mpb@all@ii The macro \pcol@do@mpb@all\lambdall\la

 $mpar(t_n, b_n)$ \@nil invokes \reserved@a giving it all of $mpar(t_i, b_1)$ at once to process them and to have the result in \reserved@b being added to \mathcal{M} .

```
1420 \end{figure} 1420 \end{
1421 \def\pcol@do@mpb@all@i#1#2#3#4{\begingroup \let\@elt\relax
                                   \gdef\pcol@mparbottom@out{}%
1422
                                   \pcol@do@mpb@all@ii#1\@nil\pcol@do@mpb@all@ii#2\@nil
1423
                                   \pcol@do@mpb@all@ii#3\@nil\pcol@do@mpb@all@ii#4\@nil
1424
1425
                                   \endgroup}
1426 \def\pcol@do@mpb@all@ii#1\@nil{%
1427
                                   \reserved@a#1\@nil
1428
                                   \xdef\pcol@mparbottom@out{\pcol@mparbottom@out{\reserved@b}}}
1429
```

11.7 Synchronization

\pcol@sync

The macro \pcol@sync is invoked solely from \pcol@output@switch for explicit synchronization in the following three cases in which \ifpcol@sync \lor \ifpcol@clear = true commonly.

- \ifpcol@sync \ ¬\ifpcol@clear to mean ordinary synchronized column-switching.
- \ifpcol@sync \ \ifpcol@clear to mean pre-flushing column height check.
- ¬\ifpcol@sync ∧ \ifpcol@clear to mean page flushing.

In any cases¹⁸⁷, first we invoke \pcol@flushcolumn for all $c \in [0, C)$ to flush the current column-page of c into S_c if the column-page is not in p_t , i.e., $\kappa_c(\beta^p) < p_t$ and then, if we have deferred floats, to ship out following float pages up to $p_t - 1$ into S_c and to place them in p_t . This float placement in p_t is only for top and bottom floats in synchronized column-switching, while a float column may be made in other cases. Then we ship out all pages p such that $p < p_t$ by \pcol@outputcolumns giving argument 1. After that, we obtain the page context of p_t by \pcol@getcurrpinfo.

Next, we measure the vertical sizes of the contents in the current column-page of c which is now in p_t for all $c \in [0, C)$ by \pcol@measurecolumn as follows, where h(x) and d(x) are the height and depth of an object x respectively.

$$\sigma = \texttt{\floatsep} \qquad \sigma_t = \begin{cases} \kappa_c(\xi) & \kappa_c(\xi) < \infty \\ \texttt{\textfloatsep} & \kappa_c(\xi) = \infty \end{cases} \qquad \sigma_b = \texttt{\textfloatsep}$$

$$f_c(t) = (\kappa_c(\lambda_t) \neq ()) \qquad f_c(m) = (\kappa_c(\beta) \neq \texttt{\textfloatsep})$$

$$f_c(f) = (\kappa_c(\tau) \neq \bot) \qquad f_c(b) = f_c(b') = (\kappa_c(\lambda_b) \neq ())$$

$$F_c(X) = \exists x \in X : f_c(x) \qquad f_b = \texttt{\textfloatsep}$$

$$v_c(t) = \texttt{\textfloatsep}$$

$$v_c(t) = \texttt{\textfloatsep}$$

$$v_c(t) = \texttt{\textfloatsep}$$

$$v_c(m) = h(\kappa_c(\beta)) + d(\kappa_c(\beta))$$

$$v_c(m) = h(\kappa_c(\beta)) + d(\kappa_c(\beta))$$

$$v_c(f) = h(\kappa_c(\tau)) + d(\kappa_c(\tau))$$

$$v_c(b) = \sum_{\phi \in \kappa_c(\lambda_b)} (h(\phi) + d(\phi)) + (|\kappa_c(\lambda_b)| - 1) \cdot \sigma + \sigma_b$$

$$v_c(b') = v_c(b) + \sigma_b$$

 $[\]overline{}^{187}$ In the last case of page flushing, invoking \pcol@flushcolumn is redundant because it is made $p=p_t$ by pre-flushing column height check always preceding the flushing, but the invocation is harmless.

That is, V_T is the maximum of combined vertical size (height plus depth) of the top floats and the main vertical list, V_B is that of the footnotes and bottom floats, and V_P is that of all items. V_P' is similar to V_P but we add \textfloatsep to the size of bottom floats. Note that V_T , V_P and V_P' are $-\infty$ if any column-pages don't have corresponding items, while $V_B = 0$ if so. Also note that c_{max} is the ordinal of the column whose size is V_P .

 D_T and D_P are the minimum δ_c and d_c respectively among those gives V_T and V_P' respectively, where δ_c is $\kappa_c(\delta)$ if $f_m = true$ or ∞ otherwise, and d_c is 0 if c has bottom float, or the depth of the last footnote if any and without any bottom float, or $\kappa_c(\delta)$ otherwise. The reason why D_T and D_P have minimums is that they are set into \prevdepth for the items just following the synchronization point, and thus a smaller value results in a larger interline skip and the special value $-1000\,\mathrm{pt}$ to inhibit the skip by, e.g., \nointerlineskip, is given the highest priority.

Note that V_P' and D_P are only for the last page and thus referred to by \pcol@output@end to close the environment, and the former is done by \pcol@makeflushedpage if it works on the page. The reason why we add \textfloatsep to V_P' is to make the last page well separated from the post-environment stuff if the tallest column, taking the addition into account, has bottom floats. Also note that we let \ifpcol@dfloats = false before scanning columns with \pcol@measurecolumn so that the switch becomes true after the scan iff a column has deferred floats (in the last page).

```
1430 %% Special Output Routines: Synchronization
1431
1432 \def\pcol@sync{%
1433 \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do\pcol@flushcolumn
1434 \pcol@outputcolumns\@ne
1435 \pcol@getcurrpinfo{\global\c@page}{\global\@colht}{\global\topskip}%
1436 \@tempdima-\maxdimen \@tempdimb-\maxdimen \pcol@colht-\maxdimen
1437 \@pageht-\maxdimen \@tempdimc\maxdimen \@pagedp\maxdimen \@tempcntb\z@
1438 \pcol@dfloatsfalse
```

As described above, any items can be empty, naturally for top floats, footnotes and bottom floats, but also including main vertical lists if the current column-pages were not in p_t before the invocation of \c all main vertical lists can be empty if all leading column-pages just have started (by \c page, for example). More weirdly, the case of all-empty main vertical lists can be accompanied with other non-empty items when columns have floats or footnotes which cannot be in p_t-1 but are found their places in p_t .

Taking it into account that any items can be empty and the other item of page-wise footnotes, we have to determine whether the following two operations are taken; invocation of
\pcol@synccolumn for each column-page to set a synchronization point or to add an infinite stretch (and shrink) to its bottom; and the examination of the height of each columnpage, taking the synchronization point to be set into account, to tell the necessity of explicit
page break with \ifpcol@flush = true. For the latter we calculate the examination target $V = \text{Qtempdimb} \text{ to be compared with } \pi^h(p_t), \text{ while for the former we determine the value of}$ a switch f = ifQtempswa so that we invoke \pcol@synccolumn iff f = true and V > 0.

For synchronized column-switching with \ifpcol@clear = false, we let $f = (V_T \ge 0)$ to mean at least one column-page has a top float or non-empty main vertical list, i.e., $F_c(\{t,m\}) = true$ for some $c \in [0,C)$. That is if $V_T < 0$, since the next items added to all column-pages are placed at the top of the page¹⁸⁸, we don't need to set synchronization points in them. As for V, we let $V = \max(V_T,0) + \max(V_B,0) + v^f$ where v^f is the sum of height-plus-depth of $\pi^f(p_t)$ and \skip· $\pi^f(p_t)$ if p_t has page-wise footnotes, or 0 otherwise¹⁸⁹. Note that it can be $V_P + v^f \le \pi^h(p_t) < V_T + V_B + v^f = V$ to mean setting the synchronization point at V_T below p_t 's top edge would push bottom stuff beyond its bottom edge and thus we need an explicit page break to place the point at the top of $p_t + 1$ (in usual cases).

For pre-flushing column height check or page flushing with \ifpcol@clear = true on the other hand, we let $f = \neg \text{locol@sync}$ to invoke \pcol@synccolumn only for page flushing and thus not for pre-flushing column height check. As for V, we let $V' = V_P'$ or $V' = V_P$ according as we working on last page or not, and then let $V = \max(V', 0) + v^f$ or V = V' according as p_t has page-wise footnotes or not. That is, we have to invoke \pcol@synccolumn unless p_t is perfectly empty.

Then if \ifpcol@clear = false and $\max(V, V - D_T' + V_E) > \pi^h(p_t)$ where $D_T' = D_T$ if $0 \le D_T < \infty$ or 0 otherwise, or \ifpcol@clear = true and $V > \pi^h(p_t)^{190}$, we flush the page. That is, if the condition above holds, we let \ifpcol@flush = true and $d = \text{pcol@nextcol} = c_{\max}$ to tell \pcol@switchcol or \pcol@flushclear to make an explicit page break in the column c_{\max} from which we restart, and f = false to skip \pcol@synccolumn to postpone the explicit synchronization. Note that the bias $V_E = \text{pcol@ensurevspace}$ in synchronized column-switching is to avoid breaking a column-page just below the synchronization point due to too small space below the point, less than \baselineskip in default but can be other threshold explicitly defined by \ensurevspace. That is, since $V - D_T + k$ \baselineskip usually means the vertical position at which k-th baseline below the synchronization point is placed, the flushing condition with $V_E = k$ \baselineskip ensures that the page is flushed iff the space below the point cannot accommodate k lines. Also note that necessary flushing with

 $^{^{188}}$ In usual cases, but it can mean some of them have negative vertical sizes. Even though we can detect such a very unlikely special case, it is very tough to define the reasonable synchronization point above the top of p_t . Therefore, we assume the point is at the top of p_t and thus do nothing.

¹⁸⁹In the real implementation, $V = -\infty$ if $V_T = V_B = -\infty$ and no page-wise footnotes are presented, but this difference does not affect the decisions because $f \wedge (V \ge 0) = (V_T < 0) \wedge (V \ge 0) = false$ and $V \le \pi^f(p_t)$ with either V = 0 or $V = -\infty$.

¹⁹⁰The examination is redundant in page flushing with \ifpcol@sync = false because it is assured that no overflow happens in any column-page by pre-flushing column height check and explicit page breaking, but is not harmful.

 $V > \pi^h(p)$ assuredly takes place even when D_T is unusually large and/or V_E is negative to make $-D_T + V_E < 0$.

Finally if $V \geq 0$ and f = true, we invoke \pcol@synccolumn for each column $c \in [0, C)$ to set a synchronization point in it or to add an infinite stretch (and shrink) at its bottom for flushing.

```
\@tempswatrue \global\pcol@flushfalse
1440
      \ifpcol@clear
1441
        \ifpcol@lastpage \@tempdimb\pcol@colht \else \@tempdimb\@pageht \fi
1442
        \ifpcol@sync \@tempswafalse \fi
1443
1444
        \ifdim\@tempdima<\z@
                                    \@tempswafalse
1445
        \else\ifdim\@tempdimb<\z@ \@tempdimb\@tempdima
1446
        \else
                                    \advance\@tempdimb\@tempdima
1447
        \fi\fi
1448
1449
      \fi
      \ifpcol@scfnote\ifvoid\pcol@footins\else
1450
        \ifdim\@tempdimb<\z@ \@tempdimb\z@ \fi
1451
        \advance\@tempdimb\ht\pcol@footins \advance\@tempdimb\dp\pcol@footins
1452
        \advance\@tempdimb\skip\pcol@footins
1453
      \fi\fi
1454
      \dimen@\@tempdimb
1455
      \ifpcol@clear\else \ifdim\dimen@<\z@\else
1456
1457
        \ifdim\@tempdimc=\maxdimen\else \ifdim\@tempdimc<\z@\else
1458
          \advance\dimen@-\@tempdimc
1459
        \fi\fi
        \advance\dimen@\pcol@@ensurevspace
1460
        \ifdim\dimen@<\@tempdimb \dimen@\@tempdimb \fi
1461
      \fi\fi
1462
      \ifdim\dimen@>\@colht
1463
        \global\pcol@flushtrue \@tempswafalse \pcol@nextcol\@tempcntb
1464
1465
      \ifdim\@tempdimb<\z@\else \if@tempswa
1466
        \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do\pcol@synccolumn
1467
      \fi\fi}
1468
1469
```

\pcol@flushcolumn

The macro \pcol@flushcolumn is invoked for each column $c \in [0, C)$ from \pcol@sync to ship out the current column-page of c into S_c if it is not leading one, i.e., $p = \kappa_c(\beta^p) < p_t$. The macro also ships out float pages from p+1 up to p_t-1 if we have deferred floats to fill them and, if this float flushing still leaves deferred floats, puts some of them to the leading column-page being current now as its top and/or bottom floats.

First we obtain the column-context in κ_c by \pcol@getcurrcol and examines if $p = \kappa_c(\beta^p) < p_t$. If it does not hold to mean c has leading column-page, we do nothing.

Otherwise, we save \ifpcol@lastpage into \ifpcol@lastpagesave turning the former switch false because we are working on a non-leading column-page definitely in a non-last page. Then we put the contents of the current column-page $\kappa_c(\beta^b)$ adding \vfil at its tail into \box255 being the TEX's standard interface to carry the main vertical list for \output routine. We also move everything in $\kappa_c(\tau)$ obtained by \pcol@getcurrfoot into \footins and return $\kappa_c(\tau)$ to \@freelist if $\kappa_c(\tau^b)$ is not void.

Then we obtain p's page context by $\pcol@getcurrpage$ and, if it has page-wise footnotes in $\pi^f(p)$, we shrink $\pcol@getcurrpage$ and stretch/shrink components of $\scalebox{skip} \cdot \pi^f(p)$ at the bottom of $\bcol@getcurrpage$ by $\pcol@getcurrpage$ and add the stretch/shrink components of $\scalebox{skip} \cdot \pi^f(p)$ at the bottom of $\bcol@getcurrpage$ by $\pcol@getcurrpage$ and, if it has page-wise footnotes in $\calebox{shrink} \cdot \pi^f(p)$, we shrink $\calebox{shrink} \cdot \pi^f(p)$ at the bottom of $\bcol@getcurrpage$ by $\calebox{shrink} \cdot \pi^f(p)$ at the bottom of $\calebox{shrink} \cdot \pi^f(p)$.

unvbox@cclv, as we did in \pcol@makecol. Otherwise we take a special care of the case that the height-plus-depth of $\kappa_c(\beta^b)$ is greater than $\pi^h(p)$ due to that its height is almost equal to $\pi^h(p)$ and thus its depth makes the hight-plus-depth exceeding $\pi^h(p)$. This excess is revealed by the \vfil we just have added making the height-plus-depth the height of \box255, and would cause overfull in \@makecol and \pcol@@makecol because they need the height, i.e., not height-plus-depth, of \box255 not exceeding $\pi^h(p)$. Therefore if it happens, we we remove the \vfil and cap the height of \box255 by \@maxdepth to pretend as if the box is directly passed from TeX's page builder.

Next we examine if $\kappa_c(\rho_t)$ was made ∞ by \pcol@makefcolumn invoked from this macro itself when it processed the column-page in the previous pre-flushing column height check for environment closing, which found a page break should be done. That is, $\kappa_c(\rho_t) = \infty$ means the current column-page was once judged to be in the last page but pre-flushing column height check forced a page break to make it non-last, it should have all deferred floats now listed in $\kappa_c(\lambda_t)$ at \end{paracol}, but their total size is less than the threshold to make a usual float column for the last page. If so, since the page is not last now, we put all floats in $\kappa_c(\lambda_t)$ by \pcol@makefcolpage as the ship-out image in \@outputbox, ignoring the contents added to \box255 in the operations above because $\kappa_c(\beta^b)$ should be empty, and letting $\kappa_c(\rho_t) = 0$ to mean the floats have been processed 191.

Otherwise, since the column-page can be put as usual, we invoke \pcol@makecol^{192} giving \@maxdepth to it to build the complete column-page in \@outputbox with depth capping and with the following setting 193.

```
\label{eq:constraints} \begin{array}{ll} \texttt{\ hox255} = \kappa_c(\beta^b) & \texttt{\ hootins} = \kappa_c(\tau) & \texttt{\ hootins} = \pi^h(\kappa_c(\beta^p)) \\ \texttt{\ hootins} = \kappa_c(\lambda_h) & \texttt{\ hootins} = \kappa_c(\lambda_t) & \texttt{\ hootins} = \kappa_c(\lambda_b) \\ \end{array}
```

Finally, regardless of $\kappa_c(\rho_t) = \infty$ or not, the resulting \Quad Quutputbox becomes $s_c(p)$ and is added to the tail of S_c by \Quad Qcons.

```
1470 \def\pcol@flushcolumn{%
      \pcol@getcurrcol
1471
1472
      \ifnum\count\@currbox<\pcol@toppage
        \ifpcol@lastpage \pcol@lastpagesavetrue \else \pcol@lastpagesavefalse \fi
1473
        \pcol@lastpagefalse
1474
        \pcol@page\count\@currbox
1475
        \setbox\@cclv\vbox{\unvbox\@currbox \vfil}%
1476
        \ifvoid\pcol@currfoot\else
          \pcol@Fb
1478
          \@cons\@freelist\pcol@currfoot
1479
1480
          \pcol@Fe{flushcolumn(colfn)}%
1481
1482
        \pcol@getcurrfoot\box
        \pcol@getcurrpage
1483
        \ifvoid\pcol@footins
1484
          \ifdim\ht\@cclv>\@colht
1485
1486
            \setbox\@cclv\vbox{\boxmaxdepth\@maxdepth \unvbox\@cclv \unskip}%
1487
        \else
          \pcol@shrinkcolbyfn\@colht\pcol@footins\relax
1489
```

 $^{191\}kappa_c(\lambda_t)$ can have any values other than ∞ because definitely it will not be referred to in its inherent sense in the situation with no further float additions and no deferred floats.

¹⁹² Neither \pcol@makecol because \box255 has \vfil at its tail and the column-page should be short enough, nor \@makecol because we need to ensure the depth of resulting \@outputbox is capped.

 $^{^{193}\}mbox{LMT}_{\mbox{E}}\mbox{X's has another $\mbox{\sc insert named $\mbox{\sc of hargepage} but paracol does not cares about it.}$

```
\setbox\@cclv\vbox{\pcol@unvbox@cclv\pcol@footins}%
1490
        \fi
1491
        \pcol@Logstart{\pcol@flushcolumn(\number\c@page:\number\pcol@currcol)}
1492
        \ifdim\@toproom=\maxdimen
1493
          \setbox\@outputbox\pcol@makefcolpage \global\@toproom\z@
1494
1495
          \pcol@@makecol\@maxdepth
1496
        \fi
1497
        \pcol@Logend\pcol@flushcolumn
1498
        \global\setbox\@currbox\box\@outputbox
1499
        \expandafter\@cons\csname pcol@shipped\number\pcol@currcol\endcsname
1500
1501
          \@currbox
```

Then for each $q \in [p+1, p_t-1]$, we repeat the followings; get q's page context by $\color getcurrpage$; shrink $\color getcurrp$

```
\advance\pcol@page\@ne
1502
1503
        \int {\tt ifx\@deferlist\@empty\else}
          \@whilenum\pcol@page<\pcol@toppage\do{%
1504
             \pcol@getcurrpage
1505
            \ifvoid\pcol@footins\else
1506
               \pcol@shrinkcolbyfn\@colht\pcol@footins\relax
1507
            \fi
1508
1509
             \@makefcolumn\@deferlist
             \if@fcolmade
1510
               \pcol@Fb
1511
               \@next\@currbox\@freelist{\global\setbox\@currbox\box\@outputbox}%
1512
1513
                 \pcol@ovf
               \pcol@Fe{flushcolumn(fcol)}%
1514
1515
               \expandafter\@cons
                 \csname pcol@shipped\number\pcol@currcol\endcsname\@currbox
1516
            \fi
1517
            \advance\pcol@page\@ne}%
1518
1519
```

Next, since we reach p_t and thus restore \ifpcol@lastpage from \ifpcol@lastpagesave because the top page can be last. Then we acquire the current column-page of c which is now in p_t and thus empty, by \@next. Then we let \@colht = \@colroom = $\pi^h(p_t)$ by \pcol@getcurrpinfo but shrinking them by \pcol@shrinkcolbyfn if p_t has page-wise footnotes, and reinitialize the float placement parameters by \pcol@floatplacement. Then, if $\kappa_c(\lambda_d)$ still has some floats, we make a float column for some of them in the top page by \pcol@makefcolumn if \ifpcol@clear = true meaning flushing, or try to move some of them to $\kappa_c(\lambda_t) = \text{Qtoplist}$ and/or $\kappa_c(\lambda_b) = \text{Qbotlist}$ by \pcol@trynextcolumn otherwise. Note that since \@colroom is used in \pcol@makefcolumn as a working register, we let \@colroom = $\pi^h(p_t)$ again after its invocation. After that we save column-context including those given by \pcol@floatplacement and modified by \pcol@makefcolumn or \pcol@trynextcolumn into κ_c by \pcol@setcurrcolnf because all footnotes are shipped out, and let $\kappa_c(\beta^p) = p_t$. We also let $\kappa_c(\beta^r) = \text{Qcolroom}$ possibly modified by \pcol@trynextcolumn but after canceling the shrinkage of \@colht due to page-wise footnotes, i.e., $\kappa_c(\beta^r) \leftarrow \kappa_c(\beta^r) + (H - H')$ where H and H' are \@colht before and after the shrinkage respectively.

1520 \ifpcol@lastpagesave \pcol@lastpagetrue \fi

```
\pcol@Fb
1521
         \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{}}\pcol@ovf
1522
        \pcol@Fe{flushcolumn(col)}%
1523
         \pcol@getcurrpinfo\@tempcnta{\global\@colht}\@tempskipa
1524
         \@pageht\@colht
1525
         \ifvoid\pcol@footins\else \pcol@shrinkcolbyfn\@colht\pcol@footins\relax \fi
1526
         \global\@colroom\@colht \pcol@floatplacement
1527
         \int \end{array} \end{array} \end{array} \end{array} \end{array}
1528
           \ifpcol@clear
1529
             \pcol@makefcolumn \global\@colroom\@colht
1530
1531
           \else
             \pcol@trynextcolumn
1532
         \fi\fi
1533
         \pcol@setcurrcolnf
1534
         \global\count\@currbox\pcol@toppage
1535
         \advance\@pageht-\@colht \advance\@pageht\@colroom
1536
1537
         \global\dimen\@currbox\@pageht
      \fi %\ifnum\count\@currbox<\pcol@toppage
1538
      \advance\pcol@currcol\@ne}
1539
1540
```

\pcol@makefcolumn

The macro $\polemath{\mbox{pcol@makefcolumn}}$ is invoked solely from $\polemath{\mbox{pcol@flushcolumn}}$ to put deferred floats in the currently empty column-page of c in the top page p_t which is being flushed. Since we have to take special care of the case of environment closing, we cannot do this operation by $\mbox{\mbox{@makefcolumn}}$, while in other cases for $\polemath{\mbox{flushpage}}$ and $\polemath{\mbox{clearpage}}$ we also have to pay a small attention.

First, we scan the copy of $\kappa_c(\lambda_d)$ applying \pcol@makefcolelt to each element to have the floats to be put in \@toplist, which is assuredly empty because the current column-page of c has already been shipped out to empty it, and those still deferred in $\kappa_c(\lambda_d)$. Prior to scan, we let $H_r = \pi^h(p_t)^{194} + \alpha$, as the space initially available for floats each of which being ϕ is assumed to consume $v(\phi) = h(\phi) + d(\phi) + \alpha$, and $H_t = \text{Qcolroom} = -\alpha$ as the initial value of the accumulated size of $v(\phi)$ for all ϕ to be put, where $\alpha = \text{lloatsep}$ if \ifpcol@lastpage = true as discussed afterward, or $\alpha = \text{Qfpsep}$ otherwise.

Then if the resulting $\ensuremath{\mathbb{Ne}} \ensuremath{\mathbb{Ne}} \ensuremath{\mathbb{Ne$

 $^{194\}pi^h(p_t)$ referred in this macro may have been shrunk by page-wise footnotes in \pcol@flushcolumn. 195It can happen if the first float is larger than $\pi^h(p_t)$.

¹⁹⁶We dare to do it knowing the natural component of \floatsep is a little bit (4pt) larger than that \@fpsep and the possibility of having fewer floats than those given by \@makefcolumn.

force a page break making p_t non-last. Also note that, in any cases, letting $\kappa_c(\rho_t) = \infty$ is safe because no longer we will have any float additions to the column-page.

Otherwise, i.e., if we are working on a non-last page to be flushed or a float column is to be made for the last page, we put all floats in \mathbb{C}^b toplist in a \mathbb{C}^b tall by \mathbb{C}^b another \mathbb{C}^b be another \mathbb{C}^b another \mathbb{C}^b tall by the float column is necessary because $\kappa_c(\beta^b)$ can be put back to the main vertical list after the pre-flushing column height check to remove skips above and below the floats, namely \mathbb{C}^b and \mathbb{C}^b the contents were not encapsulated.

```
1541 \def\pcol@makefcolumn{%
      \ifpcol@lastpage \@tempdimc\floatsep \else \@tempdimc\@fpsep \fi
1542
      \@tempdima\@colht \advance\@tempdima\@tempdimc \global\@colroom-\@tempdimc
1543
1544
      \begingroup
        \let\@elt\pcol@makefcolelt
1545
        \let\reserved@b\@deferlist
1546
1547
        \global\let\@deferlist\@empty
1548
        \reserved@b
      \endgroup
1549
      \ifx\@toplist\@empty\else
1550
        \@tempswatrue
1551
        \ifpcol@lastpage \ifx\@deferlist\@empty \ifdim\@colroom<\@fpmin
1552
1553
          \@tempswafalse \global\@toproom\maxdimen
1554
        \if@tempswa \global\setbox\@currbox\vbox{\pcol@makefcolpage}\fi
1555
1556
```

\pcol@makefcolelt

The macro $\polemath{\mbox{\mbox{$\sim$}}}$ is invoked solely from $\polemath{\mbox{\mbox{$\sim$}}}$ due to each float element ϕ in (the copy of) $\kappa_c(\lambda_d)$. We examine if $v(\phi) = h(\phi) + d(\phi) + \alpha \leq H_r$ to mean the float column being built has room large enough for the float ϕ . If so, we add ϕ to $\polemath{\mbox{$\sim$}}$ to mean the float column being built has room large enough for the float ϕ . If so, we add ϕ to $\polemath{\mbox{$\sim$}}$ to make it deferred again, and let $H_t \leftarrow H_t + v(\phi)$. Otherwise, we add ϕ to $\polemath{\mbox{$\kappa$}}_c(\lambda_d)$ by $\polemath{\mbox{$\sim$}}$ cons to make it deferred again, and let $H_r = -\infty$ so that the examinations for any succeeding elements fail.

```
1557 \def\pcol@makefcolelt#1{%
1558 \Qtempdimb\ht#1{}\advance\Qtempdimb\Qp#1{}\advance\Qtempdimb\Qtempdimc
1559 \ifdim\Qtempdimb>\Qtempdima \Qcons\Qdeferlist#1\relax
1560 \Qtempdima-\maxdimen
1561 \else \Qcons\Qtoplist#1\relax
1562 \advance\Qtempdima-\Qtempdimb \global\advance\Qcolroom\Qtempdimb
1563 \fi}
```

\pcol@makefcolpage

The macro \pcol@makefcolpage is invoked from \pcol@flushcolumn, \pcol@makefcolumn and \pcol@imakeflushedpage to build a float column having floats in \@toplist, which is then returned to \@freelist and then emptied. The floats are put in a \vbox of \@colht tall with vertical skips of \@fptop, \@fpsep and \@fpbot above, between and below them respectively. The box is then let be $s_c(p)$ or $\kappa_c(\beta^b)$ explictly or implicitly by the invokers, with an encapsulation in the case of \pcol@makefcolumn.

```
1564 \def\pcol@makefcolpage{\vbox to\@colht{%}
1565 \vskip\@fptop \vskip-\@fpsep
1566 \def\@elt##1{\vskip\@fpsep\box##1}\@toplist \vskip\@fpbot}%
1567 \pcol@Fb
1568 \xdef\@freelist{\@freelist\@toplist}\global\let\@toplist\@empty
1569 \pcol@Fe{makefcolpage}%
1570 }
```

\pcol@measurecolumn

The macro \pcol@measurecolumn is invoked for each column $c \in [0,C)$ from \pcol@sync to measure the sizes of the top floats $size_c(t)$, main vertical list $size_c(m)$, footnotes $size_c(f)$ and bottom floats $size_c(b)$ in the current column-page in the page p_t . After obtaining the column-context in κ_c by \pcol@getcurrcol, we calculate $size_c(t) = \skip \cdot \kappa_c(\beta)$ by \pcol@addflhd giving it $\kappa_c(\lambda_t)$ and $\kappa_c(\xi) = \pcol@textfloatsep$ as its arguments also to have \if@tempswa = $f_c(t)$. Note that $\kappa_c(\xi) = \infty$ means the column-page does not have any synchronization points yet and thus \textfloatsep is used in the calculation as the skip between the top floats and main vertical list, while the value itself possibly for a MVL-float discussed later is used if $\kappa_c(\xi) < \infty$. We also calculate $size_c(m) = h(\kappa_c(\beta)) + d(\kappa_c(\beta))$, and then the sum of it and $size_c(t)$.

```
1572 \def\pcol@measurecolumn{%
```

- 1573 \pcol@getcurrcol
- 1574 \@tempswafalse
- 1575 \dimen@\z@ \pcol@addflhd\@toplist\pcol@textfloatsep
- 1576 \global\skip\@currbox\dimen@
- 1577 \advance\dimen@\ht\@currbox \advance\dimen@\dp\@currbox \dimen@ii\dimen@

Next we examine if the main vertical list $\kappa_c(\beta^b)$ is empty by \pcol@ifempty and, if so, we let $\delta_c = \kappa_c(\delta) = \infty$ and save it (together with others) by \pcol@setcurrcol so that, if the column defines the V_T finally by its top floats, D_T is let ∞ and the fact that the column has empty list is remembered. Otherwise, we let $\delta_c = \kappa_c(\delta)$ and \if@tempswa = true to represent $F_c(\{t,m\}) = f_t \vee f_m$ because $f_m = true$. Then we invoke \pcol@measureupdate to let $V_T = size_c(t) + size_c(m) = SIZE_c(\{t,m\})$ and $D_T = \delta_c$ if $F_c(\{t,m\}) = true$ and $V_T < SIZE_c(\{t,m\})$.

- 1578 \pcol@ifempty\@currbox
- 1579 {\global\pcol@prevdepth\maxdimen \pcol@setcurrcol}%
- 1580 {\@tempswatrue}%
- 1581 \pcol@measureupdate\@tempdima\dimen@ii\@tempdimc\pcol@prevdepth

Next we let $size_c(f) = 0$ if $\kappa_c(\tau^b)$ is void, or otherwise let $size_c(f) = h(\kappa_c(\tau^b)) + d(\kappa_c(\tau^b)) + \kappa_c(\tau^s)^{197}$ and \if@tempswa = true because $f_c(f) = true$ and thus $F_c(\{t, m, f\}) = true$. After that, we calculate $size_c(f) + size_c(b)$ by \pcol@addflhd giving it $\kappa_c(\lambda_b)$ and ∞ to mean \textfloatsep should be used for the calculation as its argument also to have \if@tempswa = $F_c(\{t, m, f, b\})$. Then we let $V_B = size_c(f) + size_c(b)$ if $V_B < size_c(f) + size_c(b)$, and let $V_P = size_c(t) + size_c(m) + size_c(f) + size_c(b) = SIZE_c(\{t, m, f, b\})$ and $c_{\max} = c$ if $F_c(\{t, m, f, b\}) = true$ and $V_P < SIZE_c(\{t, m, f, b\})$.

```
1582 \ifvoid\pcol@currfoot \dimen@\z@
```

1583 \else

 $\label{limin_limit} 1584 \qquad \verb|\dimen@\ht\pcol@currfoot| advance\dimen@\dp\pcol@currfoot| \\$

1585 \advance\dimen@\skip\pcol@currfoot

1586 \@tempswatrue

1587 \fi

1588 \pcol@addflhd\@botlist\maxdimen

1589 \ifdim\dimen@>\@tempdimb \@tempdimb\dimen@ \fi

1590 \advance\dimen@\dimen@ii

1591 \if@tempswa \ifdim\dimen@>\@pageht

1592 \@pageht\dimen@ \@tempcntb\pcol@currcol

1593 \fi\fi

 $^{^{197}}$ We ignore the height and depth of **\footnoterule** because they are expected to be 0 and are so in the default setting.

Next, we let d_c be the depth of the lowest non-empty items among the main vertical list, footnotes and bottom floats. That is, we let $d_c \leftarrow \kappa_c(\delta)$ at first, and then, if \ifpcol@bfbottom = true, override it by $d_c \leftarrow d(\kappa_c(\tau^b))$ if there are footnotes, and finally override it by $d_c \leftarrow 0$ for the bottom floats if exist adding \textfloatsep to $SIZE_c(\{t, m, f, b\})$ to have $SIZE_c(\{t, m, f, b'\})$. This overriding order of $d(\kappa_c(\tau^b))$ and then 0 by bottom floats is reversed when \ightharpoonup if pcol@bfbottom = false according to the implementation of \@makecol. Then, we invoke \pcol@measureupdate again to let $V_P' = SIZE_c(\{t, m, f, b'\})$ and $D_P = d_c$ if $F_c(\{t, m, f, b\}) = true \text{ and } V_P' < SIZE_c(\{t, m, f, b'\}).$ It also lets $D_P = d_c$ if $F_c(\{t, m, f, b\}) = true$ true, $V_P' = SIZE_c(\{t, m, f, b'\})$ and $D_P > d_c$.

Finally, we let \ifpcol@dfloats = true if $\kappa_c(\lambda_d) \neq \emptyset$ to tell \pcol@makeflushedpage that the last page must be full size and \pcol@output@end to flush the deferred column-wise floats.

```
\dimen@ii\pcol@prevdepth
1594
      \ifpcol@bfbottom
1595
        \ifvoid\pcol@currfoot\else \dimen@ii\dp\pcol@currfoot \fi
1596
        \ifx\@botlist\@empty\else \dimen@ii\z@ \advance\dimen@\textfloatsep \fi
1597
1598
        \ifx\@botlist\@empty\else \dimen@ii\z@ \advance\dimen@\textfloatsep \fi
1599
1600
        \ifvoid\pcol@currfoot\else \dimen@ii\dp\pcol@currfoot \fi
1601
      \pcol@measureupdate\pcol@colht\dimen@\@pagedp\dimen@ii
1602
      \ifx\@deferlist\@empty\else \pcol@dfloatstrue \fi
1603
      \advance\pcol@currcol\@ne}
1604
```

\pcol@hdflelt

\pcol@addflhd The macro \pcol@addflhd $\langle list \rangle \langle tfs \rangle$ is invoked twice from \pcol@measurecolumn for a column c to measure $size_c(x)$ $(x \in \{t,b\})$ of top (x = t) or bottom (x = b) floats. The arguments and registers referred to in the macro have the followings according to x = t or x = b.

	x = t	x = b
$\langle list \rangle$	$\kappa_c(\lambda_t)$	$\kappa_c(\lambda_b)$
$\langle \mathit{tfs} \rangle$	\pcol@textfloatsep	\maxdimen
\if@tempswa	false	$F_c(\{t, m, f\})$
\dimen@	0	size(f)

The macro is also used in $\cline{1mm}$ to $\cline{1mm}$ and $\cline{1mm}$ to $\cline{1mm}$ \dimen@ having the height of \pcol@prespan for the measurement of the total height of prespanning-text stuff including top floats¹⁹⁸.

The macro at first examines if $\kappa_c(\lambda_x) = \langle list \rangle$ is empty and does nothing if so. Otherwise, \if Otempswa is turned true to have $f_c(t) = true$ for x = t or $F_c(\{t, m, f, b\}) = true$ for x = b. Then we scan all floats in $\langle list \rangle$ applying \pcol@hdflelt to each float ϕ to add $h(\phi) + d(\phi) +$ \floatsep to \dimen@, from/to which we then subtract \floatsep and add σ_x because the last/first float is followed/preceded by the vertical skip of σ_x instead of \floatsep, to have $size_c(t)$ for x = t or $size_c(f) + size_c(b)$ for x = b being returned to \pcol@measurecolumn.

Note that σ_t is $\langle tfs \rangle = \text{pcol@textfloatsep}$ if it is less than ∞ or \textfloatsep otherwise, while $\sigma_b = \text{textfloatsep}$ always because $\langle tfs \rangle = \text{maxdimen}$. Also note that σ_t can be biased by 10000 pt and thus larger than 5000 pt, if we have a MVL-float in top floats as discussed later. Another caution is that we ignore the contribution by \topfigrule nor \botfigrule because they should insert vertical items whose total height and depth are 0.

```
1605 \def\pcol@addflhd#1#2{%
     \ifx#1\@empty\else
```

¹⁹⁸In these invocations, \if@tempswa is meaningless and not examined by the invokers.

```
1607
                                                     \@tempswatrue
                                                    \let\@elt\pcol@hdflelt
1608
                                                    #1\advance\dimen@-\floatsep
1609
                                                     \ifdim#2=\maxdimen \advance\dimen@\textfloatsep
1610
1611
                                                                   \advance\dimen@\pcol@textfloatsep
1612
                                                                  \ifdim\pcol@textfloatsep>5000\p@ \advance\dimen@-\@M\p@ \fi
1613
                                                     \fi
1614
1615
                                                      1616
                                       \fi}
1617 \end{figure} $1617 \end{figure} $177 \e
                                       \advance\dimen@\floatsep}
```

\pcol@measureupdate

The macro \pcol@measureupdate $\langle V \rangle \langle v \rangle \langle D \rangle \langle d \rangle$ is invoked twice in \pcol@measurecolumn for c to update $V \in \{V_T, V_P'\}$ and $D = \{D_T, D_P\}$ as follows if \if@tempswa, being $F_c(\{t, m\})$ for $V = V_T$ or $F_c(\{t, m, f, b\})$ for $V = V_P'$, is true.

$$V \leftarrow \max(V, v) \qquad D \leftarrow \left\{ \begin{array}{ll} \min(D, d) & V = v \\ D & V \neq v \end{array} \right.$$

The arguments v and d have the followings according to V.

$$V = V_T : v = SIZE_c(\{t, m\}) \qquad d = \delta_c$$

$$V = V_P' : v = SIZE_c(\{t, m, f, b'\}) \qquad d = d_c$$

1619 \def\pcol@measureupdate#1#2#3#4{\if@tempswa
1620 \ifdim#1<#2\relax#1#2\relax#3#4\relax

 $1621 \qquad \texttt{\else} if dim #1 = #2 if dim #3 > #4 \relax #3 #4 \fi \fi \fi \fi \fi$

1622

\pcol@synccolumn

The macro \pcol@synccolumn is invoked for each column $c \in [0, C)$ from \pcol@sync to set a synchronization point at V_T from the top of the current column-page of c if \ifpcol@clear = false, or flush it otherwise. After obtaining c's column-context κ_c by \pcol@getcurrcol, we process one of the following three cases.

The first case is for flushing with \ifpcol@clear = true. In this case we simply add \vfil at the tail of the main vertical list in $\kappa_c(\beta^b)$ to make the whole column-page possibly with other items fit in a box of \@colht tall and, if $\kappa_c(\xi) \neq \infty$ to mean the column to be flushed has a synchronization point, we also add an infitite shrink of $1/10000\,\mathrm{fil}$ so as to cancel a finite shrink just below the point, as done in \pcol@makecol^{199}. We also let $\kappa_c(\delta) = 1000\,\mathrm{pt}$ to mimic TeX's mechanism of \prevdepth with the empty main vertical list in the next column-page²⁰⁰.

1623 \def\pcol@synccolumn{%
1624 \pcol@getcurrcol
1625 \ifpcol@clear
1626 \global\pcol@prevdepth\@m\p@
1627 \global\setbox\@currbox\vbox{\unvbox\@currbox}
1628 \ifdim\pcol@textfloatsep=\maxdimen \vfil
1629 \else \vskip\z@\@plus1fil\@minus.0001fil
1630 \fi}%

¹⁹⁹Just in case, because it looks impossible that the natural height of the column-page exceeds $\pi^h(p_t)$ with pre-flushing column height check.

²⁰⁰The author is not sure if this setting is really necessary but, at least, it looks working well (though other

²⁰⁰The author is not sure if this setting is really necessary but, at least, it looks working well (though other setting looks all right too).

The second and third cases are for synchronized column-switching. The second case is for $D_T = \infty$ to mean the synchronization point is set just below the top floats of a column whose main vertical list is empty because it is definitely $V_T \geq 0 > -\infty$. In this case, we should not put anything back to the main vertical list, because the column having defined the point will restart from the top of its column-page with \topskip and thus other columns should do so for the stuff following the point. Therefore, we put $\kappa_c(\beta^b)$ as the last top float, namely MVL-float because it is for the main vertical list, acquiring an \insert from \Offreelist by \Onext and assigning it to \pcolOffloat so that we pretend main vertical lists of all columns are empty.

The float has zero height and depth, and contains the followings if we have some real floats; a vertical skip of $\neg \text{floatsep}$ to go back to the bottom of the last real float; $\land c(\beta^b)$ followed by $\land c(\beta^b)$ form the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ form the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ form the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ from the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ from the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ from the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ form the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ from the last real float; and $\land c(\beta^b)$ followed by $\land c(\beta^b)$ followed by $\land c(\beta^b)$ from the last real float; and $\land c(\beta^b)$ followed by \land

Note that the process above involves \floatsep and \textfloatsep with some finite stretch and shrink, but these factors will not contribute the final result because they are canceled by \vss in the MVL-float and by the small inifinite stretch and shrink put by \pcol@makecol and this macro for flushing. Also note that $\kappa_c(\xi)$ is then biased by 10000 pt so that \pcol@cflt will not put \topfigrule because it has been already put as a part of the MVL-float or we don't have any real floats. We also let $\kappa_c(\delta) = 1000$ to mean the column-page's main vertical list is empty, so as to mimic TEX's mechanism of \prevdepth with an empty list again.

Another attention we have to pay is that column-pages with $\kappa_c(\xi) = \infty$ does not have any synchronization points, and thus $\kappa_c(\xi) < \infty$ means a synchronization has already taken place in them. If this $\kappa_c(\xi) < \infty$ happens with $D_T = \infty^{202}$, we cannot update $\kappa_c(\xi)$ because \pcol@measurecolumn took care of its value on measuring $v_c(t)$. Therefore, we do nothing if $\kappa_c(\xi) < \infty$ but just let succeeding stuff be added to the main vertical list as in column-switching without synchronization.

```
1631
      \else
        \@tempdimb\@tempdima
1632
        \advance\@tempdimb-\skip\@currbox
1633
        \ifdim\@tempdimc=\maxdimen
1634
          \ifdim\pcol@textfloatsep=\maxdimen \begingroup
1635
            \ifx\@toplist\@empty
1636
              \textfloatsep\z@ \floatsep\z@ \let\topfigrule\relax
1637
            \fi
1638
1639
            \pcol@Fb
            \@next\pcol@float\@freelist{\global\setbox\pcol@float\vbox to\z@{%
1640
              \vskip-\floatsep \topfigrule \vskip\textfloatsep
1641
              \unvbox\@currbox \vss}}\pcol@ovf
1642
1643
            \pcol@Fe{synccolumn(topfloat)}%
            \@cons\@toplist\pcol@float
1644
```

 $[\]overline{}^{201}$ This enlarging cannot be done by making the float's height $V_T - v_c(t) - \text{loatsep}$ (or \textfloatsep) because the height can be negative.

²⁰²This can happen when a synchronization with $D_T = \infty$ is immediately followed by another synchronization or, more unlikely, by additions of items whose total amount is negative and then a synchronization.

```
1645 \advance\@tempdimb\textfloatsep \advance\@tempdimb-\floatsep
1646 \advance\@tempdimb\@M\p@
1647 \global\pcol@prevdepth\@m\p@
1648 \global\pcol@textfloatsep\@tempdimb
1649 \endgroup \fi
```

The third and last case is for $D_T < \infty$ and thus most usual. In this case, we enclose everything in $\kappa_c(\beta^b)$ in a \vbox whose height is $h_c^v = V_T - v_c(t)$ and let $\kappa_c(\beta^b)$ have it so that the item following the synchronization point start at V_T . An attention we have to pay is that it can be $h_c^v < \text{topskip}$ to let TEX insert a vertical skip of the difference between them when the box is returned to the main vertical list pushing down the synchronization point a little bit 203 . Therefore, if so, we let $\kappa_c(\beta^b)$ have the followings; a \vbox of \topskip tall having its old contents at its top above which no vertical skip will be inserted; a vertical skip -topskip going back to the page top; and a vertical skip h_c^v going down to the synchronization point.

The encapsulation of the old contents $\kappa_c(\beta^b)$ in the box of h_c^v tall gives us the following two features desirable for synchronization. First, all vertical glues in the box are frozen, nullifying finite stretches in them because we insert an infinite stretch of $1/10000\,\mathrm{fil}$ at the bottom of $\kappa_c(\beta^b)$ to push up its old contents respecting other infinite stretches if any, as done by \raggedbottom, and also nullifying finite and infinite shrinks because $h_c^v \geq v_c(m)$ definitely. This freezing and nullification keeps synchronization points already in $\kappa_c(\beta^b)$ from being observed moving a little bit vertically. That is, if we have a glue just below a synchronization point and it were visible to TeX's page builder, the item below the glue could move up/down when the builder found a break point with some shrink/stretch. Though this moving up/down is inhibited by the small infinite stretch/shrink which the column-page will at its bottom finally, it is undesirable to make TeX misunderstanding that the glues are strethable/shrinkable though they are not in reality.

Second, since the boxes in all column-page are zero deep due to the infinite stretch at their bottoms and these bottoms are aligned at the synchronization point, we have a clear view of the baseline progress after the synchronization regardless of their contents. That is, we let $\kappa_c(\delta) = D_T$ to broadcast D_T to all columns, so that the baselines of first items following the synchronization point are aligned \baselineskip below the bottom baseline of the column which defines D_T^{204} , if D_T plus the hight of each item is less than \baselineskip.

In addition, we let $\kappa_c(\xi) = \text{textfloatsep}$ to indicate the column-page has the synchronization point we just have set, if it was ∞ to mean the point is the first one. By this setting, \pcol@makecol and this macro itself will know that the column-page needs to have a small infinite shrink at its bottom to cancel finite ones below the synchronization point, while \pcol@cflt acts as LATEX's \@cflt because it should be $\kappa_c(\xi) \leq 5000\,\text{pt}$ to mean the column-page does not have a MVL-float.

 $^{^{203}}$ This can happen not very unlikely especially with $v_c(t)$ a little bit less than V_T and $\kappa_c(\beta^b)$ being empty. 204 Since D_T is given by one of the tallest columns whose depth is smallest among them, it is very likely that the bottom baseline of the column is lowest among all columns. However, another column can have the lowest one when its vertical size is a little bit shorter than V_T and its depth is small (e.g., 0). Though of course we can define D_T being V_T minus the height of the column having the largest height to make the first baseline below the synchronization point apart from the lowest one by **\baselineskip**, we dare to choose the definition of D_T because such lowest baseline often means that the column have some skip at its bottom to give us the impression that the space between the baselines of the tallest column and its first item is a little bit too large.

Finally, we let $\kappa_c(\nu_t) = 0$ to inhibit futher addition of top floats because we have fixed the space for them²⁰⁵, and save it and other column-context members into κ_c by \pcol@setcurrcol.

```
1663 \global\@topnum\z@ \pcol@setcurrcol
1664 \advance\pcol@currcol\@ne}
1665
```

11.8 Page Flushing

\pcol@output@flush

The macro \pcol@output@flush is invoked solely from \pcol@specialoutput to process the \output request made by \flushpage. We invoke \pcol@makeflushedpage giving it \@colht as the height of each column-page to have the ship-out image of the top page including its spanning stuff and page-wise footnotes in \@outputbox whose height is then set to be \textheight^{206}, ensureing that its depth is capped by \boxmaxdepth = \@maxdepth. We also perform these height setting and depth capping on \pcol@rightpage if $C_L < C$ to mean parallel-paging. Then we invoke \@outputpage for shipping out, and then finally \pcol@ freshpage to have a new page to start new column-pages in it.

```
1666 %% Special Output Routines: Page Flushing
1667
1668 \def\pcol@output@flush{%
1669
      \pcol@makeflushedpage\@colht
1670
      \pcol@Logstart\pcol@output@flush
      \setbox\@outputbox\vbox to\textheight{\boxmaxdepth\@maxdepth
1671
        \unvbox\@outputbox}%
1672
      \ifnum\pcol@ncolleft<\pcol@ncol
1673
        \setbox\pcol@rightpage\vbox to\textheight{\boxmaxdepth\@maxdepth
1674
          \unvbox\pcol@rightpage}%
1675
1676
      \pcol@Logend\pcol@output@flush
1677
1678
      \@outputpage
      \pcol@freshpage}
```

\pcol@output@clear

The macro \pcol@output@clear is invoked solely from \pcol@specialoutput to process the \output request made by \clearpage. The first part up to \@outputpage and the last line of this macro are same as \pcol@output@flush to flush the top page and to have a newpage. In the remaining mid part, we invoke \pcol@flushfloats to ship out all deferred column-wise floats in all columns if any, and then do it for page-wise floats by the following invocations enclosed in a group; letting \pcol@rightpage = \bot for ordinary paging; \@dblfloatplacement to set up placement parameters followed by \f@depth = 0 to nullify the setting \f@depth = 1sp possiblly done by it as discussed in the item-(2) of §1.8; \@makefcolumn with \@dbldeferlist to have a float page in \@outputbox if any; and a loop of background painting of \@outputbox

²⁰⁵Allowing the addition is tremendously tough even when the column-page has sufficiently large space above the synchronization point.

²⁰⁶ Just in case because the height of source \@outputbox should be exactly \textheight though not specified so on its construction in \pcol@makeflushedpage.

and, if $C_L < C$, of empty \pcol@rightpage, and \@outputpage followed by \@makefcolumn repeated while we have a float page, i.e., \if@fcolmade = true.

Note that the mid part is same as that found in \@doclearpage but we omit various adjuncts surrouding it as follows; examination of \if@twocolumn because we should have multiple columns; examination of \if@firstcolumn because we have to clear the page immediately even when we are not in the first column; concatenating \@dbltoplist with \@dbldeferlist and clearing it because the author believes \@dbltoplist must be empty on the invocation of this macro; and letting \@colht = \textheight because \pcol@flushfloats did it.

```
1681 \def\pcol@output@clear{%
      \pcol@makeflushedpage\@colht
1682
      \pcol@Logstart\pcol@output@clear
1683
      \setbox\@outputbox\vbox to\textheight{\boxmaxdepth\@maxdepth
1684
1685
        \unvbox\@outputbox}%
      \ifnum\pcol@ncolleft<\pcol@ncol
1686
        \setbox\pcol@rightpage\vbox to\textheight{\boxmaxdepth\@maxdepth
1687
1688
          \unvbox\pcol@rightpage}%
1689
      \pcol@Logend\pcol@output@clear
1690
      \@outputpage
1691
      \pcol@flushfloats
1692
1693
      \begingroup
1694
        \setbox\pcol@rightpage\box\voidb@x
        \@dblfloatplacement \let\f@depth\z@
1695
        \@makefcolumn\@dbldeferlist
1696
        \@whilesw\if@fcolmade\fi{%
1697
          \def\pcol@bg@floatheight{\pcol@bg@textheight}%
1698
1699
          \setbox\@outputbox\vbox to\textheight{%
            \pcol@bg@paintbox{Ff}\unvbox\@outputbox}%
1700
          \ifnum\pcol@ncolleft<\pcol@ncol
1701
            \setbox\pcol@rightpage\vbox to\textheight{\pcol@bg@paintbox{Ff}\vfil}%
1702
          \fi
1703
          \@outputpage
1704
1705
          \@makefcolumn\@dbldeferlist}%
1706
      \endgroup
1707
      \pcol@freshpage}
1708
```

\pcol@makeflushedpage

The macro \pcol@makeflushedpage $\langle ht \rangle$ is invoked from \pcol@output@flush or \pcol@output@clear with $\langle ht \rangle = \ensuremath{\text{Qcolht}}$ and from \pcol@output@end with $\langle ht \rangle = \pcol@colht$. At first, we invoke \pcol@output@switch with setting \ifpcol@clear = true to flush all pages up to $p_t - 1$ and to let $\kappa_c(\beta^b)$ have the ship-out image of the main vertical list of each column-page c in p_t . This invocatoin also lets \pcol@colht = V_P' so that hereafter we will refer V_P' throuth $\langle ht \rangle$ if it is \pcol@colht for last page. Then after obtaining p_t 's page context to have $page(p_t) = \pi^p(p_t)$, \@colht = $\pi^h(p_t)$ and \ifpcol@nospan by \pcol@getcurrpinfo, we build the ship-out image of p_t in \@outputbox, and \pcol@rightpage if parallel-paging, taking special care of the last page case as follows.

- (1) If \ifpcol@lastpage = false, each of $\kappa_c(\beta^b)$ has ship-out image even if some or all of them are empty. It is unecessary to be aware of the perfectly empty case because it should mean the page p_t is made blank intentionally.
- (2) If $\forall ifpcol@lastpage = true$ but $\forall ifpcol@dfloats = true$ too, the last page must have full size because we will have parallel columned pages having float columns for deferred

floats. However, if the page has nothing, i.e., $\pi^i(p_t) = \pi^f(p_t) = \bot$ and $V_P' = -\infty$, we must let \@outputbox = \bot (and \pcol@rightpage = \bot as well) to avoid an unnecessary blank page is shipped out. On the other hand, if $\pi^i(p_t) \neq \bot$ or $\pi^f(p_t) \neq \bot$ while $V_P' = -\infty$, we build a full size page as usual but letting \@textbottom = \vfil temporarily to avoid underfull in the process of building columns. Note that if $\pi^f(p_t) \neq \bot$, the page-wise footnotes are always put into \@outputbox regardless \ifpcol@mgfnote because the last page is not combined with post-environment stuff.

- (3) If \ifpcol@lastpage = true, \ifpcol@dfloats = false and $V_P' = -\infty$, we have to let \@outputbox = \bot unless $\pi^i(p_t) \neq \bot$ or $\pi^f(p_t) \neq \bot$ having non-merged footnotes. If $\pi^f(p_t)$ has non-merged footnotes, \@outputbox and \pcol@rightpage must have $\pi^f(p_t)$ possibly with $\pi^i(p_t)$ but without any columns, and must be put into the main vertical list as the leading part of post-environment stuff by modifying $V_P' = 0$. On the other hand $\pi^f(p_t) = \bot$ or it has merged footnotes, \@outputbox must have only $\pi^i(p_t)^{207}$. Since page-wise floats become ordinary floats in post-environment stuff, we cannot paint its background and must remove \dbltextfloatsep at the bottom of $\pi^i(p_t)$.
- (4) If \ifpcol@lastpage = true, \ifpcol@dfloats = false and $V_P' > -\infty$, \@outputpage and \pcol@rightpage must have short columns of V_P' tall, together with $\pi^i(p_t)$ as in non-last pages but without $\pi^f(p_t)$ if it has merged footnotes.

To implement a part of special cares above, we at first let \if@tempswa = true iff \ifpcol@ lastpage = false, $V_P' > -\infty$ or $\pi^f(p_t) \neq \bot$.

1709 \def\pcol@makeflushedpage#1{%

- 1710 \pcol@cleartrue \pcol@output@switch \pcol@clearfalse
- 1711 \pcol@getcurrpinfo{\global\c@page}{\global\@colht}\@tempskipa
- 1712 \ifpcol@lastpage \@tempswafalse \else \@tempswatrue \fi
- 1713 \ifdim\pcol@colht=-\maxdimen\else \@tempswatrue \fi
- 1714 \ifvoid\pcol@footins\else \@tempswatrue \fi

Next, if $\forall ifpcol@nospan = true$ to mean the page p_t does not have spanning stuff in $\pi^i(p_t)$, we initialize both \Coutputbox and \pcolCrightpage to be \perp . Otherwise, after letting $\forall f$ to make the last page full size if we are working on it as discussed in (2), we put $\pi^i(p_t)$ in \Coutputbox, and paint its background by \pcol@bg@ paintbox \edefining the height parameter \pcol@bg@floatheight with h being the heightplus-depth of $\pi^i(p_t)$ with the following two exceptions; one is the case of \ifpcol@firstpage = true to mean we are in starting page and thus the spanning stuff is pre-environment stuff having already been painted by $\pcol@output@start$; and the other is the case of $\ideta false$ to mean we are working on a truly last page being empty except for the spanning stuff itself and thus the page-wise floats become a part of deferred floats in post-environment stuff as discussed in (3). In the latter exceptional case, excluding the case that the last page is also the starting page²⁰⁸, we also remove the last skip being \dbltextfloatsep so that those floats are naturally connected with other floats given in post-environment stuff also as discussed in (3). Then we pack the \@outputbox in itself by \vbox so that any stretch/shrink factors in it cannot affect the ship-out image especially when we paint its background²⁰⁹. Then we do the similar procedure for \pcol@rightpage and make its height and depth equal to those of $\colon 210$. Finally we temporarily add h to \topmargin as done in $\colon 210$.

²⁰⁷\pcol@rightpage must have the couterpart in right parallel-page if the spanning stuff is pre-environment stuff, while it is made \bot by \pcol@output@end if the spanning stuff are page-wise floats.

²⁰⁸Extremely exceptional because the closing environment does not have anything.

 $^{^{209}}$ Though that hardly happens.

²¹⁰If page-wise floats become a part of post-environment stuff's floats, \pcol@rightpage will be made \perp by \pcol@output@end afterward.

so that background painting of columns and so on with infinite extension can reach the paper top edge.

```
1715
      \begingroup
1716
        \ifpcol@nospan
          \global\setbox\@outputbox\box\voidb@x
1717
          \global\setbox\pcol@rightpage\box\voidb@x
1718
1719
          \ifpcol@dfloats \@tempswatrue \fi
1720
          \let\@elt\relax
1721
1722
          \edef\pcol@bg@floatheight{%
1723
            \@elt{\number\ht\pcol@spanning sp}\@elt{\number\dp\pcol@spanning sp}}%
1724
          \def\reserved@a{%
1725
            \ifpcol@firstpage\else \if@tempswa \pcol@bg@paintbox{Ff}\fi\fi}%
1726
          \@tempdima\ht\pcol@spanning \advance\@tempdima\dp\pcol@spanning
1727
          \global\setbox\@outputbox\vbox{%
            \reserved@a \unvbox\pcol@spanning
1728
            \ifpcol@firstpage\else \if@tempswa\else \unskip \fi\fi}%
1729
          \global\setbox\@outputbox\vbox{\box\@outputbox}%
1730
          \pcol@Fb
1731
          \@cons\@freelist\pcol@spanning
1732
1733
          \pcol@Fe{makeflushedpage(spanning)}%
          \ifnum\pcol@ncolleft<\pcol@ncol
1734
            \global\setbox\pcol@rightpage\vbox{%
1735
1736
              \ifpcol@paired\else \advance\c@page\@ne \fi
1737
              \reserved@a \unvbox\pcol@rightpage}%
1738
            \global\ht\pcol@rightpage\ht\@outputbox
            \global\dp\pcol@rightpage\dp\@outputbox
1739
            \global\setbox\pcol@rightpage\vbox{\box\pcol@rightpage}%
1740
          \fi
1741
1742
          \advance\topmargin\@tempdima
```

Next, after \globally letting \globally letting \globally letting \globally letting \globally letting \globally letting \globally because we will ship a page which may be the starting page shortly, we build the ship-out image of columns if required fundamentally by \ifQtempswa = true. First, if the page p_t has page-wise footnotes, we shrink \Qcolht = $\pi^h(p_t)$ by \pcol@shrinkcolbyfn to keep the room for the footnotes, to have $H = \mathbb{Q}$ ing the possibly shrunk $\pi^h(p_t)$ for the reference in \pcol@imakeflushedpage after the further possible modification of \@colht we will make shortly. Second, if \ifpcol@lastpage = true but $\ightharpoonup false$ because we need a full-sized last page, temporarily letting \P we calculate the page of the sized last page of the sized last page of the sized last page. derfull due to perfectly empty column-pages as discussed in $(2)^{211}$. Third, if we are working on a truly last page and $\langle ht \rangle < H$ to mean the tallest column is shorter than H, we let \@colht = $\langle ht \rangle$ to let \@makecol build short column-pages. Note that it is definitely $\langle ht \rangle \leq H$ because the pre-flushing column height check on the last page makes that sure. Fourth and finally, unless all columns in truly last page are empty as discussed in (3), we invoke \pcol@imakeflushedpage $\langle C^0 \rangle \langle C^1 \rangle \langle b \rangle$ once or twice, to put columns in right parallelpage to b = pcol@rightpage with $[C^0, C^1] = [C_L, C]$ if $C_L < C$, and then to put left ones in b = Qoutputbox with $[C^0, C^1) = [0, C_L)$ always²¹².

1744 \global\pcol@firstpagefalse

 $[\]overline{}^{211}$ Each column-page $cc_c(\beta^b)$ itself exists because the empty column-page has been visited by column-scan prior to **\output** request for environment closing.

²¹²The order of right to left is not essential in this macro but we follow the convention in \pcol@outputelt.

```
1745
        \if@tempswa
          \ifvoid\pcol@footins\else
1746
            \pcol@shrinkcolbyfn\@colht\pcol@footins\relax
1747
1748
1749
          \let\pcol@@hfil\relax \@pageht\@colht
          \ifpcol@lastpage \ifpcol@dfloats
1750
            \ifdim\pcol@colht<\z@ \def\@textbottom{\vfil}\fi
1751
            \pcol@lastpagefalse
1752
          \fi\fi
1753
          \ifpcol@lastpage \ifdim#1<\@colht \@colht#1\fi\fi
1754
          \ifdim\@colht<\z@ \else
1755
            \ifnum\pcol@ncolleft<\pcol@ncol
1756
               \pcol@imakeflushedpage\pcol@ncolleft\pcol@ncol\pcol@rightpage
1757
            \fi
1758
             \pcol@imakeflushedpage\z@\pcol@ncolleft\@outputbox
1759
1760
          \fi
        \fi
```

After putting all column-pages, we examine if the page p_t has page-wise footnotes in $\pi^f(p_t)$. If so, and unless p_t is a truly last page and merged footnote typesetting is in effect to mean the page-wise footnotes will be merged with post-environment stuff, we put the footnotes in $\pi^f(p_t)$ below the column-pages. Prior to this however, we let \pcol@fnheight@lpage have the height-plus-depth of the footnote, so that \pcol@output@end know the size for the background painting of the footnotes, which \pcol@imakeflushedpage performed for non-last pages. We also put an empty box of the size into \pcol@rightpage by \pcol@phantom together with the \skip component of $\pi^f(p_t)$ to keep the space necessary especially when p_t is the last page. Then we put the footnotes in $\pi^f(p_t)$ into \@outputpage by \pcol@putfootins, reclaiming the contents of $\pi^f(p_t)$ and letting $\pi^f(p_t) = \bot$ so that \pcol@output@end will be unaware of the footnotes. We also let $V_P' = \text{pcol@colht} = 0$ if p_t is a truly last page and it had $-\infty$ to indicate that the last page is not empty but has footnotes as discussed in (3).

```
\gdef\pcol@fnheight@lpage{0pt}%
1762
        \ifvoid\pcol@footins\else
1763
1764
          \@tempswatrue \ifpcol@lastpage \ifpcol@mgfnote \@tempswafalse \fi\fi
1765
          \if@tempswa
1766
            \pcol@Log\pcol@makeflushedpage{output}\pcol@footins
1767
            \@tempdima\ht\pcol@footins \advance\@tempdima\dp\pcol@footins
            \xdef\pcol@fnheight@lpage{\number\@tempdima sp}%
1768
            \ifnum\pcol@ncolleft<\pcol@ncol
1769
              \global\setbox\pcol@rightpage\vbox{\unvbox\pcol@rightpage
1770
                 \vskip\skip\pcol@footins \nointerlineskip
1771
1772
                 \pcol@phantom\pcol@footins \vskip\z@}%
            \fi
            \global\setbox\@outputbox\vbox{%
1774
              \unvbox\@outputbox \pcol@putfootins\pcol@footins}%
1775
1776
            \@cons\@freelist\pcol@footins \gdef\pcol@footins{\voidb@x}%
1777
            \pcol@Fe{makeflushedpage(pagefn)}%
1778
            \ifdim\pcol@colht=-\maxdimen \global\pcol@colht\z@ \fi
1779
          \fi
1780
        \fi
1781
      \endgroup}
1782
1783
```

\pcol@imakeflushedpage The macro \pcol@imakeflushedpage $\langle C^0 \rangle \langle C^1 \rangle \langle b \rangle$ is invoked solely in \pcol@makeflushedpage

but can be twice with $(C^0, C^1, b) = (C_L, C, \text{pcol@rightpage})$ if parallel-paging is in effect and with $(C^0, C^1, b) = (0, C_L, \text{Qoutputbox})$ always, to build the ship-out image of the right or left parallel-page p_t in the box b already having spanning stuff or its blank counterpart if any, respectively.

After opening the \vbox of the ship-out image for b, at first we examine if \ifpcol@paired = false and $C^0 > 0$, and if so we temporarily increment $page(p_t)$ by one so that we check its parity for mirrored background painting correctly. Then if the page p_t has page-wise footnotes in $\pi^f(p_t)$, we paint its background, or that of its blank counterpart, by \pcol@bg@paintbox \defining the parameter \pcol@bg@footnoteheight with the height-plus-depth of $\pi^f(p_t)$, as the very first element of the ship-out image as done in \pcol@ioutputelt, unless p_t is the truely last page for which the background painting is done in \pcol@output@end. Then we put spanning stuff in b itself if any.

Next, we invoke \pcol@buildcolseprule for column-separating rule drawing and background painting giving it H in \@colht possibly shurnk from $\pi^h(p_t)$ by page-wise footnotes, $[C^0, C^1)$ for the set of columns to be put, and \@maxdepth for non-last pages to paint the backgrounds of columns and column-separating gaps so that those of the last segment reach the page bottom, while for last page we give 0 to let the bottom be the real bottom of the columns. Then we put the painted backgrounds in \@tempboxa immediately.

```
1784 \ensuremath{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox{\mbox
                               \ifpcol@paired\else\ifnum#1=\z@\else \advance\c@page\@ne \fi\fi
1786
                               \ifvoid\pcol@footins\else \ifpcol@lastpage\else
1787
                                           \def\pcol@bg@footnoteheight{%
1788
                                                     \@elt{\ht\pcol@footins}\@elt{\dp\pcol@footins}}%
                                          \pcol@bg@paintbox{Nn}%
1789
                               \fi\fi
1790
                                \unvbox#3\nointerlineskip
1791
                               \ifpcol@lastpage \pcol@buildcolseprule\@colht#1#2\z@
1792
1793
                               \else
                                                                                                                            \pcol@buildcolseprule\@colht#1#2\@maxdepth
1794
1795
                               \unvbox\@tempboxa
```

Now we put columns in a \hbox of $W_T = \text{textwidth}$ wide. That is, for each c, being c' or C-1-c' for the c'-th iteration determined by \pcol@swapcolumn according to the effectiveness of column-swapping and the parity of $page(p_t)$, we obtain c's column-context κ_c by \pcol@getcurrcol, move $\kappa_c(\beta^b)$ into \box255, and let \footins = $\kappa_c(\tau)$ by \pcol@getcurrfoot returning it to \@freelist if c has column-wise footnotes.

²¹³ Not \pcol@makecol because the main vertical list has \vfil and, if it has a synchronization point, a infinite shrink by \pcol@synccolumn at its tail already, and we should not do any special operations for page-wise footnotes. Also it is not \@makecol because we need to ensure the depth of resulting \@outputbox is capped.

page cannot be greater than $\colonormal{$

Then we put the \@outputbox above in a \hbox of \columnwidth wide preceded by \pcol@@ hfil being \relax for the first column, while it is \pcol@hfil\\\\cerc^g\rangle, where $c^g = \text{\pcol@colsepid}$ being c or c-1 without or with column-swapping respectively, to put a column-separating gap possibly with column-separating rule segments in \pcol@tempboxa built by \pcol@buildcolseprule. Finally, we save column-context especially those for float parameters into κ_c by \pcol@setcurrcolnf because all column-wise footnotes have been shipped out.

```
1796
                  \hb@xt@\textwidth{%
                         \@tempcntb#1\@whilenum\@tempcntb<#2\do{%
1797
                               \pcol@swapcolumn\@tempcntb\pcol@currcol#1#2\relax
1798
                               \pcol@getcurrcol
1799
1800
                               \setbox\@cclv\box\@currbox
1801
                               \ifvoid\pcol@currfoot\else
1802
                                      \pcol@Fb
                                     \@cons\@freelist\pcol@currfoot
1803
                                     \pcol@Fe{imakeflushedpage(colfn)}%
1804
1805
                                \pcol@getcurrfoot\box
1806
1807
                                \@tempswafalse
1808
                                \begingroup
                                     \ifdim\@toproom=\maxdimen
1809
                                            \let\topfigrule\relax \ifdim\@colht=\@pageht \@tempswatrue \fi
1810
                                     \fi
1811
                                     \if@tempswa
1812
                                            \pcol@Logstart{\pcol@makeflushedpage(1)}%
1813
                                            \setbox\@outputbox\pcol@makefcolpage
1814
                                            \pcol@Logend{\pcol@makeflushedpage(1)}%
1815
1816
                                            \pcol@Logstart{\pcol@makeflushedpage(2)}%
1817
                                            \ifpcol@lastpage \pcol@@makecol\z@ \else \pcol@@makecol\@maxdepth \fi
1818
                                            \pcol@Logend{\pcol@makeflushedpage(2)}%
1819
1820
1821
                                      \pcol@@hfil \hb@xt@\columnwidth{\box\@outputbox\hss}%
1822
                               \endgroup
                               \verb|\edef|\pcol@0hfil{\noexpand}\pcol@hfil{\pcol@colsepid}||% \property = (a.b.) | (a.b.) | (b.b.) | (
1823
                                \pcol@setcurrcolnf
1824
                             \advance\@tempcntb\@ne}}}
1825
```

\pcol@flushfloats \pcol@iflushfloats

The macro \pcol@flushfloats is invoked from \pcol@output@clear and \pcol@output@end to flush all deferred column-wise floats in each column if any. After letting \@colht = \textheight for float columns, we iterate shipping out a page having float columns while \if@fcolmade = $\exists c \in [0, C) : (\kappa_c(\lambda_d) \neq ())$.

In the loop, we initialize \if@fcolmade = false, and then invoke \pcol@iflushfloats twice or once according to $C_L < C$ or not to mean parallel-paging is in effect or not, respectively. That is, if $C_L < C$ we invoke the macro with $[C_L, C)$ and \pcol@rightpage for the right parallel-page, and do it with $[0, C_L)$ and \@outputbox always. Note that if $C_L = C$, we let \pcol@rightpage = \bot to tell \@outputpage, which we invoke at the end of the loop to ship

out a page or a parallel-page pair, that the parallel-paging is not in effect.

The macro $\colonormal{\colon$

Then we open a \hbox of \textwidth wide and initialize f = ifQtempswa to be \ifQfcolmade. Then for each $c \in [C^0, C^1)$, being c' or C-1-c' for the c'-th iteration determined by \pcolQswapcolumn according to the effectiveness of column-swapping and the parity of \cQpage, we put an inner \hbox of \columnwidth = w_c wide preceded by \pcolQ \text{Ohfil} being \relax at initial or \pcolQhfil\langle c_g otherwise for a column-separating gap and column-separating rule, where $c_g \in \{c, c-1\}$ without or with column-swapping respectively. That is, at first we obtain c's column-context including $\kappa_c(\lambda_d)$ by \pcolQgetcurrcol and pass $\kappa_c(\lambda_d)$ to \Qmakefcolumn to produce a float column in \Quantocolumn context to be put into the inner \hbox. Then we do $f \leftarrow f \lor (\kappa_d(\lambda_d) \neq \emptyset)$ with $\kappa_d(\lambda_d)$ shrunk by \Qmakefcolumn to let f have $\exists c \in [0, C^1) : (\kappa_c(\lambda_d) \neq \emptyset)$ at the end of the loop for c, and then save the column-context into κ_c by \pcolQsetcurrcolnf because we have no footnotes in c.

After the end of the loop, we move f to ∞ for the termination check of the loop in $\pool@flushfloats$.

```
1827 \def\pcol@flushfloats{%
      \global\@colht\textheight
1828
      \@whilesw\if@fcolmade\fi{%
1829
1830
        \global\@fcolmadefalse
        \ifnum\pcol@ncolleft<\pcol@ncol
1831
          \pcol@iflushfloats\pcol@ncolleft\pcol@ncol\pcol@rightpage
1832
1833
1834
          \setbox\pcol@rightpage\box\voidb@x
1835
        \pcol@iflushfloats\z@\pcol@ncolleft\@outputbox
1836
1837
        \@outputpage}}
1838 \def\pcol@iflushfloats#1#2#3{\setbox#3\vbox{%
      \ifpcol@paired\else\ifnum#1=\z@\else \advance\c@page\@ne \fi\fi
1839
      \pcol@buildcolseprule\@colht#1#2\@maxdepth \unvbox\@tempboxa
1840
      \hb@xt@\textwidth{%
1841
1842
        \let\pcol@@hfil\relax
1843
        \if@fcolmade \@tempswatrue \else \@tempswafalse \fi
1844
        \@tempcntb#1\@whilenum\@tempcntb<#2\do{%
1845
          \pcol@swapcolumn\@tempcntb\pcol@currcol#1#2\relax
1846
          \pcol@getcurrcol
1847
          \@makefcolumn\@deferlist
          \pcol@0hfil \hb@xt@\columnwidth{%
1848
            \if@fcolmade \box\@outputbox \else \vbox to\@colht{}\fi \hss}%
1849
          \ifx\@deferlist\@empty\else \@tempswatrue \fi
1850
1851
          \edef\pcol@@hfil{\noexpand\pcol@hfil{\pcol@colsepid}}%
1852
          \pcol@setcurrcolnf
1853
         \advance\@tempcntb\@ne}%
1854
        \if@tempswa \global\@fcolmadetrue \else \global\@fcolmadefalse \fi}}}
1855
```

\pcol@freshpage The macro \pcol@freshpage is invoked from \pcol@output@flush and \pcol@output@clear to start a new page after column flushing. At first, we let $p=p_b=p_t=0$ and $\Pi=\emptyset$

because we know no pages are kept. Then we invoke $\polesize to start a new page with a <math>\polesize to following the invoker is this macro (i.e., not <math>\polesize to following to following the following the following for each column <math>c \in [0, C)$.

First we obtain c's column-context in κ_c by \pcol@getcurrcol but let p=0 and \@colroom = h, which can be modified by c' < c, without referring to $\kappa_c(\beta^p)$ nor $\kappa_c(\beta^r)$ because they are obsolete. We also save \@currbox to \pcol@currboxsave because it may be modified by \pcol@opcol if we make float columns afterward. Then we invoke \pcol@getcurrpage to have the page context of p=0, because it might be modified by a column c' < c by producing float columns. After that and the invocation of \pcol@floatplacement for setting float parameters, we invoke \pcol@startcolumn for c's column-page at p=0, and iterate \pcol@opcol and \pcol@startcolumn while a float column is made by the latter c114. Note that we give the argument 0 to each invocation of \pcol@startcolumn to keep it from inserting deferred page-wise footnotes, which will be taken care of by \pcol@restartcolumn if any. At last in the loop, we restore \@currbox from \pcol@currboxsave, let $\kappa_c(\beta^b)$ be an empty \vbox because the main vertical list is empty, and save the column-context into κ_c by \pcol@setcurrcolnf because of no footnotes obviously, after saving p and \@colroom, which might be modified by the float column production, into $\kappa_c(\beta^p)$ and $\kappa_c(\beta^r)$.

After the loop above, finally we invoke \pcol@restartcolumn to return to the column in which \flushpage or \clearpage was issued.

```
1856 \def\pcol@freshpage{%
                        \global\pcol@page\z@ \global\pcol@toppage\z@ \global\pcol@basepage\z@
1857
                        \global\let\pcol@pages\@empty \global\let\pcol@currpage\@empty
1858
1859
                        \pcol@startpage \pcol@colht\@colht
                        \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
1860
                                \pcol@getcurrcol \pcol@page\z@ \@colroom\pcol@colht
1861
                               \let\pcol@currboxsave\@currbox
1862
1863
                               \pcol@getcurrpage
1864
                                \pcol@floatplacement
1865
                                \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                                \@whilesw\if@fcolmade\fi{\pcol@opcol \pcol@startcolumn\z@}%
1866
                               \let\@currbox\pcol@currboxsave
1867
                                \global\setbox\@currbox\vbox{}%
1868
                                \global\count\@currbox\pcol@page \global\dimen\@currbox\@colroom
1869
                                \pcol@setcurrcolnf
1870
1871
                            \advance\pcol@currcol\@ne}%
1872
                        \pcol@restartcolumn}
1873
```

11.9 Last Page

\pcol@output@end

The macro <page-header> to process the \bigcup request made by \exists we invoke $\$ done by \exists we invoke $\$ done by \exists which \exists indicates, giving it $b = \$ becolocolat in which \exists of the tallest column-page to have the ship-out image of the top page in \o

Next, we define $\mathcal{M} = \pcol@mparbottom@out$ as follows. First, we invoke \pcol@getmparbottom@last giving it $y = V_P' - \ht\ensuremath{\mbox{Qoutputbox}}$ being the negative counterpart of the height of spanning stuff in the last page, to let \mathcal{M} have the occupancy information of the

²¹⁴Each column can have deferred floats on the invocation from \pcol@output@flush.

bottom marginal note in each margin if any, or mpar(y,y) otherwise. Then we transform y-coordinates in $\mathcal M$ from those for columns to those for text area by $\colon problem \{-y\}$ to have the final result. Then to pass $\colon problem post-environment typesetting, we invoke <math>\colon problem proble$

```
1874 %% Special Output Routines: Last Page
1875
1876 \def\pcol@output@end{%
     \pcol@Logstart\pcol@output@end
1877
     \pcol@makeflushedpage\pcol@colht
1878
     \@tempdima\pcol@colht \ifdim\pcol@colht<\z@ \@tempdima\z@ \fi
1879
     \advance\@tempdima-\ht\@outputbox
1880
1881
     \pcol@getmparbottom@last\@tempdima
     \pcol@bias@mpbout{-\@tempdima}
1882
     \def\pcol@do@mpbout@elem\@elt##1##2{\global\@mparbottom##2sp}%
1884
1885
     \pcol@do@mpbout
```

Next we process one of the following cases.

The first case is for \ifpcol@dfloats = true to mean the last page is followed by one or more pages having deferred column-wise floats and thus \pcol@makeflushedpage builds the ship-out image of the last page in full size in \@outputbox unless the page has nothing perfectly. Therefore, we ship the image out by \@outputbox unless it is \bot for perfectly empty case. Then we invoke \pcol@flushfloats to produce and ship out float pages, lettinng \iffcolmade = true to tell the macro that at least we will have one float page. Now we have shipped out everyting in the closing environment and thus we let \iffcol@output = false to tell \output routine to work ordinarily. Then we let \iffcolmswa = f_{sp} = true to remember we will start a new page and thus \@pagedp = δ = D_P = 1000 to mimic TeX's \prevdepth mechanism. Finally we let \@mparbottom = 0 and $\mathcal{M} = \mathcal{M}_0$ because no marginal notes are carried over to post-environment typesetting.

```
1886 \@tempswafalse

1887 \ifpcol@dfloats

1888 \ifvoid\@outputbox\else \@outputpage \fi

1889 \global\@fcolmadetrue \pcol@flushfloats

1890 \global\pcol@outputfalse

1891 \@tempswatrue \@pagedp\@m\p@ \global\@mparbottom\z@

1892 \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
```

Before proceeding to the second and third cases, we let \ightharpoonup we have nothing to ship out.

Then the second case is for $h=-\infty$ without deferred column-wise floats to mean all columns in the last page are empty and the page does not have non-merged page-wise footnotes. In this case, we examine if \pcol@firstprevdepth = \relax to mean we have had at least one new page in paracol environment, i.e., \pcol@startpage have been invoked at least once. If so, we let $f_{sp}=true$, $\delta=1000$, \@mparbottom = 0 and $\mathcal{M}=\mathcal{M}_0$ again and put nothing to the main vertical list so that the post-environment stuff starts from the top of the page. However, we have to take care of the case that $f_{ns}=false$ and thus \@outputbox has spanning stuff. If so, we acquire an \insert from \@freelist by \@next to let it have the spanning stuff, i.e., the contents of \@outputbox^{215}. Then the \insert is added to the head of \@dbldeferlist

²¹⁵It does not have \dbltextfloatsep at its tail because the skip has been removed by \pcol@makeflushedpage.

with the float placement code 10 to force LATEX's float placement mechanism to put it to the page to be started shortly.

On the other hand, $\color=0$ in decimal integer representation. Since we have not started any pages in the environment, and all columns in the last page is empty, we have almost nothing in the environment. Note that the environment can have page-wise floats but they have not yet put into any pages but are kept in $\color=0$ 0 theyer in the pre-environment stuff and postenvironment stuff must be connected naturally and thus we put the pre-environment stuff kept in $\color=0$ 0 the main vertical list by $\color=0$ 1 and keeping $f_{sp} = false^{216}$. In this case, the setting of $\color=0$ 2 marginal notes in pre-environment stuff including paracol environments preceeding it even if any.

```
\else
1893
        \global\pcol@outputfalse
1894
        \ifdim\pcol@colht=-\maxdimen
1895
          \ifx\pcol@firstprevdepth\relax
1896
            \@tempswatrue \@pagedp\@m\p@ \global\@mparbottom\z@
1897
            \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
1898
            \ifpcol@nospan\else
1899
              \pcol@Fb
1900
1901
              \@next\@currbox\@freelist{\global\setbox\@currbox\box\@outputbox}%
1902
                 \pcol@ovf
              \pcol@Fe{output@end(spanning)}%
1903
              \count\@currbox10\relax
1904
              {\let\@elt\relax \xdef\@dbldeferlist{\@elt\@currbox\@dbldeferlist}}%
1905
              \global\setbox\pcol@rightpage\box\voidb@x
1906
1907
          \else \unvbox\@outputbox \@pagedp\pcol@firstprevdepth sp\relax
1908
```

The last case without deferred floats and with some non-empty columns or non-merged pagewise footnotes is most usual. In this case, we may simply put $\column{0}{0}$ because \topskip has already been inserted in column-pages or pre-environment stuff in the box²¹⁷.

However before putting the box back to the main vertical list, we have to take care of the background painting as follows. First we let $\prolength{\mathbb{limble}{l$

²¹⁶The author of course know this situation is very unlikely but he is monomaniac.

²¹⁷If the last page has non-merged page-wise footnotes without any other items, \topskip has not been inserted, but this inconsistency without \topskip is acceptable.

Third and finally, we have to paint the background of non-merged page-wise footnotes because the painting is left by $\pcol@makeflushedpage$ for this macro. Therefore, if $\pcol@fnheight@lpage > 0$ to mean we have footnotes whose total height-plus-depth is in the macro, we paint their background by $\pcol@bg@paintbox \defining \pcol@bg@footnoteheight with the size and temporarily re\defining <math>\pcol@bg@textheight$ to be the height-plus-depth of \qcutyutbox because the foontnotes are at the bottom of the box instead of the page. Note that the order of painting is right first and then left second if we have parallel-pages because we refer the height-plus-depth of \qcutyutbox being put into the main vertical list making the box \qcutyutbox . Also note that if the right parallel-page is non-paired, we temporarily increment \qcutyutbox being put into the main vertical to side margins correctly. Another remark is that we don't modify \qcutyutbox handle infinite extension to side margins correctly. Another remark is that we don't modify \qcutyutbox \qcutyutbo

```
\else
1910
          \global\pcol@havelastpagetrue
1911
          \@tempdima\ht\@outputbox \advance\@tempdima\dp\@outputbox
1912
          \xdef\pcol@bg@preposttop@left{\number\@tempdima sp}%
1913
          \ifnum\pcol@ncolleft<\pcol@ncol
1914
1915
            \global\let\pcol@bg@preposttop@right\pcol@bg@preposttop@left
1916
          \fi
1917
          \def\pcol@bg@textheight{\delt{\ht\@outputbox}\@elt{\dp\@outputbox}}%
          \def\reserved@a{%
1918
            \ifdim\pcol@fnheight@lpage>\z@
1919
              \def\pcol@bg@footnoteheight{\@elt\pcol@fnheight@lpage}%
1920
              \pcol@bg@paintbox{Nn}%
1921
1922
            fi}%
          \ifnum\pcol@ncolleft<\pcol@ncol
1923
            \global\setbox\pcol@rightpage\vbox{%
1924
              \ifpcol@paired\else \advance\c@page\@ne \fi
1925
1926
              \reserved@a \unvbox\pcol@rightpage}%
1927
          \topskip\z@ \vbox{\reserved@a \unvbox\@outputbox}%
1928
1929
        \fi
      \fi
1930
```

Now we have put almost everything in the last page but we may still have page-wise footnotes in $\pi^f(p_t)$ to be merged with those in post-environment stuff. Therefore, we \insert them through \footins as a part of post-environment stuff, and then do that for deferred footnotes in $\Phi = \pcol@topfnotes$ without using \pcol@deferredfootins because we don't need the height capping.

```
1931 \ifvoid\pcol@footins\else
1932 \pcol@Log\pcol@output@end{insert}\pcol@footins
1933 \pcol@Fb
1934 \insert\footins{\unvbox\pcol@footins}\@cons\@freelist\pcol@footins
1935 \pcol@Fe{output@end(pagefn)}%
1936 \fi
1937 \ifvoid\pcol@topfnotes\else \insert\footins{\unvbox\pcol@topfnotes}\fi
```

The following operationss are for clean-up and set-up for the post-environment stuff; for all c, return $\kappa_c(\beta)$ obtained by \pcol@getcurrcol and $\gamma_0^c \neq \bot$ letting it \bot to \@freelist; reestablish the color stack by \pcol@restorecolorstack for column-0²¹⁸ so that the color stack is just Γ and is rewinded at \end{paracol}, and let $\Gamma = \bot$; reload κ_d for $d = \pcol@lastcol being the column in which \end{paracol} occurs to let \everypar = <math>\kappa_d(\varepsilon)$ and to let \if@nobreak

²¹⁸It can be any other column.

and \if@afterindent have the value represented by $\kappa_d(\sigma)$, so that the first paragraph of the post-environment stuff is typeset following them²¹⁹; let \pcol@prevdepth = δ so that it is set to \prevdepth by \pcol@invokeoutput; let \@colht = \@colroom = \textheight to mean the single-column page does not have any floats so far because those produced in or before the environment have already been shipped out, are put to the main vertical list packed in \@outputbox, or are in \@dbldeferlist.

As for deferred page-wise floats produced in the environment, including those once put in the last page but returned to the list by the operation described above, we move them to $\ensuremath{\mbox{\tt Qdeferlist}}$ because they are now column-wise floats. Then we invoke $\ensuremath{\mbox{\tt pcolo}}$ floatplacement to reinitialize float placement parameters. Finally, if $f_{sp} = true$, we invoke $\ensuremath{\mbox{\tt Qstartcolumn}}$ and then repeat invocations of $\ensuremath{\mbox{\tt Qopcol}}$ and $\ensuremath{\mbox{\tt Qstartcolumn}}$ while float pages are produced, after letting $\ensuremath{\mbox{\tt letting}}$ if $\ensuremath{\mbox{\tt pcolo}}$ to make $\ensuremath{\mbox{\tt Qcombinefloats}}$ work as $\ensuremath{\mbox{\tt Letting}}$'s original $\ensuremath{\mbox{\tt letting}}$.

```
\pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
1938
        \pcol@Fb
1939
        \pcol@getcurrcol \@cons\@freelist\@currbox
1940
        \ifvoid\pcol@ccuse{@box}\else
1941
          \@cons\@freelist{\pcol@ccuse{@box}}%
1942
          \pcol@ccxdef{\voidb@x}%
1943
1944
        \pcol@Fe{output@end(col)}%
1945
       \advance\pcol@currcol\@ne}%
1946
1947
      \pcol@currcol\z@ \pcol@restorecolorstack
1948
      \global\setbox\pcol@colorins\box\voidb@x
1949
      \pcol@currcol\pcol@lastcol\relax \pcol@getcurrcol
      \global\pcol@prevdepth\@pagedp
1950
      \global\@colht\textheight
1951
      \global\@colroom\textheight
1952
      \global\let\@deferlist\@dbldeferlist \gdef\@dbldeferlist{}%
1953
      \pcol@floatplacement
1954
      \pcol@lastpagefalse
1955
      \if@tempswa
1956
        \@startcolumn \@whilesw\if@fcolmade\fi{\@opcol\@startcolumn}%
1957
1958
      \pcol@Logend\pcol@output@end
1959
1960 }
1961
```

12 Starting Environment

\pcol@invokeoutput

Before giving the definition of paracol environment and commands used in it, we define the macro $\pool@invokeoutput\langle pen\rangle$ invoked from them to make an \output -request with $\pool@invokeoutput\langle pen\rangle$ invoked from them to make an \output -request with \poolength{pen} in \poolength{pen} invoked from them to make an \output -request with \poolength{pen} is similar to that for the request sequence in \output -request as follows; insert a \poolength{pen} and \poolength{pen} is kept even when we are at the top of a page; and finally restore \poolength{pen} is kept even when we are at the top of a page; and finally restore \poolength{pen}

A difference is that we zero-clear \deadcycles because it can be reach \maxdeadcycles = 100 easily if a page has many synchronizations and many columns. Another and more important

²¹⁹For rare cases that the last item of the closing environment is a sectioning command, but a user has such very unusual usage.

difference is in the save/restore of \prevdepth. First, the value of the register is saved in our own \pcol@prevdepth instead of \@tempdima by a \global assignment so that \output-routine refers to it²²¹. Second, the value restored to \prevdepth may be different from that we just have saved because \output-routine may update \pcol@prevdepth to have, for example, the value saved in $\kappa_c(\delta)$ when we left from c which we are now restarting.

In addition to above, after the invocatoin of \output-routine, we let \linewidth = $w_c - \mu$ so that the register is shrunk from w_c by the total width of left and right margins of the list-like environment surrounding paracol if $\mu = \protect\$ to mean that. Then if so, we set \parshape to let every line of paragraphs in the column c is indented by \Othersian totalleftmargin and has width of \linewidth, as IATEX's \list does. We also let \hsize = w_c because it should have the width of the column even in a list-like environment.

The macro is invoked from \pcol@zparacol (f= start), \pcol@switchcol for \switch column and column-switching environments (f= switch), \pcol@visitallcols for column-scan prior to synchronized column-switching and page flushing (f= switch), \pcol@flushclear for pre-flushing column height check (f= switch), \pcol@com@flushpage for \flushpage (f= flush), \pcol@com@clearpage for \clearpage (f= clear), and \endparacol (f= end).

```
1962 %% Starting Environment
1963
1964 \def\pcol@invokeoutput#1{\deadcycles\z@
      \pcol@Logstart{\pcol@invokeoutput
1965
        {#1:\the\pcol@currcol/\the\pcol@nextcol%
1966
1967
         \ifnum#1=-10011:\ifpcol@sync s\fi \ifpcol@clear c\fi\fi}}%
      \penalty-\@Miv \global\pcol@prevdepth\prevdepth \vbox{}%
      \penalty#1\relax \prevdepth\pcol@prevdepth
1970
      \linewidth\columnwidth \advance\linewidth-\pcol@lrmargin
      \ifdim\pcol@lrmargin>\z@ \parshape\@ne\@totalleftmargin\linewidth \fi
1971
1972
      \hsize\columnwidth
      \pcol@Logend{\pcol@invokeoutput{#1}}}
1973
1974
```

\paracol \pcol@xparacol \pcol@yparacol \pcol@zparacol The API macro $\operatorname{CL}[x][*]{C}[text]$ is invoked by $\operatorname{Degin}[text]$ to start a paracol environment. The macro sipmly examines the existence of the optional argument C_L , whose default value C_L is given by $\operatorname{Degin}[text]$, to decide the number of columns in left parallel-pages. Then if the optional argument is given, $\operatorname{Degin}[text]$ is invoked by $\operatorname{Degin}[text]$ in the optional argument is invoked by $\operatorname{Degin}[text]$ invoked by $\operatorname{Degin}[text]$ in the option

```
1975 \def\paracol{\global\pcol@pairedtrue \@ifnextchar[%]
1976 \pcol@yparacol\pcol@xparacol\}
1977 \def\pcol@xparacol#1{\pcol@zparacol[#1]{#1}}
1978 \def\pcol@yparacol[#1]{%
1979 \@ifstar{\global\pcol@pairedfalse \pcol@zparacol[#1]}%
1980 {\pcol@zparacol[#1]}}
```

In \pcol@zparacol, after making it sure to be in vertical mode by \par, at first we examine if we are neither in a box by \ifinner nor with ordinary two-column typesetting by \if@twocolumn, and complain about inappropriateness unless our expectation is satisfied. Then we let C_L and C have the value given through the corresponding arguments, unless $C_L > C$ to let us make $C_L = C$ silently. Next we examine $C_L < C$, and if not we let

²²¹The assignment is not necessary to be done \globally but we dare to do it to make all assignments to \pcol@prevdepth being \global consistently.

\ifpcol@paired = true regardless the setting in \pcol@yparacol because non-paired type-setting is meaningless without parallel-paging. On the other hand, if non-paired typesetting is specified, we let \ifpcol@swapcolumn = false but not \globally because column-swapping is meaningless in non-paired mode in the environment now starting.

Second, we perform the operations done by \item if \if@newlist = true and \if@inlabel = false to mean the first one in a list-like environment will appear at the very first line of the leftmost column. That is, we invoke \@nbitem if \if@nobreak = true, or add a penalty \@beginparpenalty and a vertical skip \@topsep—\parskip—\itemsep so that the first \item is \@topsep apart from the last line above the environment, and then let \if@newlist = false. The reason why we do these operations here is that, if the paracol environment is enclosed in a list-like environment without anything between two \begin for environments, we have to align all first \items in all columns. That is, if we did not do that, the literally first \item would do that resulting in the column having the \item led by the vertical skip of \@topsep while others should have ordinary inter-\item skips. Therefore, we perform the operations on behalf of all first \items in all columns to have the skip of \@topsep above the paracol environment we are opening. Note that if \begin{paracol} paracol} immediately follows a \begin for a trivlist-like environment, \if@inlabel = true because the first \item was given in the opening macro and thus the operations shown above has already been performed.

```
1981 \def\pcol@zparacol[#1]#2{\par
      \ifinner \@parmoderr \fi
1983
      \if@twocolumn \PackageError{paracol}{%
        Environment paracol cannot work with ordinary two-column
1984
1985
        typesetting.}\@ehb\fi
      \global\pcol@ncolleft#1\relax \global\pcol@ncol#2\relax
1986
      \ifnum\pcol@ncolleft>\pcol@ncol \global\pcol@ncolleft\pcol@ncol \fi
1987
      \ifnum\pcol@ncolleft<\pcol@ncol\else \global\pcol@pairedtrue \fi
1988
      \ifpcol@paired\else \pcol@swapcolumnfalse \fi
1989
      \if@newlist \if@inlabel\else
1990
1991
        \if@nobreak \@nbitem
        \else
1993
          \addpenalty\@beginparpenalty
1994
          \addvspace\@topsep
          \addvspace{-\parskip}\addvspace{-\itemsep}%
1995
        \fi
1996
        \global\@newlistfalse
1997
1998
      \fi\fi
```

Next we scan θ^l applying \pcol@thectrelt to each element $\theta^l \in \theta^l$ to let \pcol@thectr@ $\theta^l = \theta^l$ so that the former has the default local representation of θ^l . The macro \pcol@thectrelt also lets \the $\theta^l = \text{pcol@thectr@}\theta^l \cdot 0$ if the local representation for θ^l and c = 0 has been defined by \definethecounter. This is necessary because in the first visit to the leftmost column 0 we will neither invoke \pcol@switchcol nor thus scan θ^l with \pcol@setctrelt which defines local representations, unless a spanning text is specified with \begin \paracol\.

Next we give the initial value of $val_c(\theta^l)$ for each column c and local counter $\theta^l \in \Theta^l$ by the followings enclosed in a group. First we scan Θ_0 applying \pcol@loadctrelt to each

 $\theta^l \in \Theta_0' = \{\theta \mid \langle \theta, val_0(\theta) \rangle \in \Theta_0\}$ to have the value $val_0(\theta^l)$ in \polectrollect

```
1999 \global\let\pcol@counters\cl@@ckpt
2000 \let\@elt\pcol@remctrelt \pcol@gcounters
2001 \let\@elt\pcol@thectrelt \pcol@counters
2002 \begingroup
2003 \let\@elt\pcol@loadctrelt \csname pcol@counters0\endcsname
2004 \let\@elt\pcol@cmpctrelt \global\let\@gtempa\@empty \pcol@counters
2005 \pcol@synccounter\@gtempa
2006 \endgroup
```

Fourth, we set up a few LATEX's typesetting parameters which should have appropriate values in the environment. We let $\ifotonum = true$ so that float* environments work for page-wise floats and LaTeX's \addmarginpar determine the margin for marginal notes by $\ifotonum ber = 1$ instead of C so that its (almost surely) sole user \addmarginpar . We also let the title with \twocolumn which cannot be in the environment.

Then we invoke $\pcol@setcolumnwidth\langle C^0\rangle\langle C^1\rangle\langle r\rangle\langle s\rangle$ once or twice with $(C^0,C^1,r,s)=(0,C_L)$, $\pcol@columnratioleft$, $\pcol@colwidthspecleft$) always for left parallel-page, and with (C_L,C) , $\pcol@columnratioright$, $\pcol@colwidthspecright$) for right one if $C_L< C$ to define column widths $w_c=\pcol@columnwidth\cdot c$ and that of column-separating gaps $g_c=\pcol@columnsep\cdot c$ for all $c\in[0,C)=[0,C_L)\cup[C_L,C)$.

Then we initialize other variables as follows; $\mu = \cline{1mm} = \textwidth - \linewidth so that, if <math>\mu > 0$, \linewidth for c has $w_c - \mu$ reflecting the paragraph shape of the list-like environment surrounding paracol environment; \pcol@topskip = \topskip for the second and succeeding pages; \pcol@textfloatsep = ∞ to mean we don't have any synchronization points so far; \ifpcol@lastpage = false because the starting page is not the last so far; and \pcol@firstprevdepth = \prevdepth in decimal integer form for the extreme empty case.

We also make the macro \@combinefloats \let-equal to our own \pcol@combinefloats throughout the environment, after saving its original definition into \pcol@combinefloats for processing \output request sneaked from outsied of environment, so that our customization is in effect for any invocations including those from LaTeX's own macros. Similarly, \@addmarginpar is made \let-equal to our own \pcol@addmarginpar while its original definition is saved into \pcol@addmarginpar but in this case we need the original for the implementation of our own. On the other hand, \end@dblfloat is simply replaced with our own \pcol@end@dblfloat being what LaTeX had had until 2014 as discussed in item-(1) of §1.8.

```
2007 \global\@twocolumntrue \col@number\@ne
2008 \pcol@setcolumnwidth\z@\pcol@colleft
2009 \pcol@columnratioleft\pcol@colwidthspecleft
```

²²²Undefined in fact.

```
2010
     \ifnum\pcol@ncolleft<\pcol@ncol
       \pcol@setcolumnwidth\pcol@ncolleft\pcol@ncol
2011
         \pcol@columnratioright\pcol@colwidthspecright
2012
2013
2014
     \pcol@lrmargin\textwidth \advance\pcol@lrmargin-\linewidth
     \global\pcol@topskip\topskip
     \global\pcol@textfloatsep\maxdimen
     \pcol@lastpagefalse \xdef\pcol@firstprevdepth{\number\prevdepth}%
2017
2018
     \let\pcol@combinefloats\@combinefloats \let\@combinefloats\pcol@combinefloats
     \let\pcol@addmarginpar\@addmarginpar \let\@addmarginpar\pcol@addmarginpar
2019
     2020
```

Fifth, we save the original definition of \set@color into \pcol@set@color, and then examine if \set@color \neq \relax meaning some coloring package is loaded. If any coloring packages are not loaded, we make macros for background painting, namely \pcol@bg@paintpage, \pcol@bg@paintcolumns and \pcol@bg@paintbox, \let-equal to \relax for the first two and to \@gobble for the last so that they do nothing without coloring package.

If the coloring is enabled, on the other hand, we redefine LATFX's \set@color so that it works as \pcol@set@color@push with color stack. We also prepare the text colring mechanism to let \forall ifpcol@inner = true in every \forall vbox in the paracol environment as follows. First, we let for our own pupose, we do the followings; (1) \globally assign a token \pcol@dummytoken, which should never occurs, to \pcol@everyvbox; (2) save \everyvbox into \pcol@everyvbox locally; (3) let \everyvbox have a \the-reference to \pcol@everyvbox and \pcol@innerture to let $\forall ifpcol@inner = true;$ and then (4) make $\forall vipcol@inner = true;$ and then (4) make $\forall vipcol@inner = true;$ By the last operation (4), any \everyvbox appearing in the paracol environment is replaced with \pcol@everyvbox to keep the real \everyvbox from modified nullifying our own operation \pcol@innertrue. On the other hand, since both \everyvbox and \pcol@everyvbox are registers to hold tokens and thus any operations applicable to \everyvbox are also applicable to \pcol@everyvbox, any updates on \everyvbox and explicit references to it are simulated by \pcol@everyvbox. Then the initial tokens given to \pcol@everyvbox by the saving operation (2) or tokens given inside the environment are correctly processed whenever a \vbox is opened, toghether with \pcol@innertrue to fulfill our own purpose, because the real \everyvbox is let have a \the-reference to \pcol@everyvbox by (3). We also reserve the invocation of \pcol@ restoreeveryvbox by \aftergroup so that the macro is invoked just after \end{paracol} to examine if any \global assignments to \everyvbox has been made in the environment. The funny \global assignment (1) is done for this examination so that we detect global assignments done in the environment having been closed because they should have changed the global value of \pcol@everyvbox to something different from \pcol@dummytoken.

Then we continue the case having some coloring package to make background painting macros \pcol@bg@paintpage, \pcol@bg@paintbox and \pcol@bg@paintcolumns activated by making them \let-equal to thier @@ counterparts namely \pcol@bg@@paintpage, \pcol@bg@@paintbox and \pcol@bg@@paintcolumns which implement background painting.

Finally we empty the shadow color stack $\tilde{\Gamma} = \pcol@colorstack@shadow$ to give it initial value regardless of the availability of coloring package.

```
2021 \global\let\pcol@set@color\set@color
2022 \ifx\set@color\relax
2023 \let\pcol@bg@paintpage\relax \let\pcol@bg@paintbox\@gobble
2024 \let\pcol@bg@paintcolumns\relax
2025 \else
2026 \let\set@color\pcol@set@color@push
2027 \pcol@innerfalse
```

```
2028
        \global\pcol@everyvbox{\pcol@dummytoken}%
        \pcol@everyvbox\everyvbox
2029
        \everyvbox{\the\pcol@everyvbox \pcol@innertrue}
2030
        \let\everyvbox\pcol@everyvbox
2031
        \aftergroup\pcol@restoreeveryvbox
2032
2033
        \let\pcol@bg@paintpage\pcol@bg@@paintpage
        \let\pcol@bg@paintbox\pcol@bg@@paintbox
        \let\pcol@bg@paintcolumns\pcol@bg@@paintcolumns
2035
2036
      \gdef\pcol@colorstack@shadow{}%
2037
```

The sixth settings are for (mainly column-wise) footnotes. We initialize two footnote-related count registers letting $b_f = \pcol@footnotebase$ have $\c@footnote$ and zero-clearing $n_f = \pcol@footnotes$. Then we redefine LaTeX's API macros \footnote, \footnotemark and \footnotetext to let them be our own \pcol@footnote, \pcol@footnotemark and \pcol@footnotetext so that they have starred-versions. The other API macro to be redefined, if pagewise footnote typesetting is in effect, is \footnoterule which lets \columnwidth = \textwidth before invoking its original version saved in \pcol@footnoterule so that it acts as in single-columned typesetting rateher than multi-columned. Then we redefine LaTeX's internal macro \@footnotetext letting it be our own \pcol@fntext for encapsulating a footnote in a \vbox and for deferred \insertion with page-wise footnote typesetting.

```
2038 \pcol@footnotebase\c@footnote \global\pcol@nfootnotes\z@
2039 \let\footnote\pcol@footnote
2040 \let\footnotemark\pcol@footnotemark
2041 \let\footnotetext\pcol@footnotetext
2042 \ifpcol@scfnote
2043 \def\footnoterule{{\columnwidth\textwidth \pcol@footnoterule}}%
2044 \fi
2045 \let\@footnotetext\pcol@fntext
```

Seventh, we let \marginpar, \@mn@@marginnote and \@xympar be our own versions \pcol@marginpar, \pcol@marginnote and \pcol@xympar respectively for the emulation of \marginnote, saving the original version of the first and third into \pcol@@marginpar and \pcol@@xympar. Then we inactivate API macros \twosided and \footnotelayout together with their backward-compatible macros \swapcolumninevenpages, \noswapcolumnineven pages, \multicolumnfootnotes, \singlecolumnfootnotes and \mergedfootnotes, so that they commonly invoke \pcol@ignore because their inherent operations turning corresponding switches are harmful in paracol environment. Note that the inactivation of \twosided is done by redefinition of \pcol@twosided because we need optional argument processing by \twosided even when it is inactivated.

```
2046
      \let\pcol@marginpar\marginpar \let\marginpar\pcol@marginpar
2047
      \let\@mn@@marginnote\pcol@marginnote
2048
      \let\pcol@cxympar\@xympar \let\@xympar\pcol@xympar
      \def\pcol@twosided[#1]{\pcol@ignore\twosided}%
      \def\swapcolumninevenpages{\pcol@ignore\swapcolumninevenpages}%
2050
      \def\noswapcolumninevenpages{\pcol@ignore\noswapcolumninevenpages}%
2051
2052
      \def\footnotelayout#1{\pcol@ignore\footnotelayout}%
2053
      \def\multicolumnfootnotes{\pcol@ignore\multicolumnfootnotes}%
2054
      \def\singlecolumnfootnotes{\pcol@ignore\singlecolumnfootnotes}%
      \def\mergedfootnotes{\pcol@ignore\mergedfootnotes}%
```

Eigth, we scan the list \pcol@localcommands of $\langle com \rangle$ being the name of commands, e.g., switchcolumn, available only in the environment or customized for the environment, applying \pcol@defcomelt to each $\langle com \rangle$ to let $\langle com \rangle = \text{pcol@com@} \cdot \langle com \rangle$ the latter of which is the

real implementation of the former. Note that the list does not have all environment-local API commands but we omit \column(*) for column(*) environments because their implementations \pcol@com@column(*) are modified after the first invocation. Therefore, we \define \column(*) to have \pcol@com@column(*) in their bodies²²³. We also give the first \definitions of \pcol@com@column(*) to let them do nothing but re\define themselves by \pcol@defcolumn unless \pcol@com@column* is given an optional spanning text argument which is directly processed by \pcol@sptext, if they appear as the first column-switching command/environment after \begin{paracol}. Then we re\define \paracol itself so that it will complain of illegal nesting by \PackageError.

```
\let\@elt\pcol@defcomelt \pcol@localcommands
2056
2057
      \def\column{\pcol@com@column}%
      \@namedef{column*}{\@nameuse{pcol@com@column*}}%
2058
      \global\let\pcol@com@column\pcol@defcolumn
      \global\@namedef{pcol@com@column*}{\pcol@defcolumn
        \@ifnextchar[%]
2061
2062
         \pcol@sptext\relax}%
      \def\paracol##1{\PackageError{paracol}{%
2063
        Environment paracol cannot be nested.}\@eha}%
2064
```

Ninth, we let \output have our output routine \pcol@output as its sole token, and then make \output request with \penalty = \pcol@op@start by \pcol@invokeoutput to invoke \pcol@output@start for initialization, after letting \@elt = \relax to make it sure that any lists can be manipulated without unexpected application of a macro to their elements.

```
2065 \output{\pcol@output}%
2066 \let\@elt\relax
2067 \pcol@invokeoutput\pcol@op@start
```

Tenth and finally, we let \pcol@nextcol = 0 in case \begin{paracol} has the optional argument for spanning text, and invoke \pcol@sptext if it has. Otherwise, we invoke \pcol@colpream·0 being the column preamble of the first column 0, which will be invoked by \pcol@switchcol if spanning text is given.

```
2068 \pcol@nextcol\z@
2069 \@difnextchar[%]
2070 \pcol@sptext{\@nameuse{pcol@colpream0}}}
```

\pcol@paracol The macro \pcol@paracol has the definition of \paracol, which is redefined in the macro itself, so that the only referrer \pcol@icolumncolor examines if it appears in paracol, i.e., \pcol@paracol ≠ \paracol.

```
2071 \let\pcol@paracol\paracol
2072
```

\thecolumn The API macro \thecolumn gives the value of \pcol@currcol to users to let them know which column they are working in so that, for example, they do some column-dependent opreations.

2073 \def\thecolumn{\number\pcol@currcol}

\pcol@ignore The macro \pcol@ignore $\langle macro \rangle$ is to complain that the $\langle macro \rangle$ being one of the followings appears in paracol environment.

```
\twosided, \swapcolumninevenpages, \noswapcolumninevenpages,
\footnotelayout, \multicolumnfootnotes, \singlecolumnfootnotes,
\mergedfootnotes
```

²²³We can do this for other commands instead of adhearing to \let to eliminate the execption, but the author loves to use \let as much as possible.

That is, these macros, except for \twosided, are re\defined in \pcol@zparacol to invoke this macro with the argument identifying themselves, which is shown in the warning message given by \PackageWarning. As for \twosided, the target of the re\definition is \pcol@twosided so that its optional argument is captured before the complaint.

```
2075 \def\pcol@ignore#1{\PackageWarning{paracol}{The command \string#1 is not
     effective in paracol environment and thus ignored}}
2077
```

\pcol@localcommands

The macro \pcol@localcommands is the list of the names of the following environment-local API commands (or *local commands* in short) and is solely referred to by \pcol@zparacol.

```
\switchcolumn
                \endcolumn(*)
                                     \nthcolumn(*)
                                                        \endnthcolumn(*)
\leftcolumn(*)
                \endleftcolumn(*)
                                    \rightcolumn(*)
                                                        \endrightcolumn(*)
\flushpage
                                     \cleardoublepage
                \clearpage
\synccounter
                \syncallcounters
```

Note that we omit \column(*) from the list as discussed in the description of \pcol@zparacol.

```
2078 \def\pcol@localcommands{%
      \@elt{switchcolumn}%
      \@elt{endcolumn}\@elt{endcolumn*}%
2080
2081
      \@elt{nthcolumn}\@elt{endnthcolumn}\@elt{nthcolumn*}\@elt{endnthcolumn*}
      \@elt{leftcolumn}\@elt{endleftcolumn}\@elt{leftcolumn*}\@elt{endleftcolumn*}}
2082
      \@elt{rightcolumn}\@elt{endrightcolumn}%
        \@elt{rightcolumn*}\@elt{endrightcolumn*}%
2084
2085
      \Oelt{flushpage}\Oelt{clearpage}\Oelt{cleardoublepage}%
2086
      \Qelt{synccounter}\Qelt{syncallcounters}}
```

\pcol@defcomelt

The macro \pcol@defcomelt is invoked solely from \pcol@zparacol to be applied to each element $\langle com \rangle$ in \pcol@localcommands. Two lengthy \lets with \expandafters are for doing $\left(\cot \left(\cos \right) \right) = \left(\cos \left(\cos \right) \right)$ to bind the environment-local API command $\left(\cos \right)$ and its implementation $\prolecom @\cdot (com)$.

```
2087 \def\pcol@defcomelt#1{%
      \expandafter\let\expandafter\reserved@a\csname pcol@com@#1\endcsname
2088
      \expandafter\let\csname #1\endcsname\reserved@a}
2089
2090
```

\pcol@end@dblfloat

\@dbldeferlist As discussed in §1.8, 2015 version of LATFX no longer uses \@dbldeferlist but the macro itself is still kept in LATEX. However it will be removed in future to make the first \@cons with it resulting in an error. Therefore, here we have its top level definition with empty duplicatedly in case of its future elimination. The macro \end@dblfloat, on the other hand, is replaced with a new definition in the new LATEX of course, and thus we define \pcol@end@dblfloat here to keep its old definition and to replace the new one in paracol environment as discussed in item-(1) of §1.8.

```
2091 \gdef\@dbldeferlist{}
2092 \def\pcol@end@dblfloat{%
      \if@twocolumn
        \@endfloatbox
2094
2095
        \ifnum\@floatpenalty <\z@
          \@largefloatcheck
2096
          \@cons\@dbldeferlist\@currbox
2097
        \fi
2098
        \ifnum \@floatpenalty =-\@Mii \@Esphack\fi
2099
2100
```

```
\end@float
2101
       \fi
2102
2103 }
```

13 Column Width Setting

\columnratio \pcol@icolumnratio \pcol@columnratioleft \pcol@columnratioright The API macro \columnratio $\{r_0^l, r_1^l, \cdots, r_{k^l-1}^l\}$ $[r_0^r, r_1^r, \cdots, r_{k^r-1}^r]$ defines the column width fraction r_c^l for column c in left parallel-pages and optionally r_c^r for those in right parallelpages. This macro and its callee \pcol@icolumnratio just \globaly \define macros \pcol@ columnratioleft and \pcol@columnratioright whose bodies have the first and second arguments respectively, or commonly have the first if the second optional one is not given, so that they are given to \pcol@setcolwidth@r as its third argument through \pcol@setcolumnwidth invoked in \pcol@zparacol. Both of \pcol@columnratioleft and \pcol@columnratioright are initialized to be empty so that all columns have same width and are separated by \columnsep as default. Note that \pcol@columnratioleft can be made \let-equial to \relax by the related API macro \setcolumnwidth so that \pcol@setcolumnwidth knows which of specifications given by two API macros is effective and chooses \pcol@setcolwidth@r or \pcol@setcolwidth@s.

```
2104 %% Column Width Setting
2105
2106 \def\columnratio#1{\global\let\pcol@colwidthspecleft\relax
      \gdef\pcol@columnratioleft{#1}%
      \@ifnextchar[%]
        \pcol@icolumnratio{\gdef\pcol@columnratioright{#1}}}
2109
2110 \def\pcol@icolumnratio[#1]{\gdef\pcol@columnratioright{#1}}
2111 \columnratio{}\relax
```

\setcolumnwidth \pcol@isetcolumnwidth \pcol@colwidthspecleft \pcol@colwidthspecright

The API macro \setcolumnwidth $\{s_0^l, s_1^l, \cdots, s_{k^l-1}^l\}$ [$s_0^r, s_1^r, \cdots, s_{k^r-1}^r$] defines the column width specification s_c^l for column c in left parallel-pages and optionally s_c^r for those in right parallel-pages, where each specification s_c^x has the form of $[w_c][/[g_c]]$ for width and gap specifier w_c and g_c . After \lefting \pcol@columnratioleft = \relax to disable the setting by \columnratio and to enable that done by this macro, the macro and its callee \pcol@isetcolumnwidth just \globaly \define macros \pcol@colwidthspecleft and \pcol@colwidthspecright whose bodies have the first and second arguments respectively, or commonly have the first if the second optional one is not given, so that they are given to \pcol@setcolwidth@s as its fourth argument through \pcol@setcolumnwidth invoked in \pcol@zparacol. Both of \pcol@colwidthspecleft and \pcol@colwidthspecright are initially undefined because the default specification is given by \columnratio{}.

```
2113 \def\setcolumnwidth#1{\global\let\pcol@columnratioleft\relax
      \gdef\pcol@colwidthspecleft{#1}%
2114
2115
      \@ifnextchar[%]
        \pcol@isetcolumnwidth{\gdef\pcol@colwidthspecright{#1}}}
2117 \def\pcol@isetcolumnwidth[#1]{\gdef\pcol@colwidthspecright{#1}}
```

zparacol but can be twice, with;

```
(C^0, C^1, \langle ratio \rangle, \langle spec \rangle) = (0, C_L, \texttt{\pcol@columnratioleft}, \texttt{\pcol@colwidthspecleft})
```

always and with;

```
(C^0, C^1, \langle ratio \rangle, \langle spec \rangle) = (C_L, C, \pcol@columnratioright, \pcol@colwidthspecright)
```

if $C_L < C$ for parallel-paging. The macro simply invokes \color{o} if \color{o} colored setcolumn because \color{o} invokes \color{o} or \color{o} or \color{o} otherwise, with all arguments given by \color{o} pcolored.

```
2119 \def\pcol@setcolumnwidth{%
2120 \ifx\pcol@columnratioleft\relax \let\reserved@a\pcol@setcolwidth@s
2121 \else \let\reserved@a\pcol@setcolwidth@r
2122 \fi
2123 \reserved@a\
2124
```

\pcol@setcolwidth@r

The macro \pcol@setcolwidth@r $\langle C^0 \rangle \langle C^1 \rangle \langle ratio \rangle \langle spec \rangle$ is invoked solely from \pcol@zparacol through \pcol@setcolumnwidth once or twice with the arguments described in the explanation of the latter macro. The macro calculates $w_c = \text{\pcol@columnwidth} \cdot c$ for all $c \in [C^0, C^1)$, from the fractions $r_0, r_1, \ldots, r_{k-1}$ given through the third argument $\langle ratio \rangle$, which was given to \columnratio and then kept in \pcol@columnratioleft or \pcol@columnratioright. The macro also lets $g_c = \text{\pcol@columnsep} \cdot c = \text{\columnsep}$ for all $c \in [C^0, C^1)$.

First, we calculate $W = \text{textwidth} - (C^1 - C^0 - 1) \times \text{columnsep}$ being the sum of w_c for all $c \in [C^0, C^1)$. Then we let $w_c = r_d W$ and $g_c = \text{columnsep}$ for all $c \in [C^0, k')$ where $k' = \min(k, C^1 - 1)$, in the \Qfor loop scanning r_d for all $d = c - C^0 \in [0, k)$. Finally, we let $w_c = (W - \sum_{d=C^0}^{k'-1} w_d)/(C^1 - C^0 - k')$ and $g_c = \text{columnsep}$ for all $c \in [k', C^1)$. Note that \pcolQcolumnwidth c and \pcolQcolumnsep c are macros having the integer representations of w_c and g_c with the unit sp.

```
2125 \def\pcol@setcolwidth@r#1#2#3#4{%
       \@tempcntb#2\advance\@tempcntb-#1\advance\@tempcntb\m@ne
2127
       \@tempdima-\columnsep \multiply\@tempdima\@tempcntb
2128
       \advance\@tempdima\textwidth \@tempdimb\@tempdima
       \@tempcnta#1\relax\@tempcntb#2\advance\@tempcntb\m@ne
2129
       \ensuremath{\texttt{Qfor}\ensuremath{\texttt{reserved@a:=\#3}do\{\%\ensuremath{\texttt{%}}\ensuremath{\texttt{%}}}
2130
2131
         \ifnum\@tempcnta<\@tempcntb
           \@tempdimc\reserved@a\@tempdima
2132
           \expandafter\xdef\csname pcol@columnwidth\number\@tempcnta\endcsname{%
2133
2134
              \number\@tempdimc sp}%
2135
           \global\@namedef{pcol@columnsep\number\@tempcnta}{\columnsep}%
2136
           \advance\@tempdimb-\@tempdimc
2137
           \advance\@tempcnta\@ne
2138
         fi}%
2139
       \@tempcntb#2\advance\@tempcntb-\@tempcnta
2140
       \divide\@tempdimb\@tempcntb
       \@whilenum\@tempcnta<#2\do{%
2141
         \expandafter\xdef\csname pcol@columnwidth\number\@tempcnta\endcsname{%
2142
2143
           \number\@tempdimb sp}%
2144
         \global\@namedef{pcol@columnsep\number\@tempcnta}{\columnsep}%
         \advance\@tempcnta\@ne}%
2146 }
2147
```

\pcol@setcolwidth@s
\pcol@setcw@c
\pcol@setcw@s
\pcol@setcw@filunit

The macro \pcol@setcolwidth@s $\langle C^0 \rangle \langle C^1 \rangle \langle ratio \rangle \langle spec \rangle$ is invoked solely from \pcol@zparacol through \pcol@setcolumnwidth once or twice with the arguments described in the explanation of the latter macro. The macro calculates $w_c = \text{\pcol@columnwidth} \cdot c$ for all $c \in [C^0, C^1)$ and $g_c = \text{\pcol@columnsep} \cdot c$ for all $c \in [C^0, C^1-1)$, from the column/gap specifications $s_0, s_1, \ldots, s_{k-1}$ given through the fourth argument $\langle spec \rangle$, which was given to \setcolumnwidth and then kept in \pcol@colwidthspecleft or \pcol@colwidthspecright.

Each specification s_d for w_c and g_c where $c = C^0 + d$ has the form $[w'_d][/[g'_d]]$ to specify the natural width w^n_d and g^n_d and inifite stretch factor w^f_d and g^f_d of column/gap sepcfication as follows;

$$w_d^n = \begin{cases} 0 & w_d' = \emptyset \\ 0 & w_d' = f \text{ fill} \\ natural(w_d') & \text{otherwise} \end{cases} \qquad w_d^f = \begin{cases} 1 & w_d' = \emptyset \\ f & w_d' = f \text{ fill} \\ stretch(w_d') & \text{otherwise} \end{cases}$$

$$g_d^n = \begin{cases} \text{columnsep} & g_d' = \emptyset \\ 0 & g_d' = f \text{ fill} \\ natural(g_d') & \text{otherwise} \end{cases} \qquad g_d^f = \begin{cases} 0 & g_d' = \emptyset \\ f & g_d' = f \text{ fill} \\ stretch(g_d') & \text{otherwise} \end{cases}$$

where natural(x) is the natural width of the skip x and stretch(x) is the infinite stretch factor of x. Note that any finite stretch factors or any shirnk factors do not affect them, and infinite stretch units fil, fill and filll are not distinguished. From factors above, we determine w_c and g_c as follows;

$$\begin{split} W &= \sum_{d=0}^{m-2} (w_d^n + g_d^n) + w_{m-1}^n \\ F &= \sum_{d=0}^{m-2} (w_d^f + g_d^f) + w_{m-1}^f \\ x_c &= \begin{cases} (W_T/W) x_{c-C^0}^n & W \geq W_T \ \lor \ F \leq 0 \\ x_{c-C^0}^n + (x_{c-C^0}^f/F)(W_T - W) & W < W_T \ \land \ F > 0 \end{cases} \quad (x \in w, g) \end{split}$$

where $W_T = \text{textwidth}$ and $m = C^1 - C^0$.

To perform the assignments above, the macro at first invoke \pcol@setcw@scan $\langle C^0 \rangle \langle C^1 \rangle \{spec\}$ letting \pcol@setcw@c = \pcol@setcw@s = \pcol@setcw@accumwd and \pcol@setcw@filunit = 1pt to scan s_d for all $d \in [0,m)$ and to accumulate $W+g^n_{m-1}$ and $F+g^f_{m-1}$ in \dimen@ and \dimen@ii and then subtract g^n_{m-1} and g^f_{m-1} from them to have W and F. Note that F is represented by a dimension with the unit of pt by the definition of \pcol@setcw@filunit. Then we invoke \pcol@setcw@calcfactors to calculate $(W_T/W) = \pcol@setcw@scale$ and $(W_T-W)/F = \pcol@setcw@scale$ Finally we scan s_d again but in this case we let \pcol@setcw@c = \pcol@setcw@set{width}, \pcol@setcw@s = \pcol@setcw@set{sep} and \pcol@setcw@filunit = \@tempdimb = $(W_T-W)/F$ to let w_c and g_c have the values shown above.

2148 \def\pcol@setcolwidth@s#1#2#3#4{\begingroup

- 2149 \dimen@\z@ \dimen@ii\z@ \def\pcol@setcw@filunit{\@ne\p@}%
- 2150 \let\pcol@setcw@c\pcol@setcw@accumwd \let\pcol@setcw@s\pcol@setcw@accumwd
- 2151 \pcol@setcw@scan#1#2{#4}%
- 2152 \advance\dimen@-\@tempdima \advance\dimen@ii-\@tempdimb
- 2153 \pcol@setcw@calcfactors
- 2154 \def\pcol@setcw@c{\pcol@setcw@set{width}}%
- ${\tt 2155} \qquad {\tt def\pcol@setcw@s{\pcol@setcw@set{sep}}}\%$

```
2156 \let\pcol@setcw@filunit\dimen@ii
2157 \pcol@setcw@scan#1#2{#4}%
2158 \endgroup}
```

\pcol@setcw@scan

The macro \pcol@setcw@scan $\langle C^0 \rangle \langle C^1 \rangle \{spec\}$ is to scan first $m = C^1 - C^0$ elements in $\langle spec \rangle = s_0, s_1, \ldots$ being the column/gap specifications given to \setcolumnwidth. At first we add ',' as many as m to the tail of $\langle spec \rangle$ to make it sure the resulting $\langle spec \rangle$ has m or more elements. Then we scan all elements in the extended $\langle spec \rangle$ by a \@for loop having many \expandafter but equivalent to;

```
\ensuremath{\texttt{Qfor}\ensuremath{\texttt{reserved@a:=}s_0,s_1,...}} do\{body\}
```

In the body above, we invoke \pcol@setcw@getspec s_i /\@nil to parse s_i to have w_i^n , w_i^f to be processed by \pcol@setcw@c and g_i^n and g_i^f by \pcol@setcw@s, for all $i \in [0, m)$.

```
2159 \def\pcol@setcw@scan#1#2#3{\def\reserved@a{#3}%
      \@tempcnta#1\relax \@whilenum\@tempcnta<#2\do{
        \edef\reserved@a{\reserved@a,}\advance\@tempcnta\@ne}%
2161
2162
      \@tempcnta#1\relax
      \expandafter\0for\expandafter\reserved0a\expandafter:\expandafter=\reserved0a
2163
        \do{%
2164
          \ifnum\@tempcnta<#2\relax
2165
            \expandafter\pcol@setcw@getspec\reserved@a//\@nil
2166
2167
2168
          \advance\@tempcnta\@ne}}
```

\pcol@setcw@getspec@i \pcol@setcw@getspec@i \pcol@setcw@fill The macro \pcol@setcw@getspec $\langle w'_d \rangle / \langle g'_d \rangle / \langle garbage \rangle$ \@nil is used solely in \pcol@setcw@scan to parse a column/gap specification $s_d = [w'_d] [/[g'_d]]$, to extract factors w^n_d , w^f_d , g^n_d and g^f_d , and to process width factors by \pcol@setcw@c and gap factors by \pcol@setcw@s. Since the macro is invoked with arguments in the form of $s_d / / \text{Qnil}$, if s_d has '/' in it w'_d and g'_d should have everything preceding and following the '/' respectively while $\langle garbage \rangle$ should have the redundant '/'. Otherwise, i.e., if s_d does not have '/', $w'_d = s_d$ and $g'_d = \emptyset$ while $\langle garbage \rangle = \emptyset^{224}$. Therefore, we invoke \pcol@setcw@getspec@i $\langle default \rangle \{x'_d\}$ twice with $\langle default \rangle, x'_d \rangle = (\text{fill}, w'_d)$ for a column and $\langle default \rangle, x'_d \rangle = (\text{columnsep}, g'_d)$ for a gap, and \pcol@setcw@c and \pcol@setcw@s after each invocation respectively.

In this macro, at first we scan all tokens in x'_d by \P to remove all space tokens in it \P . Then if R'_d after the space removal has nothing, we let $R'_d = \langle default \rangle$. Next we examine if $R'_d = f$ in a trickey way by temporarily \P thing \P and $R'_d = f$ and making an assignment " \P the space remains and \P that is, if $R'_d = f$ thill, \P the space will have R'_d which must be a proper skip and \P remains unchanged from \P about the space R'_d which must be a proper skip and \P remains unchanged from \P and \P the space R'_d to let \P to let \P the space R'_d again R'_d . Otherwise, we invoke \P columns to let \P to let \P the space R'_d to R'_d to let \P the space R'_d the space R'_d to R'_d to let \P the space R'_d the space R'_d the space R'_d to R'_d to R'_d the space R'_d the space R'_d to R'_d the space R'_d the space R'_d the space R'_d to R'_d the space R'_d the space R'_d the space R'_d to R'_d the space R'_d the space R'_d the space R'_d to R'_d the space R'_d to R'_d the space R'_d the space R'_d the space R'_d the space R'_d to R'_d to R'_d the space R'_d

Now \Quad tempskipa has x_d^n as its natural component and may have some infinite strectch component x_d^f specified explicitly or with \fill. Therefore, we assign \Quad tempskipa to \Quad tempskipa

 $^{^{225}}$ A proper skip specification and " $f\$ fill" is always proper without space tokens in them.

 $^{^{226}}$ Because the first assignment is done in a group.

make it sure it has both strech and shrink components²²⁷ keeping infinite stretch factor if any, invoke $\colored{pcol@extract@fil}$ giving it $\tolered{the-expansion}$ of $\colored{qtempskipa}$ as the argument to let $\colored{qtempdimb} = x_d^f \times \colored{qtempdimb}$.

```
2169 \def\pcol@setcw@getspec#1/#2/#3\@nil{%
      \pcol@setcw@getspec@i\fill{#1}\pcol@setcw@c
      \pcol@setcw@getspec@i\columnsep{#2}\pcol@setcw@s}
2172 \def\pcol@setcw@getspec@i#1#2{%
      \def\reserved@a{}%
2173
      \@tfor\reserved@b:=#2\do{\edef\reserved@a{\reserved@a\reserved@b}}
2174
      \ifx\reserved@a\@empty \let\reserved@a#1\fi
2175
      \let\@gtempa\relax
2176
      {\def\fill{1\p0\gdef\0gtempa{}}\0tempskipa\reserved0a}%
2177
2178
      \ifx\@gtempa\relax \@tempskipa\reserved@a\relax
      \else \expandafter\pcol@setcw@fill\reserved@a
2181
      \@tempdima\@tempskipa
      \advance\@tempskipa0\p@\@plus\@m\p@\@minus\@m\p@\relax
2182
      \expandafter\pcol@extract@fil\the\@tempskipa\@nil}
2183
2184 \def\pcol@setcw@fill#1\fill{\def\reserved@b{#1}%
      \ifx\reserved@b\@empty \let\reserved@b\@ne \fi
      \@tempskipa0\p@\@plus\reserved@b fil\relax}
2186
2187
```

\pcol@setcw@accumwd

The macro \pcol@setcw@accumwd is made \let-equal to \pcol@setcw@c and \pcol@setcw@s commonly and thus invoked from \pcol@setcw@getspec with setting \@tempdima = x_d^n and \@tempdimb = $x_d^f \times 1$ pt, where $x \in \{w,g\}$. The macro simply add them to \dimen@ and \dimen@ii repsectively to accumurate x_d^n and x_d^f in them.

2188 \def\pcol@setcw@accumwd{\advance\dimen@\@tempdima \advance\dimen@ii\@tempdimb}

\pcol@setcw@set

The macro \pcol@setcw@set{wors} is made the body of \pcol@setcw@c with $\langle wors \rangle =$ width and of \pcol@setcw@s with $\langle wors \rangle =$ sep and thus invoked from \pcol@setcw@getspec with setting \@tempdima = x_d^n and

$$(\texttt{\pcol@setcw@scale}, \texttt{\qcmpdimb}) \in \{(\emptyset, \, (x_d^f/F)(W_T-W)), \, (W_T/W, \, 0)\}$$

Therefore, we calculate $x_c = \color= \color$

2189 \def\pcol@setcw@set#1{%

 ${\tt 2190 \quad \tt \classification} \end{\tt advance} {\tt \classification} a {\tt \classification}$

 ${\tt 2191 } \verb| expandafter\xdef\csname pcol@column#1\number\@tempcnta\endcsname{\%}} \\$

2192 \number\@tempdima sp}}

2193

\pcol@setcw@calcfactors
 \pcol@setcw@calcf
 \pcol@setcw@scale

The macro \pcol@setcw@calcfactors is used solely in \pcol@setcolwidth@s to calculate $\phi_s = \pcol@setcw@scale$ and $\phi_f = \dimen@ii$ as follows

$$(\phi_s, \phi_f) = \begin{cases} (W_T/W, \ 0) & W \ge W_T \ \lor \ F \le 0 \\ (1, \ (W_T - W)/F) & W < W_T \ \land \ F > 0 \end{cases}$$

where $W = \dim Q$, $F \times 1$ pt = $\dim Q$ in and $W_T = \det Q$ and $\varphi_s = 1$ is represented by empty body of $\gcd G$. First we deal with the special and trivial case of

 $^{^{227}}$ Almost sure because they could be -1000 pt, but we ignore the possibility.

 $W=W_T$ to let $\phi_s=1$ and $\phi_f=0$ so as to avoid arithmetic error in the calculation of W_T/W . If $W\neq W_T$ on the other hand, we calculate W_T/W by \pcol@setcw@calcf $\langle W_T\rangle\langle W\rangle\langle\phi_s\rangle$ to have a provisional result. Then if $W< W_T$ and F>0, we let $\phi_s=1$ and invoke \pcol@setcw@calcf again giving it (W_T-W) and $F\times 1$ pt but throw away the result $(W_T-W)/(F\times 1$ pt) because \@tempdimb should have $(W_T-W)/F$ which is then set into $\phi_f=$ \dimen@ii. Otherwise, we keep the provisional result of ϕ_s as the final one and let $\phi_f=$ \dimen@ii = 0.

The macro \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ calculates $z \approx x/y$ and let \@tempdimb = $Z = z \times 1$ pt as follows. First we find the following three parameters.

```
\begin{split} k_1 &= \min\{k \,|\, k \geq 0, \ x \cdot 2^k \geq 2^{13} \, \mathtt{pt}\} \\ k_2 &= \max\{k \,|\, y \bmod 2^k = 0\} \\ k_3 &= \min\{k \,|\, k \geq 0, \ \lceil y/2^{k_2 + k} \rceil \leq 2^{15}\} \end{split}
```

With these parameters, we calculate $z' = \lfloor (x \cdot 2^{k_1})/\lceil y/2^{k_2+k_3} \rceil \rfloor$ to have a good approximation of $(x/y) \cdot 2^k$ where $k = k_1 + k_2 + k_3$ without arithmetic overflow. Then if $z'/2^k \geq 2^{14}$ or in other words Z is larger than \maxdimen, we complain that by \PackageError and, in case a user dare to continue the typesetting process, we let $Z = 10000\,\mathrm{pt}$. Otherwise, we calculate $Z = (z'/2^k) \cdot 2^{16} = z' \cdot 2^{16-k}$ to have it in \@tempdimb by $Z = z' \times 2^{16-k}$ if k < 16, or by $Z = z'/2^{k-16}$ otherwise. Finally we invoke \pcol@extract@pt giving it \the-representation of Z to have z.

Note that it is assured $z \leq x/y$ regardless of successfulness of the calculation and thus the scaling $\phi_s x_d^n$ and strething $x_d^n + \phi_f x_d^f$ cannot exceed their exact value to make it also sure that $\sum_{c=C^0}^{C^1-2} (w_c + g_c) + w_{C^1-1} \leq W_T$ and thus the series of columns and column-separating gaps should not cause overfull when a page is shipped out with \hfil added to each column-separating gap for underfull avoidance.

```
2194 \def\pcol@setcw@calcfactors{%
      \ifdim\dimen@=\textwidth \def\pcol@setcw@scale{}\dimen@ii\z@
2196
2197
        \pcol@setcw@calcf\textwidth\dimen@\pcol@setcw@scale
2198
        \ifdim\dimen@<\textwidth \ifdim\dimen@ii>\z@
2199
          \def\pcol@setcw@scale{}%
          \@tempdimc\textwidth \advance\@tempdimc-\dimen@
2200
          \pcol@setcw@calcf\@tempdimc\dimen@ii\reserved@a \dimen@ii\@tempdimb
2201
        \else \dimen@ii\z@ \fi
2202
2203
        \else \dimen@ii\z@ \fi
2204
2205 \def\pcol@setcw@calcf#1#2#3{%
      \@tempdimb#1\@tempdima#2\@tempcnta\z@
      \ifdim\@tempdima=\z@ \@tempdima1sp\relax\fi
2207
2208
      2209
        \multiply\@tempdimb\tw@ \advance\@tempcnta\@ne}%
      \@tempdimc\@tempdima
2210
      \@whiledim\@tempdima=\@tempdimc\do{%
2211
        \divide\@tempdimc\tw@ \multiply\@tempdimc\tw@
2212
2213
        \ifdim\@tempdima=\@tempdimc
2214
          \divide\@tempdima\tw@ \divide\@tempdimc\tw@ \advance\@tempcnta\@ne
2215
2216
      \advance\@tempdima-1sp\relax
2217
      \@whilenum\@tempdima>32768\do{\divide\@tempdima\tw@ \advance\@tempcnta\@ne}%
2218
      \advance\@tempdima1sp\relax
2219
      \divide\@tempdimb\@tempdima \@tempdimc\@tempdimb \@tempcntb\@tempcnta
```

```
\@whilenum\@tempcntb>\z@\do{\divide\@tempdimc\tw@ \advance\@tempcntb\m@ne}
2220
      \ifnum\@tempdimc>16383\relax
2221
        \PackageError{%
2222
         Scaling/filling factor for column/gap width is too large.}\@eha
2223
2224
        \@tempdimb\@M\p@
        \@tempcntb\sixt@@n \advance\@tempcntb-\@tempcnta
2226
        \ifnum\@tempcntb<\z@
2227
          \@whilenum\@tempcntb<\z@\do{\divide\@tempdimb\tw@ \advance\@tempcntb\@ne}%
2228
2229
        \else
2230
          \c \
            \multiply\@tempdimb\tw@ \advance\@tempcntb\m@ne}%
2231
2232
        \fi
      \fi
2233
      \expandafter\pcol@extract@pt\the\@tempdimb#3}
2234
```

\pcol@defkw
\pcol@kw@pt
\pcol@kw@plus
\pcol@kw@minus
\pcol@kw@fil

The macro \pcol@defkw1.0 $\langle pt \rangle_{\square} \langle plus \rangle_{\square}1.0 \langle fil \rangle_{\square} \langle minus \rangle_{\square}1.0 \langle garbage \rangle$ \@nil is used just once at the top level to \define \pcol@kw@pt, \pcol@kw@plus, \pcol@kw@minus and \pcol@kw@fil letting them have $\langle pt \rangle = \text{pt}$, $\langle plus \rangle = \text{plus}$, $\langle minus \rangle = \text{minus}$ and $\langle fil \rangle = \text{fil}$ in their body respectively but with \catcode = 12 (other) which is used in \the-representation of glues. For the definition, we invoke \pcol@defkw giving it \the-representation of \@tempskipa letting it have 1 pt plus 1 fil minus 1 fil having all keywards we need to have^228. The macro \pcol@kw@pt is used in \pcol@extract@fil@ii $\langle unit \rangle$ \@nil to examine if $\langle unit \rangle = \text{pt}$, and in \pcol@def@extract@pt to \define \pcol@extract@pt having pt in its argument specification. The macros \pcol@kw@plus and \pcol@kw@minus are used only in \pcol@def@extract@fil having plus and minus, and \pcol@extract@fil@iii having fil, in their argument specifications respectively.

```
2236 \@tempskipa 1\p@\@plus1fil\@minus1fil\relax
2237 \def\pcol@defkw1.0#1 #2 1.0#3 #4 1.0#5\@nil{%
2238 \def\pcol@kw@pt{#1}\def\pcol@kw@plus{#2}\def\pcol@kw@fil{#3}%
2239 \def\pcol@kw@minus{#4}}
2240 \expandafter\pcol@defkw\the\@tempskipa\@nil
```

\pcol@def@extract@fil
 \pcol@extract@fil@i
 \pcol@extract@fil@ii
\pcol@extract@fil@iii
 \pcol@extract@fil@iii

The macro $\pcol@extract@fil\langle garbge_1\rangle \plus \subseteq \langle s\rangle \mbox{ minus} \langle garbage_2\rangle \mbox{ onil is used solely in $$\pcol@setcw@getspec@i to extract the infinite stretch factor f in the stretch component s of a column/gap specification x'_d and to let $$\end{to} \processeteq \mbox{ on } \processeteq \mbox{ on$

\def\pcol@extract@fil#1\plus\#2\minus#3\@nil{\pcol@extract@fil@i#2\@nil}

just once at the top level. Then since s should have the form $\langle n \rangle.\langle m \rangle\langle unit \rangle$ where n and m are decimal digit sequences and $\langle unit \rangle \in \{\text{pt,fil,fill,fill}\}$, we examine if $\langle unit \rangle = \text{pt}$ or not by a trickey way in $\coint(m) \cdot (m \cdot unit) \cdot (m \cdot u$

 $^{^{228}}$ We can do what \pcol@defkw does by temporarily giving \catcode = 12 to the characters for the keywords of course, but this method is much easier.

otherwise invoke $\pcol@extract@fil@iii\langle f\rangle fil\langle garbage\rangle \ensuremath{\mbox{Qnil}}\ giving it s because it should$ have a postfix being fil, fill or fill, to have \emptyset tempdimb = $f \cdot u$ finally. Note that since \pcol@extract@fil@iii also has the keyword fil in its argument specification, we \define it using \pcol@def@extract@fil@iii, whose body is equivalent to

```
\def\pcol@extract@fil@iii#1fil#2\@nil{%
    \@tempdimb\pcol@setcw@filunit\relax \@tempdimb#1\@tempdimb}
```

just once at the top level too. 2242 \edef\pcol@def@extract@fil{% \def\noexpand\pcol@extract@fil $\label{localization} $$\#1\simeq \pcol@kw@plus\simeq \#2\simeq \pcol@kw@minus\#3\neq \noexpand\enint{%} $$$ 2244 \noexpand\pcol@extract@fil@i##2\noexpand\@nil}} 2246 \pcol@def@extract@fil 2247 \def\pcol@extract@fil@i#1.#2\@nil{\def\reserved@a{#1.#2}% \afterassignment\pcol@extract@fil@ii\count@#2\@nil} 2249 \def\pcol@extract@fil@ii#1\@nil{\def\reserved@b{#1}% \ifx\reserved@b\pcol@kw@pt \@tempdimb\z@ \else \expandafter\pcol@extract@fil@iii\reserved@a\@nil 2251 2252 fi2253 \edef\pcol@def@extract@fil@iii{% 2254 \@tempdimb\noexpand\pcol@setcw@filunit\relax \@tempdimb##1\@tempdimb}} 2255 $2256 \pcol@def@extract@fil@iii$

\pcol@extract@pt

 $\protect\$ The macro $\protect\$ is solely used in $\protect\$ to extract ffrom a dimension in the form of fpt and to let the macro $\langle scale \rangle$ have f. Since this macro has the keyword pt in its argument specification, we \define it using \pcol@def@extract@pt, whose body is equivalent to

```
\def\pcol@extract@pt#1pt#2{\def#2{#1}}
```

```
just once at the top level again.
2258 \edef\pcol@def@extract@pt{%
     \def\noexpand\pcol@extract@pt##1\pcol@kw@pt##2{\def##2{##1}}}
2260 \pcol@def@extract@pt
2261
```

Counter Operations

\globalcounter \pcol@globalcounter@s \pcol@globalcounter \pcol@gcounters The API macro \globalcounter{ctr}, implemented by \pcol@globalcounter and also used in $\protect\$ and thus adds it to $\Theta^g = \pcolegeounters$, which has page at initial. Note that we examines if $\langle ctr \rangle \in \Theta^g$ prior to the addition to avoid the duplication in Θ^g . Also note that initial definition of \pcol@gcounters is done by \gdef just for consistent \global assignments to it. On the other hand \globalcounter*, implemented by \pcol@globalcounter@s, makes all counters kept in \clockpt global by letting \pcol@gcounters have the list. Switching these two functionality is done by \globalcounter examining if it is followed by a * by \@ifstar.

```
2262 %% Counter Operations
2264 \def\globalcounter{\@ifstar\pcol@globalcounter@s\pcol@globalcounter}
```

```
2265 \ensuremath{\mbox{\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{}\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox{$\mbox
2266 \def\pcol@globalcounter#1{{%
                                          \@tempswafalse \def\reserved@a{#1}%
2267
                                          \def\@elt##1{\def\reserved@b{##1}%
2268
2269
                                                         \ifx\reserved@a\reserved@b \@tempswatrue \fi}%
                                          \pcol@gcounters
                                          \if@tempswa\else \@cons\pcol@gcounters{{#1}}\fi}}
 2272 \gdef\pcol@gcounters{\@elt{page}}
```

\localcounter The API macro \localcounter{ctr}, also used in \pcol@fnlayout@c to localize the counter footnote, declares that $\langle ctr \rangle$ is a local counter, and thus removes it from Θ^g by \pcol@ removecounter if $\langle ctr \rangle \neq page$.

```
2273 \def\localcounter#1{%
      \expandafter\ifx\csname c@#1\endcsname\c@page\else
        \pcol@removecounter\pcol@gcounters{#1}%
2275
2276
      \fi}
```

\pcol@remctrelt \pcol@removecounter \pcol@iremctrelt

The macro $\protect\operatorname{pcol}\protect\operatorname{gr}\protect\operatorname{gr}\protect\operatorname{pcol}\protect\operatorname{gr}\protect\operatorname{pcol}\protect\operatorname{gr}$ global counter $\theta^g \in \Theta^g$ to remove it from $\Theta = \pcol@counters$ in which we have Θ^l finally. The macro also moves $\class{cle}\theta^g = \zeta(\theta^g)$ to $\class{pcolected}\theta^g$ to keep the list of the descendant local counters of θ^g in it, and then re\defines \close \close \pcol@stepcounter{ θ^g } so that it is invoked on $\mathsf{stepcounter}\{\theta^g\}$ to let $val_c(\theta^l) = 0$ for all $c \in [0,C)$ and $\theta^l \in \zeta(\theta^g)$, if $\theta^g \neq \text{page}$. These operations are performed by a lengthy sequence with many occurrences of \expandafter, \csname and \endcsname but the sequence is equivalent to the following.

```
\verb|\label{eq:closed}| \textbf{let} \\ \textbf{cl0} \cdot \theta^g \\ \textbf{cl0} \cdot \theta^g \\ \textbf{cl0} \cdot \theta^g
\ \c0.\theta^g\c0page\else\ \def\cl0.\theta^g\pcol0stepcounter\{\theta^g\}\fi
```

As for the removal of θ^g from Θ , we invoke \pcol@removecounter(Θ'){ θ } giving it $\Theta' = \Theta$ and $\theta = \theta^g$. This macro, also invoked from \localcounter{ θ^l } with $\Theta' = \Theta^g$ and $\theta = \theta^l$, does $\Theta'' \leftarrow \Theta', \ \Theta' = \emptyset$, and then apply \pcol@iremctrelt $\langle \Theta' \rangle$ to each $\theta' \in \Theta''$ to let $\Theta' \leftarrow \Theta' \cup \{\theta'\}$ by \@cons if $\theta' \neq \theta$.

```
2277 \def\pcol@remctrelt#1{%
      \expandafter\let\expandafter\reserved@a\csname cl@#1\endcsname
2278
      \expandafter\let\csname pcol@cl@#1\endcsname\reserved@a
2279
      \expandafter\ifx\csname c@#1\endcsname\c@page\else
2280
2281
        \@namedef{cl@#1}{\pcol@stepcounter{#1}}%
2282
      \pcol@removecounter\pcol@counters{#1}}
2284 \def\pcol@removecounter#1#2{%
      \def\reserved@a{#2}\let\reserved@b#1\relax \global\let#1\@empty
2286
      {\def\@elt{\pcol@iremctrelt#1}\reserved@b}}
2287 \def\pcol@iremctrelt#1#2{%
      \def\reserved@b{#2}%
2288
2289
      \ifx\reserved@a\reserved@b\else \@cons#1{{#2}}\fi}
```

2290

\definethecounter The API macro \definethecounter $\langle \theta^l \rangle \langle c \rangle \langle rep \rangle$ define the local representation $\langle rep \rangle$ for a local counter θ^l in a column c. It \defines \pcol@thectr@ $\theta^l \cdot c$ to have $\langle rep \rangle$ in its body.

2291 \def\definethecounter#1#2#3{\@namedef{pcol@thectr@#1#2}{#3}}

\pcol@thectrelt The macro \pcol@thectrelt $\langle \theta^l \rangle$ is invoked solely in \pcol@zparacol and is applied to each $\theta^l \in \Theta^l$ to define its local representation of default and that of the leftmost column 0. It per-

forms a lengthy sequence with many occurrences of \expandafter, \csname and \endcsname but the sequence is equivalent to the followings.

```
\label{eq:left} $$ \left( \theta^l - \theta^l \right) = \theta^l . $$
\ifx\pcol@thectr@\theta^l.0\relax\else \let\the\theta^l=\pcol@thectr@\theta^l.0 \fi
```

```
2292 \def\pcol@thectrelt#1{%
      \expandafter\let\expandafter\reserved@a\csname the#1\endcsname
      \expandafter\let\csname pcol@thectr@#1\endcsname\reserved@a
2294
      \expandafter\let\expandafter\reserved@a\csname pcol@thectr@#10\endcsname
2295
      \ifx\reserved@a\relax\else
2296
2297
        \expandafter\let\csname the#1\endcsname\reserved@a
2298
```

\pcol@loadctrelt \pcol@storecounters \pcol@storectrelt The macro \pcol@loadctrelt $\langle \theta^l \rangle \langle val_c(\theta^l) \rangle$ is invoked from \pcol@zparacol and \pcol@ synccounter and is applied to each element $\langle \theta^l, val_c(\theta^l) \rangle \in \Theta_c$ for a column c to define a macro \pcol@ctr@ $\theta^l = v(\theta^l)$ having $val_c(\theta^l)$ in its body for a temporary use. This macro or its redefined version is then referred to by $\pcol@cmpctrelt(\theta^l)$ or $\pcol@storectrelt(\theta^l)$. The latter is invoked from \pcol@storecounters via \pcol@sscounters to add $\langle \theta^l, v(\theta^l) \rangle$ to \Qgtempa by \Qcons to rebuild Θ_c for a column c in \Qgtempa.

The macro \pcol@storecounters is invoked solely from \pcol@synccounter $\langle \theta \rangle$ to update a local counter θ with $val(\theta)$ for counter synchronization. That is, \pcol@storecounters is used to add $\langle \theta^l, v(\theta^l) \rangle$ to \Ogtempa for all $\theta^l \in \Theta^l$ by \pcolOsscounters giving it \pcolO storectrelt as its argument, where $v(\theta^l)$ is modified if $\theta^l = \theta$ or unmodified otherwise after it is defined by \pcol@loadctrelt.

```
2300 \def\pcol@loadctrelt#1#2{\@namedef{pcol@ctr@#1}{#2}}
2301 \def\pcol@storecounters{\pcol@sscounters\pcol@storectrelt}
2302 \def\pcol@storectrelt#1{\@cons\@gtempa{{#1}{\@nameuse{pcol@ctr@#1}}}}
```

\pcol@savectrelt

\pcol@savecounters The macro \pcol@savecounters is invoked from \pcol@com@syncallcounters, \pcol@ stepcounter and \pcol@switchcol to let Θ_c for a column c have the list of $\langle \theta^l \rangle$ val $_c(\theta^l)$ where $val_c(\theta^l)$ is the value of $\backslash c@\theta^l$ to be saved in the list. It does this operation invoking \pcol@sscounters giving it \pcol@savectrelt as its argument.

> The macro \pcol@savectrelt $\langle \theta^l \rangle$ adds $\langle \theta^l, val_c(\theta^l) \rangle$ to \@gtempa by \@cons to rebuild Θ_c for a column c in $\backslash \mathbb{Q}$ tempa.

```
2303 \def\pcol@savecounters{\pcol@sscounters\pcol@savectrelt}
2304 \end{20} and \end{20} an
```

\pcol@sscounters

The macro \pcol@sscounters $\langle elt \rangle$ is invoked from \pcol@storecounters with $\langle elt \rangle$ = \pcol@storectrelt or \pcol@savecounters with $\langle elt
angle =$ \pcol@savectrelt to build $\Theta_c =$ \pcol@counters $\cdot c$ for a column c. To do that, it lets \@gtempa = () and then apply $\langle elt \rangle$ to all $\theta^l \in \Theta^l = \text{pcol@counters}$ to have updated Θ_c in \@gtempa. Then finally, \@gtempa is moved into Θ_c by \xdef^{229} .

```
2305 \def\pcol@sscounters#1{\begingroup
      \global\let\@gtempa\@empty
      \let\@elt#1\relax \pcol@counters
2307
2308
      \let\@elt\relax
      \expandafter\xdef\csname pcol@counters\number\pcol@currcol\endcsname{%
2309
2310
        \@gtempa}%
```

 $^{^{229}\}mathrm{It}$ can be done by \global\let more efficiently but it is lengthy due to two \expandafter.

```
2311 \endgroup}
2312
```

\pcol@cmpctrelt

The macro $\polential \polential \polential$

```
2313 \def\pcol@cmpctrelt#1{\@tempswafalse \@tempcnta\@nameuse{c@#1}%  
2314 \expandafter\ifx\csname pcol@ctr@#1\endcsname\relax \@tempswatrue  
2315 \else\ifnum\@nameuse{pcol@ctr@#1}=\@tempcnta\else \@tempswatrue  
2316 \fi\fi  
2317 \if@tempswa \@cons\@gtempa{{#1}}\fi}  
2318
```

\synccounter \pcol@com@synccounter

The macro \pcol@com@synccounter $\langle\theta\rangle$, being the implementation of the environment-local API macro \synccounter, lets $val_c(\theta) = val(\theta)$ for all $c \in [0, C)$. That is, the value of the counter θ is broadcasted to all columns for the counter synchronization of θ . This broadcast is done by \pcol@synccounter with an argument \Qelt{\theta} so that it works only on θ .

2319 \def\pcol@com@synccounter#1{\pcol@synccounter{\@elt{#1}}}

\pcol@synccounter \pcol@syncctrelt

The macro \pcol@synccounter\(lst\) is invoked from \pcol@zparacol with $\langle lst\rangle = \text{Qgtempa}$ and from \pcol@com@synccounter\(\langle tr)\) with $\langle lst\rangle = \text{Qelt}\{ctr\}$, to let $val_c(\theta) = val(\theta)$ for all $c \in [0,C)$ and all θ in $\langle lst\rangle$. To do that, at first we move $\langle lst\rangle$ into \reserved@a in order to make \Qgtempa free so that it can be used in \pcol@storecounters. Next, for each $c \in [0,C)$, we let $v(\theta^l) = val_c(\theta^l)$ by applying \pcol@loadctrelt to all $\langle \theta^l, val_c(\theta^l) \rangle \in \Theta_c$, then scan $\langle lst\rangle$ applying \pcol@syncctrelt\(\phi\rangle\) for each θ in $\langle lst\rangle$ to let $v(\theta) = val(\theta)$, and finally store all $v(\theta^l)$ back to Θ_c by \pcol@storecounters, where $v(\theta)$ is \pcol@ctr@ θ .

```
2320 \def\pcol@synccounter#1{{%}
2321 \let\@elt\relax \edef\reserved@a{#1}%
2322 \pcol@currcol\z@ \@whilenum\pcol@currcol\\pcol@ncol\do{%}
2323 \let\@elt\pcol@loadctrelt \@nameuse{pcol@counters\number\pcol@currcol}%
2324 \let\@elt\pcol@syncctrelt \reserved@a
2325 \pcol@storecounters
2326 \advance\pcol@currcol\@ne}}
2327 \def\pcol@syncctrelt#1{%}
2328 \expandafter\edef\csname pcol@ctr@#1\endcsname{\number\@nameuse{c@#1}}}
```

\syncallcounters \pcol@com@syncallcounters

The macro \pcol@com@syncallcounters, being the implementation of the environment-local API macro \syncallcounters, makes all local counters in all columns have the value in the current column. That is, for each $c \in [0, C)$, we invoke \pcol@savecounters to let $val_c(\theta^l) = val(\theta^l)$ for all $\theta^l \in \Theta^l$.

```
2330 \def\pcol@com@syncallcounters{{\mathscr{k}}}
2331 \pcol@currcol\z@ \@whilenum\pcol@currcol\\pcol@ncol\do{\mathscr{k}}
2332 \pcol@savecounters \advance\pcol@currcol\@ne}}
2333
```

\pcol@setctrelt

The macro $\c olumn c$ and is applied to each $\c olumn c$ and $\c olumn c$ and is applied to each $\c olumn c$ and $\c olu$

```
\else \let\the\cdot \theta^l=\pcol@thectr@\cdot \theta^l \cdot c
2334 \def\pcol@setctrelt#1#2{%
2335
      \global\csname c@#1\endcsname#2\relax
      \expandafter\ifx\csname pcol@thectr@#1\number\pcol@currcol\endcsname\relax
2336
       \expandafter\let\expandafter\reserved@a\csname pcol@thectr@#1\endcsname
2337
2338
2339
        \expandafter\let\expandafter\reserved@a
          \csname pcol@thectr@#1\number\pcol@currcol\endcsname
2340
     \fi
2341
     \expandafter\let\csname the#1\endcsname\reserved@a}
2342
2343
```

\pcol@stepcounter
 \pcol@stpldelt
 \pcol@stpclelt

The macro \pcol@stepcounter $\langle \theta^g \rangle$ is invoked from \stepcounter $\langle \theta^g \rangle$ for a global counter θ^g because \close \close is modified by \pcol@remctrelt so as to invoke this macro to zero-clear local counters $\theta \in \zeta(\theta^g)$. To do that, we do the followings in a group for each $c \in [0,C)$. First we apply \pcol@stpldelt $\langle \theta^l \rangle \langle val_c(\theta^l) \rangle$ to each $\langle \theta^l, val_c(\theta^l) \rangle \in \Theta_c$ to let $val(\theta^l) = val_c(\theta^l)$ locally. Then we apply \pcol@stpclelt $\langle \theta \rangle$ to each $\theta \in \zeta(\theta^g)$ to let $val(\theta) = 0$. Finally, we invoke \pcol@savecounters to let $val_c(\theta^l) = val(\theta^l)$ for all $\theta^l \in \Theta^l$ to reflect the zero-clear of $\theta \in \zeta(\theta^g)$.

After the operations above, we apply \P to each $\theta \in \zeta(\theta^g)$ for \S for \S clearing.

```
2344 \def\pcol@stepcounter#1{\begingroup
      \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
2346
        \let\@elt\pcol@stpldelt \@nameuse{pcol@counters\number\pcol@currcol}%
        \let\@elt\pcol@stpclelt \@nameuse{pcol@cl@#1}%
2347
2348
        \pcol@savecounters
       \advance\pcol@currcol\@ne}%
2349
2350
      \endgroup
      \let\@elt\@stpelt \@nameuse{pcol@cl@#1}}
2351
2352 \def\pcol@stpldelt#1#2{\csname c@#1\endcsname#2\relax}
2353 \def\pcol@stpclelt#1{\csname c@#1\endcsname\z@}
2354
```

15 Column-Switching Commands and Environments

\pcol@par

Before giving the definition of column-switching commands and environments, we define a commonly used macro \pcol@par, which do \par if necessary, i.e., we are not in vertical mode. The reason why we don't simply do \par is that it may have some definition different from \@@ par and thus an incautious repetition of \par may cause undesirable results. This macro is used in \pcol@com@switchcolumn, \pcol@sptext, \pcol@com@endcolumn, \pcol@flushclear, and \endparacol.

\switchcolumn \pcol@com@switchcolumn \pcol@switchcolumn \pcol@iswitchcolumn The macro $\protect\operatorname{\sc Npcol@com@switchcolumn}[d]$, being the implementation of the environment-local API macro $\sc Nswitchcolumn$, switches to the column d if provided through its optional argument, or to $d = (c+1) \mod C$ otherwise where c is the ordinal of the current column. After making

it sure to be in vertical mode by $\col@par$, it invokes $\col@defcolumn$ to give $\column(*)$ their \cdefinitions for occurrences not as the very first column-switching command or environment of the current paracol environment. Then, after calculating $d = (c+1) \mod C$, this macro simply invokes $\ccol@switchcol[d]$ with or without the calculated d depending on the existence of the optional argument delimitor '['.

The macro $\prolemnt{\cite{Construction} Description} description of the execution by $$\operatorname{\cite{Construction} Description} description of the execution by $$\operatorname{\cite{Construction} Description} description of the execution by $$\operatorname{\cite{Construction} Description} description of the execution of t$

The macro $\protect{pcol@switchcolumn[\langle text\rangle]}$ invokes $\protect{pcol@switchcolumn[\langle text\rangle]}$ if the optional argument is provided, or $\protect{pcol@switchcol}$ otherwise, after letting $\protect{letting \protect}$ for explicit synchronization.

```
2359 \def\pcol@com@switchcolumn{\pcol@par
      \pcol@defcolumn
2360
2361
      \@tempcnta\pcol@currcol \advance\@tempcnta\@ne
2362
      \ifnum\@tempcnta<\pcol@ncol\else \@tempcnta\z@ \fi
2363
      \@ifnextchar[%]
        \pcol@switchcolumn{\pcol@switchcolumn[\@tempcnta]}}
2364
2365 \def\pcol@switchcolumn[#1]{%
      \pcol@nextcol#1\relax
2366
      \@tempswafalse
2367
2368
      \ifnum#1<\z@ \@tempswatrue \fi
      \ifnum#1<\pcol@ncol\else \@tempswatrue \fi
2370
      \if@tempswa
        \PackageError{paracol}{%
2371
2372
          Column number \number#1 must be less than \number\pcol@ncol}\@eha
2373
        \pcol@nextcol\z@
      \fi
2374
      \@ifstar\pcol@iswitchcolumn\pcol@switchcol}
2375
2376 \def\pcol@iswitchcolumn{%
      \global\pcol@synctrue
2377
2378
      \@ifnextchar[%]
        \pcol@sptext\pcol@switchcol}
2379
2380
```

\pcol@sptext

Next, we let \ifpcol@sptextstart = false and \ifpcol@sptext = true to indicate the main vertical list contains only the spanning text and it is to be captured by \output routine. Then the $\langle text \rangle$ is put in a group in which we let \columnwidth = \hsize = \textwidth and \linewidth = \textwidth - μ with \parshape to indent lines by \@totalleftmargin if $\mu > 0$, to let spanning text span across all columns reflecting the indentation in the list-like environments surrounding paracol if any. We also let \col@number = 1 to ensure again that \maketitle produces a title without \twocolumn if it is in the spanning text.

Then, after invoking \pcol@par to ensure to be in vertical mode, we \globalize \@svsechd and \@svsec which may be defined in a lower-level sectioning command such as \paragraph in

the spanning text so that they are properly expanded in \everypar inserted at the beginning of the first paragraph of the column to which we switch shortly, even when the sectioning command is used inappropriately in the spanning text. We also \globalize \everypar by a sequence with three \expandafter so that \pcol@output@switch for the synchronized column-switching we make shortly broadcasts it to other columns. Finally after closing the group, we let \pcol@nextcol = d and \pcol@sync = true to set another synchronization point below the spanning text and to make the captured text combined with pre-spanning-text stuff, and then invoke \pcol@switchcol to switch the coloumn d.

```
2381 \long\def\pcol@sptext[#1]{%
      \@tempcnta\pcol@nextcol
2382
      \global\pcol@synctrue \pcol@nextcol\z@
2383
      \global\pcol@sptextstarttrue
2384
2385
      \pcol@switchcol
      \global\pcol@sptextstartfalse \global\pcol@sptexttrue
2386
      \begingroup
2387
        \columnwidth\textwidth \hsize\columnwidth
2388
        \linewidth\columnwidth \advance\linewidth-\pcol@lrmargin
2389
        \ifdim\pcol@lrmargin>\z@ \parshape\@ne\@totalleftmargin\linewidth \fi
2390
        \col@number\@ne #1\pcol@par
2391
        \global\let\@svsechd\@svsechd \global\let\@svsec\@svsec
2392
2393
        \expandafter\global\expandafter\everypar\expandafter{\the\everypar}%
2394
      \pcol@nextcol\@tempcnta \global\pcol@synctrue \pcol@switchcol}
2395
```

\pcol@switchcol

The macro \pcol@switchcol is invoked from \pcol@switchcolumn, \pcol@iswitchcolumn, \pcol@isw

Next, if $\ightharpoonup 1$ Next, if $\ightharpoonup 2$ vertex, we do the followings. At first we let $V_E = \proleonup 2$ vspace have the natrual component of \pcol@ensurevspace which can have a glue specified by \ensurevspace, so that it is referred to by \pcol@sync as the minimum space required below the synchronization point we are now setting. Second, we invoke \pcol@visitallcols temporarily turning $\forall ifpcol@sync = false$ for column-scanning to visit all columns but current one to give T_FX's page builder the chance to break column-pages in the top page with page-wise footnotes which could have not been presented in the last visit of the columns. Third, we make an \output request with \penalty = \pcol@op@switch to invoke \pcol@output@switch by $\protect\$ victor with $\$ if pcol@sync = true to make synchronized switch to the column d. This invocation may result in $\left(\frac{1}{2}\right)$ in $\left(\frac{1$ broken before setting the synchronization point. Therefore if so, since \pcol@output@switch switched to the tallest column rather than d, we put $\$ vfil and $\$ penalty-10000 to force page break, make column-scan with \newpage put into each column to have some floats in the column in the new top page, and then invoke \pcol@output@switch again until it returns $\forall f$ if pcol f full f if f is the synchronization point switching to the column d. Then as the last operation specific to synchronized column-switching, we invoke \ensurevspace with \baselineskip to give the default of V_E for the next synchronization.

Otherwise, i.e., if $\ightharpoonup = false$, we simply make the \output request for $\pole output@switch$ to switch to the column d.

Then we scan Θ_d applying \pcol@setctrelt to each $\langle \theta^l, val_d(\theta^l) \rangle \in \Theta_d$ to let $val(\theta^l) = val_d(\theta^l)$. We also scan $T = \pcol@aconly applying \pcol@aconlyelt to each <math>\langle t_c, c \rangle \in T$ to inhibit \addcontentsline to the contents file of type t_d as specified so by \addcontentsonly $\langle t_d \rangle$ $\langle d \rangle$. After that, we let \@elt = \relax to make it sure that any lists can be manipulated with-

out unexpected application of a macro to their elements.

Finally, we invoke $\coloredge coloredge colo$ mean the column-switching is for a spanning text, or c = d otherwise.

```
2397 \def\pcol@switchcol{%
      \pcol@savecounters
2398
      \ifpcol@sync
2399
2400
        \@tempdima\pcol@ensurevspace\relax
        \edef\pcol@@ensurevspace{\number\@tempdima sp\relax}%
2401
        \global\pcol@syncfalse \pcol@visitallcols\@@par \global\pcol@synctrue
2402
        \pcol@invokeoutput\pcol@op@switch
2403
        \@whilesw\ifpcol@flush\fi{%
2404
          \vfil \penalty-\@M
2405
2406
          \global\pcol@syncfalse \pcol@visitallcols\newpage \global\pcol@synctrue
2407
          \pcol@invokeoutput\pcol@op@switch}%
        \ensurevspace{\baselineskip}%
2409
      \else
2410
        \pcol@invokeoutput\pcol@op@switch
      \fi
2411
      \let\@elt\pcol@setctrelt
2412
      \csname pcol@counters\number\pcol@currcol\endcsname
2413
      \let\@elt\pcol@aconlyelt \pcol@aconly \let\@elt\relax
2414
      \@nameuse{pcol@colpream\ifpcol@sptextstart-1\else\number\pcol@currcol\fi}}
2415
2416
```

 \color{o} The macro \color{o} is italled so \color{o} , invoked from \color{o} witched and \color{o} color of the macro \color{o} invoked from \color{o} and \color{o} color of the macro \color{o} invoked from \color{o} and \color{o} color of the macro \color{o} invoked from \color{o} and \color{o} invoked from \color{o} and \color{o} invoked from \color{o} inv performs column-scanning putting $\langle cs \rangle$ into the visited columns. That is, we repeat the invocation of \pcol@output@switch to visit d through \pcol@invokeoutput with \penalty = \pcol@op@switch for all $d \in [0, C) - \{c\}$. In each visit, we put $\langle cs \rangle \in \{\Qopar, \newpage\}$ to have a chance of or to force page break in each visited column-page. Finally we go back to cto restore its column-context especially when we are leaving the column 0 for spanning text. That is, $\kappa_c(\sigma)$ and $\kappa_c(\varepsilon)$ should be presented to \pcol@output@switch to broadcast them to other columns.

```
2417 \def\pcol@visitallcols#1{\begingroup
      \@tempcnta\z@ \@tempcntb\pcol@currcol
2418
      \@whilenum\@tempcnta<\pcol@ncol\do{%
2419
        \ifnum\@tempcnta=\@tempcntb\else
2420
2421
          \pcol@nextcol\@tempcnta \pcol@invokeoutput\pcol@op@switch #1%
2422
        \advance\@tempcnta\@ne}%
2423
      \pcol@nextcol\@tempcntb \pcol@invokeoutput\pcol@op@switch
2424
2425
      \endgroup}
```

\column* \pcol@com@column \pcol@com@column* \pcol@defcolumn The macros \pcol@com@column(*), the implementations of the environment-local API commands \column(*), starts the environment column(*). Basically, the macros do \switch column(*), but if the environment starts just after \begin{paracol} the macro have to switch to the column 0. Therefore, the definitions for this very-beginning appearance are given in \pcol@zparacol to do (almost) nothing, and then those for other ones are given by \pcol@ defcolumn invoked in \pcol@com@switchcolumn to invoke \pcol@switchenv{column(*)}(*) which then invokes \switchcolumn. Note that the definition of non-starred \pcol@com@column has \relax after the invocatoin of \pcol@switchenv so that \@ifnextchar and \@ifstar to examine the existence of '[' and '*' definitely tells us no even if the body of the environment

```
2427 \def\pcol@defcolumn{%
                                                                                                                                                                                     \gdef\pcol@com@column{\pcol@switchenv{column}\relax}%
                                                                                                                                                                                      \global\@namedef{pcol@com@column*}{\pcol@switchenv{column*}*}}
                                                                                                                                                          The macros \pcol@com@nthcolumn(*)\langle d\rangle, \pcol@com@leftcolumn(*) and \pcol@com@right
                                                                                      \nthcolumn
                                                                                                                                                            column(*) are the implementations of environment-local API macros \t nthcolumn(*)\langle d \rangle,
                                                                                 \nthcolumn*
                                                                                                                                                            \leftcolumn(*) and \rightcolumn(*) respectively. They start corresponding environments
                                   \pcol@com@nthcolumn
                                                                                                                                                            nthcolumn(*), leftcolumn(*), and rightcolumn(*) simply invoking \pcol@switchenv{env}
                              \pcol@com@nthcolumn*
                                                                                \leftcolumn
                                                                                                                                                            (*), where \langle env \rangle is the name of each environment, giving it d, 0 and 1 repectively as its optional
                                                                           \leftcolumn*
                                                                                                                                                          argument for the target column.
                            \pcol@com@leftcolumn*2432 \@namedef{pcol@com@nthcolumn*}#1{\pcol@switchenv{nthcolumn*}[#1]*}
                                                                           \rightcolumn 2433 \def\pcol@com@leftcolumn{\pcol@switchenv{leftcolumn}[0]\relax}
                                                                     \rightcolumn* 2434 \@namedef{pcol@com@leftcolumn*}{\pcol@switchenv{leftcolumn*}[0]*}
                      \verb|\pcol@com@rightcolumn| 2435 \\ | def\pcol@com@rightcolumn{\pcol@switchenv{rightcolumn}[1] \\ | relax{}| def\pcol@com@rightcolumn}| (a) | for each of the property of the pro
                   \verb|\pcol@com@rightcolumn*| 2436 $$ \end{fight} $$$ \end{fight} $$ \end{fight} $$ \end{fight} $$ \end{fight} $$$ \end{fig
                                                         \pcol@switchenv
                                                                                                                                                          The macro \pcol@switchenv\langle env \rangle is invoked from \pcol@com@\langle env \rangle where \langle env \rangle \in \{\text{column}\}
                                                                                                                                                             (*), nthcolumn(*), leftcolumn(*), rightcolumn(*)} to invoke \switchcolumn with the argu-
                                                                                                                                                            ments following \langle env \rangle given by the invoker macros. Before invoking \switchcolumn, we save
                                                                                                                                                            it in \reserved@a for the invocation and re\define it so that it will complain the illegal usage
                                                                                                                                                            of column-switching commands/environments in the environment \langle env \rangle by \PackageError.
                                                                                                                                                   2438 \def\pcol@switchenv#1{\let\reserved@a\switchcolumn
                                                                                                                                                                                     \def\switchcolumn{\PackageError{paracol}{%
                                                                                                                                                                                                Column switching commands and environments cannot be used in #1}\@eha}
                                                                                                                                                   2440
                                                                                                                                                   2441
                                                                                                                                                                                     \reserved@a}
                                                                                                                                                   2442
                                                                                      \endcolumn The macro \pcol@com@endcolumn is the implementation of the environment-local API macro
                                                                                                                                                            \endcolumn to close column environment.
                                                                                                                                                                                                                                                                                                                                                                                                                         The macro makes it sure we are in verti-
                                                                                 \endcolumn*
                                                                                                                                                          cal mode by \pcol@par and \globalize \everypar so that it is saved in \kappa_c(\varepsilon) of the
                                  \pcol@com@endcolumn
                                                                                                                                                           current column c on the switch to another column. The macro also gives the comm-
                              \pcol@com@endcolumn*
                                                                                                                                                            mon definition of \pcol@com@endcolumn* for \endcolumn*, \pcol@com@endnthcolumn(*) for
                                                                     \endnthcolumn
                                                                                                                                                             \endnthcolumn(*), \pcol@com@endleftcolumn(*) for \endleftcolumn(*), and \pcol@com@
                                                                \endnthcolumn*
                 \pcol@com@endnthcolumn endrightcolumn(*) for \endrightcolumn(*).
           \verb|\pcol@com@endnthcolumn*|_{2443} \label{pcol@com@endcolumn*||_2443} $$ \end{|\pcol@com@endcolumn*|} $$
                                                               \endleftcolumn 2444 \expandafter\global\expandafter\everypar\expandafter{\the\everypar}}
                                                         \verb|\end| end | ftcolumn*| 2445 \verb|\expandafter| let| csname | pcol@com@endcolumn*| lendcsname| pcol@com@endcolumn*| lendcsname| pcol@com@endcolumn*| lendcsname| l
           \verb|\pcol@com@endleftcolumn|| 2446 \verb|\let\pcol@com@endnthcolumn|| pcol@com@endcolumn|| and a second conditions are also conditions as a second condition of the conditions are also conditions as a second condition of the conditions are also conditions as a second condition of the conditions are also conditions as a second condition of the conditions are also conditions as a second condition of the conditions are also conditions as a second condition of the conditions are also conditions are also conditions as a second condition of the conditions are also condit
      \verb|\pcol@com@endleftcolumn*| 2447 \verb|\expandafter\let\csname| pcol@com@endnthcolumn*| endcsname\pcol@com@endcolumn*| and the property of the p
                                                         \verb|\endrightcolumn|| 2448 \verb|\endrightcolumn||
                                                   \label{thm:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:column:col
                      \define column preamble \define column preamble \define the column preamble \define the column preamble \define \def
```

starts with a '[' or '*'.

for the column c or that for spanning texts if c=-1. After assiging c to \Qtempcnta to ensure

c is a number, the macro \pcol@colpream $\cdot c$ is \defined to have $\langle pream \rangle$.

```
2453 \def\definecolumnpreamble#1#2{\@tempcnta#1\relax
      \expandafter\gdef\csname pcol@colpream\number\@tempcnta\endcsname{#2}}
2454
2455
```

\ensurevspace \pcol@ensurevspace \pcol@@ensurevspace

The API macro \ensurevspace{space} is to declare that the synchronization point following it must be thrown to the next page unless the page has the vertical $\langle space \rangle$ below the synchronization point. The macro makes a dummy assignment of $\langle space \rangle$ to \Qtempdima to ensure the argument is a dimension including forced one, or in other words to raise an error if not in this macro rather than at the time $\langle space \rangle$ is evaluated in \pcol@switchcol. Then $\langle space \rangle$ is kept in \pcol@ensurevspace so that \langle space \rangle is evaluated in \pcol@switchcol for the synchronization in question to pass the value to $\pcol@sync$ through the macro $\pcol@ensurevspace = V_E$, especially when it has register references, for example to \baselineskip. To give the default of \pcol@ensurevspace, we invoke \ensurevspace at the top level with \baselineskip.

```
2456 \def\ensurevspace#1{{\@tempdima#1\relax \gdef\pcol@ensurevspace{#1}}}
2457 \ensurevspace{\baselineskip}
2458
```

16 Disabling \addcontentsline

\addcontentsonly \pcol@aconly The API macro \addcontentsonly $\langle t \rangle \langle c \rangle$ makes the type t contents file written by commands appearing only in the column c. The macro simply add the pair $\langle t, c \rangle$ to the list $T = \protect{\protect\protec$ and lot so far, by the fact \pcol@ac@def t is defined, or abort execution by \PackageError.

```
2459 %% Disabling \addcontentsline
2460
2461 \def\addcontentsonly#1#2{%
2462
      \@ifundefined{pcol@ac@def@#1}
        {\PackageError{paracol}{Unknown contents type #1}\@eha}\relax
2463
      \cons\pcol@aconly{{#1}{#2}}}
2464
2465 \gdef\pcol@aconly{}
```

 $\protect\$ The macro $\protect\$ is invoked solely in $\protect\$ for the columnswitching to column c, and is applied to each $\langle t_d, d \rangle \in T$ to enable \addcontentsline for t_d if d=c by the invocation of \pcol@ac@def@· t_d with an argument enable, or to disable if $d\neq c$ with disable.

```
2467 \def\pcol@aconlyelt#1#2{%
      \ifnum#2=\pcol@currcol \@nameuse{pcol@ac@def@#1}{enable}%
2468
2469
      \else \@nameuse{pcol@ac@def@#1}{disable}%
2470
```

\pcol@gobblethree \pcol@addcontentsline

The macro \pcol@gobblethree $\langle file \rangle \langle sec \rangle \langle entry \rangle$ is used in \pcol@ac@disable@toc and \pcol@ ac@caption to make \addcontentsline \let-equal to this macro, which does nothing but discarding three arguments, for disabling. The macro \pcol@addcontentsline is the LATEX's original \addcontentsline and is used in the macros mentioned above to let \addcontentsline act as original.

```
2471 \def\pcol@gobblethree#1#2#3{}
2472 \let\pcol@addcontentsline\addcontentsline
2473
```

\pcol@ac@def@toc \pcol@ac@enable@toc \pcol@ac@disable@toc The macro $\protect\operatorname{QacQdefQtoc}\langle eord \rangle$ is invoked solely in $\protect\operatorname{QacQnlyelt}\{toc\}\langle e \rangle$ to enable or disable \addcontentsline according to \(eord \) by making \@sect \let-equal to \pcol@ ac@enable@toc which is the LATEX's original \@sect, or to \pcol@ac@disable@toc respectively. The macro \pcol@ac@disable@toc $\langle a_1 \rangle \langle a_2 \rangle \langle a_3 \rangle \langle a_4 \rangle \langle a_5 \rangle \langle a_6 \rangle [\langle a_7 \rangle] \langle a_8 \rangle$ at first disables \addcontentsline by making it \let-equal to \pcol@gobblethree, then invokes the original \@sect saved in \pcol@ac@enable@toc ginving it all arguments a_1 to a_8 , and finally enables it by making it $\ensuremath{\mbox{let-equal}}$ to $\ensuremath{\mbox{\mbox{col}@addcontentsline}}$. Note that the argument a_7 is surrounded by { and } on the invocation of \@sect to conceal ']' in a_7 .

```
2474 \def\pcol@ac@def@toc#1{%
     \expandafter\let\expandafter\@sect\csname pcol@ac@#1@toc\endcsname}
2476 \let\pcol@ac@enable@toc\@sect
2477 \def\pcol@ac@disable@toc#1#2#3#4#5#6[#7]#8{%
      \let\addcontentsline\pcol@gobblethree
      \pcol@ac@enable@toc{#1}{#2}{#3}{#4}{#5}{#6}[{#7}]{#8}%
2479
2480
      \let\addcontentsline\pcol@addcontentsline}
2481
```

\pcol@ac@def@lof \pcol@ac@def@lot \pcol@ac@caption@enable \pcol@ac@caption@disable \pcol@ac@caption@def \pcol@ac@caption@if@lof \pcol@ac@caption@if@lot The macro $\protect\operatorname{pcol@ac@def@lof}\langle eord\rangle$ and $\protect\operatorname{pcol@ac@def@lot}\langle eord\rangle$ are invoked solely in enable $\langle t \rangle$ or \pcol@ac@caption@disable $\langle t \rangle$ according to $\langle eord \rangle$, and then these macros invoke \pcol@ac@caption@def $\langle s
angle \langle t
angle$ where s= \@tempswatrue or s= \@tempswafalse respectievely to let \@caption = \pcol@ac@caption and \pcol@ac@caption@if@t = s which are \letequal to \@tempswatrue in default. That is, \pcol@ac@catption@if@·t lets \if@tempswa = $true iff \addcontentsline for t is to be enable.$

```
2482 \end{argmap} $2482 \end{a
2483 \end{argmath} $2483 \end{argmath} $$ \end{argmath} $$ \end{argmath} $$ 2483 \end{argmath} $$ \end{arg
2484 \label{pcolQacQcaptionQenable} \label{pcolQacQcaptionQdef\def} \\ 2484 \label{pcolQacQcaptionQenable} 
2485 \def\pcol@ac@caption@disable{\pcol@ac@caption@def\@tempswafalse}
2486 \def\pcol@ac@caption@def#1#2{\let\@caption\pcol@ac@caption
2487 \expandafter\let\csname pcol@ac@caption@if@#2\endcsname#1}
2488 \let\pcol@ac@caption@if@lof\@tempswatrue
2489 \let\pcol@ac@caption@if@lot\@tempswatrue
```

\pcol@ac@caption@latex

 $\label{lem:condition} \begin{tabular}{ll} The macro $$ \col@ac@caption $$ to $$ (larp) $$ (lar$ ac@caption@def to do what \@caption do but with enabling/disabling \addcontentsline. At first, it invokes $\pcol@ac@cation@if@\cdot t$ where $t = \ext@\cdot \langle type \rangle$ to let $\if@tempswa$ be true or false according to the enable/disable status of t. Then, after letting $\$ addcontentsline = $\polement{\colored}$ for disabling if false, we invoke $\polement{\colored}$ caption@latex, being the LATEX's original \@caption, giving all three arguments of \pcol@ac@caption itself surrounding $\langle lcap \rangle$ with { and } for the concealment of ']'. Finally, we let \addcontentsline = \pcol@addcontentsline so that other macros uses it with its original definition.

```
2490 \long\def\pcol@ac@caption#1[#2]#3{%
      \@nameuse{pcol@ac@caption@if@\@nameuse{ext@#1}}%
2492
      \if@tempswa\else \let\addcontentsline\pcol@gobblethree \fi
      \pcol@ac@caption@latex{#1}[{#2}]{#3}%
2493
      \let\addcontentsline\pcol@addcontentsline}
2495 \let\pcol@ac@caption@latex\@caption
2496
```

17 Page Flushing Commands

\flushpage
\pcol@com@flushpage
\clearpage
\pcol@com@clearpage
\cleardoublepage
\pcol@com@cleardoublepage

The macros \pcol@com@flushpage, \pcol@com@clearpage and \pcol@com@cleardoublepage are the implementations of environment-local API macro \flushpage, \clearpage and \cleardoublepage respectively. The first two have a common structure in which we at first invoke \pcol@flushclear for column-scan and pre-flushing column height check, and then make an \output request by \pcol@invokeoutput with \penalty being \pcol@op@flush or \pcol@op@clear according to the commands. On the other hand the last one simply invokes \pcol@com@clearpage unconditionally, and then \pcol@com@flushpage^{230} if two-sided paging is enabled by \if@twoside = true, we are in an even-numbered page, and \ifpcol@paired = false to mean we are not doing non-paired parallel-paging.

```
2497 %% Page Flushing Commands
2498
2499 \def\pcol@com@flushpage{\pcol@flushclear\voidb@x
2500 \pcol@invokeoutput\pcol@op@flush}
2501 \def\pcol@com@clearpage{\pcol@flushclear\voidb@x
2502 \pcol@invokeoutput\pcol@op@clear}
2503 \def\pcol@com@cleardoublepage{\pcol@com@clearpage
2504 \if@twoside \ifodd\c@page\else \ifpcol@paired\else \pcol@com@flushpage
2505 \fi\fi\fi}
```

\pcol@flushclear

The macro $\pool@flushclear\langle box\rangle$, invoked from $\pool@com@flushpage$, $\pool@com@clear page$ and $\pool@com@clear page$ and $\pool@com@clear page$ flushing or environment closing. After confirming we are in vertical mode by $\pool@com@clear page$ and letting $d = \pool@com@clear page$ prool@comrol to stay in c, we invoke $\pool@com@clear page$ visitallcols for column-scan to give $\pool@com@clear page$ builder the chance to break the top page prior to flushing it.

Then we repeat pre-flushing column height check invoking $\pool@output@switch$ through $\pool@invokeoutput$ with $\pool@op@switch$ and $\pool@clear = \pool@sync = true$ until the special $\pool@op@switch$ if pcol@flush = false and $\pool@op@switch$ and $\pool@o$

Finally we let \ightharpoonup its default setting, i.e., false.

```
2506 \def\pcol@flushclear#1{\pcol@par
      \pcol@nextcol\pcol@currcol
2507
      \pcol@visitallcols\@@par
      \pcol@cleartrue \global\pcol@synctrue
      \ifpcol@lastpage \pcol@lastpagesavetrue \else \pcol@lastpagesavefalse \fi
2510
2511
      \pcol@invokeoutput\pcol@op@switch \ifvoid#1\else \global\pcol@flushtrue \fi
2512
      \@whilesw\ifpcol@flush\fi{%
        \pcol@lastpagefalse
2513
2514
        \vfil \penalty-\@M \pcol@cleartrue \global\pcol@synctrue
2515
        \ifpcol@lastpagesave \pcol@lastpagetrue \fi
2516
        \pcol@invokeoutput\pcol@op@switch
```

²³⁰Unlike IATEX's **\cleardoublepage**, it is unnecessary to put an empty **\hbox** before **\flushpage** because it is active even at the top of a page.

```
2517 \ifvoid#1\else \global\pcol@flushtrue \fi}%
2518 \pcol@clearfalse}
2519
```

18 Commands for Footnotes

\footnotelayout
\pcol@fnlayout@p
\pcol@fnlayout@m
\multicolumnfootnotes
\singlecolumnfootnotes
\mergedfootnotes

The API macros \footnotelayout{l} is to determine that footnotes are column-wise (l = c), page-wise without merging (l = p), or merged and page-wise (l = m). The macro examines if $l \in \{c, p, m\}$ by the existence of the corresponding macro \pcol@fnlayout@l and invokes it, or complains if not by \PackageError.

The macros \pcol@fnlayout@c, \pcol@fnlayout@p and \pcol@fnlayout@m turn switches $f_s = \ensuremath{\mbox{\mbox{outem} Grad}} = \ensuremath{\mbox{\mbox{\mbox{outem} Grad}}} = \ensuremath{\mbox{\mbox{outem} Grad}} = \ensuremath{\mbox{\mbox{\mbox{outem} Grad}}} = \ensuremath{\mbox{\mbox{\mbox{\mbox{outem} Grad}}} = \ensuremath{\mbox{\mbox{\mbox{\mbox{outem} Grad}}} = \ensuremath{\mbox{\$

l	$ f_s $	f_m	f_a	footnote
С	false	false	false	local
р	true	false	true	global
m	true	true	true	global

Note that turning \ifpcol@fncounteradjustment is done by \fincounteradjustment (true) or \nofncounteradjustment (false). Also note that the setting of \ifpcol@fncounteradjustment and the globalization/localization of footnote are just to give defaults and thus can be overridden by API macros giving non-default settings. Another remark is that backward-compatible macros \multicolumnfootnotes, \singlecolumnfootnotes and \mergedfootnotes are \let-equal to \pcol@fnlayout@c, \pcol@fnlayout@p and \pcol@fnlayout@m respectively.

```
2520 %% Commands for Footnotes
2521
2522 \def\footnotelayout#1{\@ifundefined{pcol@fnlayout@#1}%
2523 {\PackageError{paracol}{Unknown footnote layout specifier #1}}%
2524 {\@nameuse{pcol@fnlayout@#1}}}
2525 \def\pcol@fnlayout@c{\global\pcol@scfnotefalse \global\pcol@mgfnotefalse}
2526 \localcounter{footnote}\nofncounteradjustment}
2527 \def\pcol@fnlayout@p{\global\pcol@scfnotetrue \global\pcol@mgfnotefalse}
2528 \globalcounter{footnote}\fncounteradjustment}
2529 \def\pcol@fnlayout@m{\pcol@fnlayout@p\global\pcol@mgfnotetrue}}
2530
2531 \let\multicolumnfootnotes\pcol@fnlayout@p
2533 \let\mergedfootnotes\pcol@fnlayout@m
2534
```

\@footnotetext
 \pcol@fntext
 \pcol@fntexttop
\pcol@fntextother

The macro \polement{text} is our own version of \polement{ATEX} 's \polement{def} of the theorem and \polement{level} through \polement{level} through \polement{level} original and our own are made \polement{level} pcolezparacol, our own is active throughout the environment. The customization is done to examine if the footnote should be deferred and to encapsulate the footnote in a \polement{level} vbox.

The deferred footnote insertion is in effect if the footnote typesetting is page-wise and \footnote or \footnotetext appears in a page $p < p_t$. If so, we put the footnote $\langle text \rangle$ encapsulated in a \vbox by \pcol@fntextbody to the tail of $\Phi = \pcol@topfnotes$ with \penalty\interlinepenalty preceding it for the split in \pcol@deferredfootins, using

\pcol@fntextother{text} whose sole user is this macro. Note that the decision of deferring is done based on $p = \pcol@page$ which could be less than that of the page in which the footnoted text appears because the paragraph having the text will have a page break before the text. Therefore, p for the footnote can be p_t , but this misjudment will not cause problems because the footnote will eventually be put in p_t through Φ when the page break occurs.

Otherwise the footnote $\langle text \rangle$ is processed by \cline{text} , also used solely in this macro, to \cline{text} is processed by \cline{text} , also used solely in this macro, to \cline{text} is processed by \cline{text} , also used solely in this macro, to \cline{text} in through \cline{text} following it to allow \cline{text} page builder to split footnotes.

Note that $\protect\p$

```
2535 \def\pcol@fntext{%
      \let\reserved@a\pcol@fntexttop
2537
      \ifpcol@scfnote \ifnum\pcol@page<\pcol@toppage
2538
        \let\reserved@a\pcol@fntextother
2539
      \fi\fi
      \reserved@a}
2540
2541 \long\def\pcol@fntexttop#1{%
2542
      \pcol@Logfn{\pcol@fntexttop{\@thefnmark}}%
      \insert\footins{\pcol@fntextbody{#1}\penalty\interlinepenalty}}
2543
2544 \long\def\pcol@fntextother#1{%
      \global\setbox\pcol@topfnotes\vbox{\unvbox\pcol@topfnotes
        \penalty\interlinepenalty\pcol@fntextbody{#1}}}
2546
```

\pcol@fntextbody

The macro $\pcol@fntextbody{text}$, invoked from $\pcol@fntexttop$ and $\pcol@fntext$ other, encapsulates the footnote $\langle text \rangle$ in a $\pcol@fntext$ beight is $h_{max} = \textheight - \skip \textheight$ at tallest. The encapsulation is to inhibit page breaks in a footnote because the split by the break will make some skips and other items eliminated causing a weird result when split portions are *joined*. The height capping is thus required to find a page in which the footnote resides.

The macro at first does operations done in LATEX's \@footnotetext to put $\langle text \rangle$ in \@tempboxa but with one exception that \hsize = \textwidth rather than \columnwidth when page-wise footnote typesetting is in effect. Note that this part is blindly copied from the original though it should be meaningless to set \interlinepenalty, \splittopskip, \splitmaxdepth and \floatingpenalty because $\langle text \rangle$ is encapsulated.

Then the height-plus-depth of the box is compared with h_{max} and, if it exceeds the limit, the height of the box is set h_{max} , the footnote is made followed by a **\vss** to avoid overfull, and a warning message of too tall is put by **\PackageWarning**. Finally, the box is put into **\footnotins** or Φ by the invoker of this macro.

```
2547 \long\def\pcol@fntextbody#1{\setbox\@tempboxa\vbox{%
        \reset@font\footnotesize
2548
        \interlinepenalty\interfootnotelinepenalty
2549
        \splittopskip\footnotesep
2550
        \splitmaxdepth\dp\strutbox \floatingpenalty\@MM
2551
        \hsize \ifpcol@scfnote \textwidth \else \columnwidth \fi
2552
2553
2554
        \protected@edef\@currentlabel{\p@footnote\@thefnmark}%
2555
        \color@begingroup
2556
        \@makefntext{%
          \rule\z@\footnotesep\ignorespaces#1\@finalstrut\strutbox}%
2557
2558
        \color@endgroup}%
2559
      \@tempdima\ht\@tempboxa \advance\@tempdima\dp\@tempboxa
```

```
\Otempdimb\textheight \advance\Otempdimb-\skip\footins
2560
      \ifdim\@tempdima>\@tempdimb
2561
        \setbox\@tempboxa\vbox to\@tempdimb{\unvbox\@tempboxa\vss}%
2562
        \PackageWarning{paracol}{Too tall footnote}%
2563
2564
      \box\@tempboxa}
2565
```

\fncounteradjustment \nofncounteradjustment

The API macros \fincounteradjustment and \nofncounteradjustment turns \ifpcol@ fncounteradjustment true or false, to enable or disable the footnote counter adjustment letting \contote = $b_f + n_f$ in \end{paracol}, respectively. After the definition we disable the adjustment to give the default setting.

```
2567 \def\fncounteradjustment{\global\pcol@fncounteradjustmenttrue}
2568 \def\nofncounteradjustment{\global\pcol@fncounteradjustmentfalse}
2569 \nofncounteradjustment
```

\pcol@footnoterule \pcol@footnote \pcol@@footnotemark \pcol@@footnotetext

The macros \pcol@footnoterule, \pcol@@footnote, \pcol@@footnotemark and \pcol@@ footnotetext are to keep the original defitions of \footnoterule, \footnote, \footnotemark and \footnotetext in them, respectively, so that we define our own versions with references to the originals.

```
2571 \let\pcol@footnoterule\footnoterule
2572 \let\pcol@@footnote\footnote
2573 \let\pcol@@footnotemark\footnotemark
2574 \let\pcol@footnotetext\footnotetext
```

\footnote \pcol@footnote \pcol@ifootnote \footnotemark \pcol@footnotemark \pcol@ifootnotemark

The macros \pcol@footnote and \pcol@footnotemark are the implementations of our own versions of \footnote and \footnotemark which are made \let-equal to them by \pcol@ zparacol, respectively. The reasons why we need to have our own are two-fold; to have starred version of them; and to maintain $n_f = \text{pcol@nfootnotes}$ for the footnote counter adjustment.

The implementations of the starred versions \footnote*[num] {text} and \footnotemark* [num] have common structure in which we invoke $\pcol@adjustfnctr(macro)[num]$ if '*' is given, to let \confortnote have the number relative to $b_f = \protect\$ or to itself. Then the macros \pcol@ifootnote or \pcol@ifootnotemark are invoked from \pcol@ adjustfnctr or the else-part of \@ifstar to perform the operations common to both cases with and without '*', i.e., invoking the original version \pcol@footnote or \pcol@footnotemark after incrementing n_f . One caution is that $\langle macro \rangle = \prolemont{\cite{Control}}$ but $\langle macro \rangle = \{\pcol@ifootnotemark\relax\}\$ for $\pcotnotemark\$ so that $\pcol@ifootnotemark\$ in \pcol@@footnotemark invoked from \pcol@ifootnotemark eats \relax to terminate space skipping and thus spaces following [num] are kept.

```
2575 \def\pcol@footnote{\@ifstar{\pcol@adjustfnctr\pcol@ifootnote}\pcol@ifootnote}
2576 \def\pcol@ifootnote{\global\advance\pcol@nfootnotes\@ne \pcol@@footnote}
2577 \def\pcol@footnotemark{\@ifstar
     {\pcol@adjustfnctr{\pcol@ifootnotemark\relax}}%
      \pcol@ifootnotemark}
2580 \def\pcol@ifootnotemark{\global\advance\pcol@nfootnotes\@ne
     \pcol@@footnotemark}
```

\pcol@adjustfnctr

The macro $\protection \protection \prote$ \pcol@footnote and \pcol@footnotemark, calculates the number to be set into \c@footnote \pcol@calcfnctr by \pcol@calcfnctr $\langle num \rangle$ \@nil after processing the optional argument $\langle num \rangle$ by \pcol@

iadjustfnctr with default '+1', and then invoke $\langle macro \rangle$ being \pcol@ifootnote or \pcol@ifootnote with the number \c@footnote should have and the counter is incremented by \stepcounter in \pcol@@footnote or \pcol@@footnote wark, we decrement the counter prior to invoke $\langle macro \rangle$.

The macro \pcol@calcfnctr $\langle num \rangle$ \@nil, also invoked from \pcol@iifootnotetext, calculate m specified by $\langle num \rangle$ as follows, where f = c@footnote, to return it through \@tempcnta.

$$m = \begin{cases} f + k & \langle num \rangle = +k \\ f - k & \langle num \rangle = -k \\ b_f + k & \langle num \rangle = k \end{cases}$$

```
2582 \def\pcol@adjustfnctr#1{\@ifnextchar[%]
                              \{\pcol@iadjustfnctr{\#1}\} \{\pcol@iadjustfnctr{\#1}[+1]\} \} 
2584 \ensuremath{\mbox{\sc 1}} 4 \ensuremath{\mbox{\sc 1}} = 1 \
                             \global\c@footnote\@tempcnta \global\advance\c@footnote\m@ne#1}
2586 \def\pcol@calcfnctr#1#2\@nil{\@tempcnta\c@footnote
                             \def\reserved@a{#1}\def\reserved@b{+}%
2587
2588
                             \ifx\reserved@a\reserved@b \advance\@tempcnta#2\relax
2589
                             \else \def\reserved@b{-}%
                             \ifx\reserved@a\reserved@b \advance\@tempcnta-#2\relax
                             \else \@tempcnta\pcol@footnotebase \advance\@tempcnta#1#2\relax
2591
2592
                             fi\fi
```

\footnotetext \pcol@footnotetext \pcol@iifootnotetext \pcol@iifootnotetext The macros \pcol@footnotetext is the implementation of our own versions of \footnotetext which is made \let-equal to it by \pcol@zparacol. The reasons why we need to have our own is to have the starred version. That is, if '*' is not given, we simply invoke the original version \pcol@@footnotetext. Otherwise we invoke \pcol@ifootnotetext which then examines if the optional argument [num] is presented. If so, we invoke \pcol@ifootnotetext in which \pcol@calcfnctr $\langle num \rangle$ \@nil is invoked to have the value m being the footnote ordinal with which we invoke \pcol@@footnotetext[m] with two \expandafters to extract m from \@tempcnta. Otherwise, i.e., [num] is not given, we increment \c@footnote by \stepcounter before invoking \pcol@@footnotetext.

```
2593 \def\pcol@footnotetext{\@ifstar\pcol@ifootnotetext\pcol@@footnotetext}
2594 \def\pcol@ifootnotetext{\@ifnextchar[%]
2595 \pcol@iifootnotetext{\stepcounter{footnote}\pcol@@footnotetext}}
2596 \def\pcol@iifootnotetext[#1]{\pcol@calcfnctr#1\@nil
2597 \expandafter\pcol@@footnotetext\expandafter[\number\@tempcnta]}
2598
```

19 Commands for Marginal Notes

\marginpar
\pcol@marginpar
\pcol@marginnote
\pcol@marginnote
\pcol@marginnote
\pcol@mn@warning
\@xympar
\pcol@xympar
\pcol@xympar

The API macro \marginnote[left]{right}[voffset] given by the package marginnote is emulated using \marginpar[left]{right} and \pcol@addmarginpar in \output routine. The basic mechanism is to pass the vertical offset $\langle voffset \rangle$ to \pcol@addmarginpar through \dimen $\langle b \rangle$ where b is the \insert to carry $\langle left \rangle$. The offset passing is implemented as follows.

• \marginpar is made \let-equal to our own version \pcol@marginpar in \pcol@zparacol so that it \let the macro \pcol@mparoffset be \z@ and then invoke LATEX's origincal version kept in \pcol@@marginpar, because the marginal note given by \marginpar will not be shifted.

- The internal macro \@mn@@marginnote [left] {right} [voffset] defined in marginnote is made \let-equal to our own version \pcol@marginnote in \pcol@zparacol so that it \defines \pcol@mparoffset to have $\langle voffset \rangle$ and then invoke \pcol@marginpar [left] {right} for the emulation. In the invokation, marginnote's typesetting macros \margin font, \raggedleftmarginnote and \raggedrightmarginnote are attached to $\langle left \rangle$ and $\langle right \rangle$.
- LaTeX's internal macro \@xympar for the last operations of \marginpar is made \letequal to our own version in \pcol@zparacol so that it assigns the offset in \pcol@mparoffset to \dimen\@marbox for \left\, if \@floatpenalty < 0 to mean other macros for \marginpar have not detected any errors.

In addition, we raise a warning that \marginnote is emulated by \pcol@mn@warning, which is made \let-equal to \relax in the caller \pcol@marginnote after the invokation so that the warning message is put just once.

```
2599 %% Commands for Marginal Notes
2600
2601 \def\pcol@marginpar{\let\pcol@mparoffset\z@ \pcol@@marginpar}
2602 \long\def\pcol@marginnote[#1]#2[#3]{\endgroup
      \pcol@mn@warning \global\let\pcol@mn@warning\relax
2604
      \def\pcol@mparoffset{#3}%
      \pcol@@marginpar[\marginfont\raggedleftmarginnote#1]%
2605
                       {\marginfont\raggedrightmarginnote#2}}
2606
2607 \def\pcol@mn@warning{%
      \PackageWarning{paracol}{\string\margninnote\space is emulated by
2608
        \string\marginpar.}}
2609
2610 \def\pcol@xympar{%
2611
      \ifnum\@floatpenalty<\z@ \global\dimen\@marbox\pcol@mparoffset\relax \fi
2612
      \pcol@@xympar}
2613
```

20 Two-Sided Typesetting

\twosided
\pcol@twosided
\pcol@twosided@p
\pcol@twosided@m
\pcol@twosided@b
\swapcolumninevenpages
\noswapcolumninevenpages

The API macro \twosided[T] where $T=t_1t_2\cdots$ is to enable/disable two-sided paging with \if@twoside = true/false (p \in / \notin T), two-sided column-swapping with \ifpcol@swapcolumn = true/false (c \in / \notin T), two-sided marginal note placement with \ifpcol@swapmarginpar = true/false (m \in / \notin T), and/or two-sided background painting with \ifpcol@swapmarginpar = true/false (b \in / \notin T) individually, or to enable all of them as a whole when the optional argument is not given.

The macro invokes $\pcol@twosided$ with the optional argument T if provided, or with T = pcmb otherwise to enable all features. Then $\pcol@twosided$ at first turns all the switches false an then scans all non-space tokens $t \in T$ invoking $\pcol@twosided@t$ if it is defined and thus $t \in \{p, c, m, b\}$ to turn the corresponding switch true, or complains that the feature t is unknown.

Note that backward-compatible API macros \swapcolumninevenpages and \noswapcolumn inevenpages are still availabel to turn \ifpcol@swapcolumn true an false respectivey.

```
2614 %% Column Swapping
2615
2616 \def\twosided{\@ifnextchar[%]
2617 {\pcol@twosided}{\pcol@twosided[pcmb]}}
2618 \def\pcol@twosided[#1]{%
```

```
\global\@twosidefalse \global\pcol@swapcolumnfalse
2619
      \global\pcol@swapmarginparfalse \global\pcol@bg@swapfalse
2620
      \@tfor\reserved@a:=#1\do{%
2621
        \@ifundefined{pcol@twosided@\reserved@a}%
2622
2623
          {\PackageError{paracol}{Unknown two-siding feature \reserved@a}}%
          {\@nameuse{pcol@twosided@\reserved@a}}}}
2625 \def\pcol@twosided@p{\global\@twosidetrue}
2626 \def\pcol@twosided@c{\global\pcol@swapcolumntrue}
2627 \def\pcol@twosided@m{\global\pcol@swapmarginpartrue}
2628 \def\pcol@twosided@b{\global\pcol@bg@swaptrue}
2629
2630 \def\swapcolumninevenpages{\global\pcol@swapcolumntrue}
2631 \ \texttt{def} \\ \texttt{noswapcolumninevenpages{\global\pcol@swapcolumnfalse}}
```

\pcol@swapcolumn \pcol@colsepid

The macro \pcol@swapcolumn $\langle c_1\rangle\langle c_2\rangle\langle C^0\rangle\langle C^1\rangle$ converts the column ordinal c or position c' in the \count register c_2 to the position or ordinal to set it in the \count register c_2 , for a parallel-page having columns $c\in [C^0,C^1)$. That is, we let $c_2=(C^1-1)-(c_1-C^0)$ if \ifpcol@swapcolumn = true to mean the column-swapping is in effect and \c@page is even, while $c_2=c_1$ otherwise. We also let $c^g=\pcol@colsepid=c_2-1$ if swapped, or $c^g=c_2$ otherwise, so that it has the ordinal of the column-separating gap physically following the column c_2 .

The macro is used in $\pcol@ioutputelt$, $\pcol@addmarginpar$, $\pcol@imakeflushedpage and <math>\pcol@iflushfloats$ with $(c_1,c_2)=(c',c)$, and in $\pcol@addmarginpar$ (another use) with $(c_1,c_2)=(c,c')$. Note that in the uses in the macros above except for $\pcol@addmarginpar$, $\pcol@addmarginpar$ on the other hand, $\pcol@addmarginpar$ on the other hand, $\pcol@addmarginpar$ or the ship-out page number to produce a weird result if their parities are different, due to page jump. However this problem is not so severe because it just affects the position of marginal notes which $\pcol@addmarginpar$ itself may misplace.

```
2633 \def\pcol@swapcolumn#1#2#3#4{%}
      \edef\pcol@colsepid{\number#1}%
2634
2635
      \ifpcol@swapcolumn
2636
        \ifodd\c@page\relax #2#1\relax
2637
        \else
          #2#4\relax \advance#2-#1\relax \advance#2#3\relax \advance#2-\tw0
2638
2639
          \edef\pcol@colsepid{\number#2}%
          \advance#2\@ne
2640
        \fi
2641
2642
      \else #2#1\relax
2643
      \fi}
```

\marginparthreshold \pcol@marginparthreshold \pcol@mpthreshold@1 \pcol@mpthreshold@r The API macro \marginparthreshold{t_l} [t_r] determines the smallest ordinal t_l of columns in left parallel-pages whose marginal notes go to the right margin in fundamental setting of marginal note positioning, while the threshold in right parallel-pages is given by t_r if provided or by t_l otherwise. That is, marginal notes given in a column c in a page p s.t. $c \in [0, C_L)$ (resp. $[C_L, C)$) go left if $c < t_l$ (resp. $c < t_r$) while they go right if $c \ge t_l$ (resp. $c \ge t_r$), providing

 $(\infty col@swapmarginpar \land page(p) \bmod 2 = 0) \not\equiv \inf@reversemargin = false$

or the margins are swapped otherwise.

²³¹Or the \dimen register \z@.

The macro \defines \pcol@mpthreshold@l to let it have t_l after a assigning t_l to $\cline{tempcnta}$ to ensure t_l gives some number, and then do the same for $\protect{pcol@mpthreshold@}$ r with t_r by \pcol@marginparthreshold if t_r is provided, or let the marco have t_l otherwise. Note that at the top level we do \marginparthreshold{1} to give defaults. Also note that \pcol@mpthreshold@l and \pcol@mpthreshold@r are referred to solely in \pcol@ addmarginpar.

```
2645 \def\marginparthreshold#1{\@tempcnta#1\relax
      \xdef\pcol@mpthreshold@l{\number\@tempcnta}%
      \@ifnextchar[%]
2647
        \pcol@marginparthreshold(\xdef\pcol@mpthreshold@r{\number\@tempcnta}}}
2648
2649 \def\pcol@marginparthreshold[#1]{\dempcnta#1\relax}
      \xdef\pcol@mpthreshold@r{\number\@tempcnta}}
2651 \marginparthreshold{1}
2652
```

Commands for Text Coloring 21

\columncolor \pcol@xcolumncolor \pcol@ycolumncolor \pcol@columncolor The API macro \columncolor [mode] $\{color\}$ [c] defines the default color specified by $\langle color \rangle$ optionally with color $\langle mode \rangle$ of the column c being the current column or that specified by the optional argument. After \defining \pcol@colorcommand being the \string of this macro itself, and processing two optional arguments $\langle mode \rangle$ and c through macros \pcol@xcolumncolor, \pcol@ycolumncolor and \pcol@columncolor, the macro \pcol@ icolumncolor{cmd}[c] is invoked to perform real operations with the coloring command $\langle cmd \rangle = \text{\color}[mode] \{color\}.$

```
2653 %% Commands for Text Coloring
2655 \def\columncolor{\def\pcol@colorcommand{\string\columncolor}%
    \@ifnextchar[%]
      \pcol@xcolumncolor\pcol@ycolumncolor}
2658 \def\pcol@xcolumncolor[#1]#2{\pcol@columncolor{\color[#1]{#2}}}
2659 \def\pcol@ycolumncolor#1{\pcol@columncolor{\color{#1}}}
2660 \def\pcol@columncolor#1{\@ifnextchar[%]
```

\normalcolumncolor The API macro \normalcolumncolor[c] defines the default color of the column c, being the current column or that specified by the optional argument, is \normalcolor. That is, after \defining \pcol@colorcommand being the \string of this macro itself, this macro simply invokes $\pcol@icolumncolor{cmd}[c]$ to perform real operations with the coloring command $\langle cmd \rangle = \text{\ normal} \text{\ color.}$

```
2662 \def\normalcolumncolor{\def\pcol@colorcommand{\string\normalcolumncolor}%
2663
     \@ifnextchar[%]
2664
        {\pcol@icolumncolor\normalcolor}%
        {\pcol@icolumncolor\normalcolor[\number\pcol@currcol]}}
2665
```

\pcol@icolumncolor \pcol@iicolumncolor \pcol@scancst@shadow The macro $\protect\operatorname{pcol@icolumncolor}\{cmd\}[c], invoked from <math>\protect\operatorname{pcol@columncolor}$ and $\protect\operatorname{normal}$ columncolor, performs the operations to define the default color of the column c with the coloring command $\langle cmd \rangle \in \{ \color[mode] \{ color \}, \normalcolor \}$ as follows. First we examine if \set@color is not \relax and we are in non-internal vertical or non-restricted horizontal mode and, if not, we complain the command whose name is in \pcol@colorcommand is ineffective by \PackageWarning and do nothing.

Otherwise and if we are not in a paracol environment, i.e., \paracol is not \let-equal to \pcol@paracol, we simply invoke \pcol@icolumncolor to let $\hat{\gamma}_0^c = \text{pcol@columncolor} \cdot c$ have the color χ specified by $\langle cmd \rangle$ so that the next \begin{paracol} \paracol} will let γ_0^c have the coloring \special for χ . If we are in a paracol environment but in a column $c' \neq c$, on the other hand, we also let $\hat{\gamma}_0 = \chi$ but in addition let $\gamma_0^c = \text{pcol@columncolor@box} \cdot c$ have the coloring \special for χ immediately so that it is effective in the next column-switching to c. This immediate setting of γ_0^c is done by invoking $\langle cmd \rangle$ with the original \set@color saved in \pcol@set@color and the nullification of \aftergroup, after acquiring an \insert for it if necessary,

Otherwise, i.e., if we are in a paracol environment and in the column c, at first we invoke $\col@scancst@shadow$ to rewind $\hat{\varGamma}^c$ applying $\col@elt=\reset@color$ to $\hat{\gamma}_i\in\hat{\varGamma}^c$. Then, after letting $\hat{\gamma}_0^c=\chi$, we invoke $\col@scancst@shadow$ again to reestablish $\hat{\varGamma}^c$ with the new $\hat{\gamma}_0^c$ so that $\hat{\gamma}_0^c$ is at the bottom of the color stack in .tex. In this scan $\color color color$ to let it have $\hat{\gamma}_i$ and then invokes $\col@eltcolor$ to put the coloring $\scalectolor color color$

The macro \pcol@iicolumncolor $\langle cmd\rangle\langle c\rangle$ at first invokes $\langle cmd\rangle$ to let \current@color have the printer-specific color information χ of $\langle color\rangle$ or what \normalcolor specifies, temporarily letting \set@color be \relax to let \color or \normalcolor just do the \definition of \current@color without putting coloring \specials nor preparing color stack popping. Then we \xdefine $\hat{\gamma}_0^c = \text{pcol@columncolor} \cdot c$ to have χ .

The macro \pcol@scancst@shadow applies \@elt to $\hat{\gamma}_0^c$ to put a coloring or uncoloring \special for it if it is defined, and then do the same for all $\hat{\gamma}_i \in \hat{\Gamma} = \pcol@colorstack@shadow$.

```
2666 \def\pcol@icolumncolor#1[#2]{%
2667
      \@tempswafalse
2668
      \ifpcol@inner \@tempswatrue \fi
2669
      \ifinner
                     \@tempswatrue \fi
      \ifmmode
                     \@tempswatrue \fi
2670
      \ifx\set@color\relax
2671
2672
        \PackageWarning{paracol}{\pcol@colorcommand\space is not effective
2673
          without some coloring package}%
2674
      \else\if@tempswa
        \PackageWarning{paracol}{\pcol@colorcommand\space is not effective
2675
2676
          when not in outer par mode}%
2677
      \else
2678
        \begingroup
        \let\@elt\relax
2679
        \ifx\pcol@paracol\paracol
2680
          \pcol@iicolumncolor{#1}{#2}%
2681
        \else\ifnum#2=\pcol@currcol
2682
          \def\@elt##1{\reset@color}\pcol@scancst@shadow
2683
2684
          \pcol@iicolumncolor{#1}{#2}%
          \def\@elt##1{\def\current@color{##1}\let\aftergroup\@gobble
2685
            \pcol@set@color}%
2686
2687
          \pcol@scancst@shadow
          \setbox\@tempboxa\vbox{\let\set@color\pcol@set@color
2688
            \let\aftergroup\@gobble #1}%
2689
          \ht\@tempboxa1sp \dp\@tempboxa1sp \wd\@tempboxa\z@\relax
2690
          \insert\pcol@colorins{\box\@tempboxa}%
2691
2692
          \ifvmode\if@nobreak \nobreak \fi\fi
```

```
\else
2693
          \pcol@iicolumncolor{#1}{#2}%
2694
          \pcol@currcol#2\relax
2695
          \ifvoid\pcol@ccuse{@box}%
2696
            \@next\@currbox\@freelist{}\pcol@ovf
2697
            \pcol@ccxdef{\@currbox}%
2698
2699
           \global\setbox\pcol@ccuse{@box}\vbox{\let\set@color\pcol@set@color
2700
2701
            \let\aftergroup\@gobble #1}%
2702
        \fi\fi
        \endgroup
2703
      \fi\fi
2704
2705
      \ignorespaces}
2706 \def\pcol@iicolumncolor#1#2{{\let\set@color\relax #1%
      \expandafter\xdef\csname pcol@columncolor#2\endcsname{\current@color}}}
2707
2708 \def\pcol@scancst@shadow{%
      \pcol@ifccdefined{\@elt{\pcol@ccuse{}}}\relax
2709
2710
      \pcol@colorstack@shadow}
2711
```

\pcol@mcpushlimit
\set@color
\pcol@set@color
\pcol@set@color@push

The macro \pcol@set@color@push is invoked whenever IATEX's counterpart \set@color appears in a paracol environment through coloring commands such as \color, because \pcol@zparacol replaces IATEX's macro with it saving the original version in \pcol@set@color, if the original \set@color is not \relax to mean some coloring package is in use. This original version is used through \pcol@set@color by \pcol@bg@paintregion@i, \pcol@output@start and \pcol@icolumncolor besides this macro \pcol@set@color@push, while \output lets \set@color = \pcol@set@color for the references outside of our control.

The macro at first invokes its original version being $\col@set@color$ to put an appropriate coloring \special to .dvi and reserve the invocation of \special color by \aftergroup . Then, it performs one of two different operations depending on TeX's mode, i.e., math mode or not. If we are in math mode and not in a \box{vbox} , at first we increment $m = \pcol@mcid$ and examine if $m > \pcol@mcpushlimit = 1000$, and if so we stop the execution with $\pcol@mcid$ and examine order to avoid too many macros $\pcol@reset@color@mpop@\cdot m$ are defined .Otherwise, i.e., if $m \le \pcol@mcpushlimit$, we reserve the invocation of the macro $\pcol@reset@color@mpop@\cdot i$ for our own pop by \aftergroup defining the macro as $\pcol@reset@color@mpop{m}$. If we are not in math mode, on the other hand, and neither in a $\pcol@reset@color@mpop{m}$. If we are not in math mode, on the other hand, and neither in a $\pcol@reset@color@mpop{m}$ reserve the invocation of the macro .

Then, regardless that we are in math mode or not, we push the contents of \current@color, which \set@color should refer to as the color information to be set, into the shadow color stack $\hat{\Gamma} = \pcol@colorstack@shadow$ for the stack rewinding/reestablishing in \columncolor and \normalcolumncolor. Since this push is done non-\globally with \edef, we save/restore the definition of \@elt to/from \pcol@elt@save before/after the push, resepctively²³⁴. Then we \insert a \vbox through \pcol@colorins for the push of γ_i or $\gamma_{i,m}$ to Γ_r synchronous with a page break or column-switching. The height of the \vbox is 1 pt, depth is 0 and width is m sp if we are in math mode or 0 otherwise, and its contents is the coloring \special given by \pcol@set@color so that the \special is what the macro put at the beginning of this macro but

 $^{^{232}}$ And let m=1 to allow a user to continue the execution bravely.

 $^{^{233}}$ We could make the number of math-mode coloring operations virtually unlimited by putting all digits of the decimal representation of m followed by a terminator by multiple \aftergroups so that \pcol@reset@color@mpop is put by \aftergroup prior to them to capture them as its argument, but limiting with $2^{31}-1$ is still necessary and that with 1000 is reasonable.

 $^{^{234}}$ Just in case.

without the reservation of \reset@color. After the insertion, we put \pcol@fcwhyphenate, being \hskip\z@ when \coloredwordhyphenated is effective, to split the coloring \special from the first colored word so that the word may be hyphenated if we are in horizontal mode. If we are in vertical mode, on the other hand, we do \nobreak if \if@nobreak = true to keep the \insertion from being followed by a page break.

```
2712 \def\pcol@mcpushlimit{1000}
2713 \def\pcol@set@color@push{\pcol@set@color
2714
      \ifmmode\else\ifinner \pcol@innertrue \fi\fi
2715
      \ifpcol@inner\else
2716
        \ifmmode
          \global\advance\pcol@mcid\@ne
2717
          \ifnum \pcol@mcid>\pcol@mcpushlimit\relax
2718
            \PackageError{paracol}{Too many coloring commands in math mode}\Qehb
2719
2720
            \global\pcol@mdid\@ne
          \fi
2721
          \@tempdima\pcol@mcid sp\relax
2722
2723
          \expandafter\aftergroup
            \csname pcol@reset@color@mpop@\number\pcol@mcid\endcsname
2724
2725
          \expandafter\xdef
2726
            \csname pcol@reset@color@mpop@\number\pcol@mcid\endcsname
2727
              {\noexpand\pcol@reset@color@mpop{\number\pcol@mcid}}%
        \else
2729
          \aftergroup\pcol@reset@color@pop \@tempdima\z@
2730
        \fi
2731
        \let\pcol@elt@save\@elt \let\@elt\relax
2732
        \edef\pcol@colorstack@shadow{\pcol@colorstack@shadow\@elt{\current@color}}%
2733
        \let\@elt\pcol@elt@save
        \setbox\@tempboxa\vbox{\let\aftergroup\@gobble \pcol@set@color}%
2734
        \ht\@tempboxa1sp \dp\@tempboxa\z@ \wd\@tempboxa\@tempdima
2735
        \insert\pcol@colorins{\box\@tempboxa}\ifhmode \pcol@fcwhyphenate \fi
2736
2737
        \ifvmode\if@nobreak \nobreak \fi\fi
2738
      \fi}
```

\pcol@reset@color@pop \pcol@reset@color@mpop The macro \pcol@reset@color@pop and its math-mode relative \pcol@reset@color@mpop $\{m\}$ are invoked by \aftergroup mechanism in \pcol@set@color@push, directly for the former and through the macro \pcol@reset@color@mpop@·m for the latter. They \insert a \vbox for γ_i^- or $\gamma_{i,m}^-$ to add it to Γ_r synchronously with a page break or column-switching. Therefore, the height and depth of the \vbox are 0 and width is 0 for γ_i^- or m sp for $\gamma_{i,m}^-$. The contents of the \vbox is an uncoloring \special given by \reset@color but this is done just for debugging to show what \pcol@colorins has by, for example, \pcol@ShowBox. Then if we are in vertical mode and \if@nobreak = true, we do \nobreak to keep the \insertion from being followed by a page break even in \pcol@reset@color@mpop because its corresponding \pcol@set@color@push may have been in a displayed math construct after which we are in vertical mode.

One caution is that $\coloreset@color@pop$ can be invoked outside the paracol environment in which the corresponding $\coloreset@color@push$ appears. In this case with $\coloreset@color@push$ appears. In this case with $\coloreset@color@push$ appears and cannot make the $\coloreset@coloreset@color@push$ appears. In this case with $\coloreset@color@push$ appears.

```
2740 \def\pcol@reset@color@pop{%
2741 \ifpcol@output
2742 \setbox\@tempboxa\vbox{\reset@color}%
2743 \ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa\z@
```

```
2744 \insert\pcol@colorins{\box\@tempboxa}%
2745 \ifvmode\if@nobreak \nobreak \fi\fi
2746 \fi}
2747 \def\pcol@reset@color@mpop#1{%
2748 \setbox\@tempboxa\vbox{\reset@color}%
2749 \ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa#1sp\relax
2750 \insert\pcol@colorins{\box\@tempboxa}%
2751 \ifvmode\if@nobreak \nobreak \fi\fi
2752 }
2753
```

\coloredwordhyphenated \nocoloredwordhyphenated \pcol@fcwhyphenate The API macro \coloredwordhyphenated \defines the macro \pcol@fcwhyphenate being \hskip\z@ so that the null space is inserted after the coloring \special and \insert put by \pcol@set@color@push if we are in horizontal mode, so that the word following them can be hyphenated. The other API macro \nocoloredwordhyphenated makes \pcol@fcwhyphenate = \relax to inhibit the insertion. Since the null skip is a line break candidate, the skip might cause an unexpected and undesirable line break. However, this demerit is less important than the merit of making it possible to hyphenate the first word in multi-column documents with narrow lines, and thus we make \coloredwordhyphenated effective in default while giving users a means to disable the insertion (occasionally) by \nocoloredwordhyphenated.

```
2754 \def\coloredwordhyphenated{\def\pcol@fcwhyphenate{\hskip\z@}}
2755 \def\nocoloredwordhyphenated{\let\pcol@fcwhyphenate\relax}
2756 \coloredwordhyphenated
2757
```

22 Commands for Column-Separating Rule Color and Background Painting

\colseprulecolor
\pcol@defcseprulecolor@x
\pcol@defcseprulecolor
\pcol@defcseprulecolor
\normalcolseprulecolor@i
\pcol@colseprulecolor

The macro \colseprulecolor[mode] $\{color\}[c]$ \defines \pcol@colseprulecolor to have the $\langle color \rangle$ optionally with coloring $\langle mode \rangle$ of all column-separating rules if the optional argument c is not provided, or \pcol@colseprulecolor·c that of the rule drawn between a particular column pair c and c+1. After \defining \pcol@colorcommand to be \colseprulecolor in case we have to give a warning, the macro invokes \pcol@defcseprulecolor@x[mode] $\{color\}$ or \pcol@defcseprulecolor@y $\{color\}$ according to the provision of the optional argument $\langle mode \rangle$ to invoke \pcol@defcseprulecolor with argument $\{cmd\} = \text{color}[mode]\{color\}$ so that this macro invokes \pcol@defcseprulecolor@i $\{cmd\}[c]$ where $c = \emptyset$ if the optional argument c is not provided.

The macro \normalcolseprulecolor[c], on the other hand, defines \pcol@colseprule color[$\cdot c$] with whatever \normalcolor gives, and thus it invokes \pcol@defcseprulecolor@i letting $\langle cmd \rangle =$ \normalcolor, after \defining \pcol@colorcommand to be \normalcolsep rulecolor.

The macro \pcol@defcseprulecolor@i{cmd}[c] examines if \set@color = \relax to mean no coloring packages have been loaded and, if so, do nothing giving a warning the command in \pcol@colorcommand is not effective. Otherwise, we examine if $\langle cmd \rangle$ has proper arguments by invoking it but temporally nullifying \set@color and then \define \pcol@colseprulecolor[$\cdot c$] to be $\langle cmd \rangle$.

Note that at the top level we $\ensuremath{\texttt{define pcol@colseprulecolor}}$ to be $\ensuremath{\texttt{normalcolor}}$ to give the default for all column-separating rules. Also note that macros $\ensuremath{\texttt{pcol@colseprulecolor}}$.

are referred to solely in $\prol@colseprulecolor$ for columns for which $\prol@colseprulecolor \cdot c$ is not defined.

```
2758 %% Commands for Column-Separating Rule Color and Background Painting
2759
2760 \def\colseprulecolor{\def\pcol@colorcommand{\string\colseprulecolor}%
2761
      \@ifnextchar[%]
        \pcol@defcseprulecolor@x\pcol@defcseprulecolor@y}
2762
2763 \def\pcol@defcseprulecolor@x[#1]#2{\pcol@defcseprulecolor{\color[#1]{#2}}}
2764 \def\pcol@defcseprulecolor@y#1{\pcol@defcseprulecolor{\color{#1}}}
2765 \def\pcol@defcseprulecolor#1{\@ifnextchar[%]
      {\pcol@defcseprulecolor@i{#1}}{\pcol@defcseprulecolor@i{#1}[]}}
2767 \def\normalcolseprulecolor{%
2768
      \def\pcol@colorcommand{\string\normalcolseprulecolor}%
2769
      \@ifnextchar[%]
        {\pcol@defcseprulecolor@i\normalcolor}%
2770
        {\pcol@defcseprulecolor@i\normalcolor[]}}
2771
2772 \def\pcol@defcseprulecolor@i#1[#2]{%
      \ifx\set@color\relax
        \PackageWarning{paracol}{\pcol@colorcommand\space is not effective
2774
2775
          without some coloring package}%
2776
        {\let\set@color\relax #1}%
2777
        \global\@namedef{pcol@colseprulecolor#2}{#1}%
2778
2779
2780 \gdef\pcol@colseprulecolor{\normalcolor}
```

\backgroundcolor
\nobackgroundcolor
\pcol@backgroundcolor@e
\pcol@backgroundcolor@i
\pcol@backgroundcolor@ii
\pcol@backgroundcolor@iii
\pcol@backgroundcolor@iv
\pcol@backgroundcolor@iv

The macro \backgroundcolor{region} [mode] {color} defines the $\langle color \rangle$ optionally with $\langle mode \rangle$ of the $\langle region \rangle$ whose syntax is specified as follows.

```
\begin{split} \langle region \rangle &::= \langle regionid \rangle \langle extension \rangle \\ \langle regionid \rangle &::= \langle a \rangle \mid \langle corg \rangle \, [c] \\ & \langle a \rangle ::= \langle corg \rangle \mid \texttt{s} \mid \texttt{S} \mid \texttt{t} \mid \texttt{T} \mid \texttt{1} \mid \texttt{L} \mid \texttt{r} \mid \texttt{R} \mid \texttt{f} \mid \texttt{F} \mid \texttt{n} \mid \texttt{N} \mid \texttt{p} \mid \texttt{P} \\ & \langle corg \rangle ::= \texttt{c} \mid \texttt{C} \mid \texttt{g} \mid \texttt{G} \\ \langle extension \rangle ::= \emptyset \mid (x_0\,,y_0) \mid (x_0\,,y_0)\, (x_1\,,y_1) \end{split}
```

On the other hand, the counteraprt macro \nobackgroundcolor{region} undefines the color of $\langle region \rangle$. Both macros invoke \pcol@backgroundcolor giving all arguments to it to parse the argument $\langle region \rangle$, after letting $f_{def} = \if@tempswa = true$ and \pcol@backgroundcolor@e = \pcol@backgroundcolor@w in \backgroundcolor, or $f_{def} = \if@tempswa = true$ and \pcol@backgroundcolor@e = \pcol@backgroundcolor@z in \nobackgroundcolor. Note that the \let-assignment to \pcol@backgroundcolor@e is effective when we found an error in the parse of the argument $\langle region \rangle$ to throw away what remains in the argument unprocessed and, for \backgroundcolor, the other arguments $[mode] \{color\}$.

Then the macro \pcol@backgroundcolor examines if \pcol@bg@@·a is defined, and if not, raises an error that a is invalid and then, in case the user dare to continue the execution, invokes \pcol@backgroundcolor@e to throw all arguments away after letting a' = pcol@bg@region = xx so that the undefining \pcol@bg@color·a' does not cause any troubles. Otherwise, i.e., if \pcol@bg@@·a is defined, it invokes \pcol@backgroundcolor@i[c] or \pcol@backgroundcolor@ii according to the provision of the optional argument [c], after \defining a' = pcol@bg@region to be a. Then \pcol@backgroundcolor@i examines

if $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colored{colored}$ is defined, and if not, raises are error again in a similar way, or otherwise invokes $\colored{colored}$

Then if $f_{def} = true$, the macro \pcol@backgroundcolor@ii examines if \set@color = \relax, and if so it complains that any coloring packages have not been loaded and invokes \pcol@backgroundcolor@w just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ iii after adding a' to the tail of \pcol@bg@defined. On the other hand if $f_{def} = false$, it invokes \pcol@backgroundcolor@z without checking the availability of coloring macros.

The macro \pcol@backgroundcolor@iii at first invokes \pcol@bg@defext{d}{e} with e=0 for all $d\in\{1,r,t,b\}$ to have default (no) extensions. Then if (x_0,y_0) is provided, \pcol@bg@defext is invoked again by \pcol@backgroundcolor@iv for all $d\in\{1,r,t,b\}$ but with $e=x_0$ for $d\in\{1,r\}$ and with $e=y_0$ for $d\in\{t,b\}$. Further, if (x_1,y_1) is also provided, \pcol@bg@defext is invoked once again by \pcol@backgroundcolor@v for all $(d,e)\in\{(r,x_1),(b,y_1)\}$. Finally \pcol@backgroundcolor@v invokes \pcol@backgroundcolor@x, which is also invoked from \pcol@backgroundcolor@iii and \pcol@backgroundcolor@iv if they find no (further) extensions.

```
2782 \def\backgroundcolor#1{\@tempswatrue
      \let\pcol@backgroundcolor@e\pcol@backgroundcolor@w
2783
      \pcol@backgroundcolor#1\@nil}
2784
2785 \def\nobackgroundcolor#1{\@tempswafalse
      \let\pcol@backgroundcolor@e\pcol@backgroundcolor@z
      \pcol@backgroundcolor#1\@nil}
2788 \def\pcol@backgroundcolor#1{%
2789
      \@ifundefined{pcol@bg@@#1}%
2790
        {\PackageError{paracol}%
           {Invalid background coloring region identifier #1}%
2791
2792
         \def\pcol@bg@region{xx}\pcol@backgroundcolor@e}%
2793
        {\def\pcol@bg@region{#1}%
         \@ifnextchar[%]
2794
           \pcol@backgroundcolor@i \pcol@backgroundcolor@ii}}
2795
2796 \def\pcol@backgroundcolor@i[#1]{%
      \@ifundefined{pcol@bg@mayhavecol@\pcol@bg@region}%
        {\PackageError{paracol}%
2798
           {Column number \number#1 is not effective for background coloring region
2799
2800
            \pcol@bg@region}%
2801
         \def\pcol@bg@region{xx}\pcol@backgroundcolor@e}%
2802
        {\edef\pcol@bg@region{\pcol@bg@region @#1}%
2803
         \pcol@backgroundcolor@ii}}
2804 \def\pcol@backgroundcolor@ii{%
      \if@tempswa
2805
2806
        \ifx\set@color\relax
2807
          \PackageWarning{paracol}{\string\backgroundcolor\space is not effective
            without some coloring package}%
2808
          \let\reserved@b\pcol@backgroundcolor@w
2809
2810
        \else
2811
          \let\reserved@b\pcol@backgroundcolor@iii
2812
          \@cons\pcol@bg@defined{{\pcol@bg@region}}%
        \fi
2813
2814
      \else
        \let\reserved@b\pcol@backgroundcolor@z
2815
2816
      \reserved@b}
2817
```

```
2818 \def\pcol@backgroundcolor@iii{%
      \pcol@bg@defext{1}\z@ \pcol@bg@defext{r}\z@
      \pcol@bg@defext{t}\z@ \pcol@bg@defext{b}\z@
2820
      \@ifnextchar(%)
2821
        \pcol@backgroundcolor@iv \pcol@backgroundcolor@x}
2822
2823 \def\pcol@backgroundcolor@iv(#1,#2){%
      \pcol@bg@defext{1}{#1}\pcol@bg@defext{r}{#1}%
      \pcol@bg@defext{t}{#2}\pcol@bg@defext{b}{#2}%
2825
2826
      \@ifnextchar(%)
        \pcol@backgroundcolor@v \pcol@backgroundcolor@x}
2827
2828 \def\pcol@backgroundcolor@v(#1,#2){%
      \pcol@bg@defext{r}{#1}\pcol@bg@defext{b}{#2}%
2829
      \pcol@backgroundcolor@x}
```

\pcol@backgroundcolor@x \pcol@backgroundcolor@y The macro $\pol@backgroundcolor@x$ is used in $\pol@backgroundcolor@iii$, $\pol@backgroundcolor@v$ to define the color for background painting of the region $a' = \pol@bg@region$. Since the macro is followed by the arguments $[mode]\{color\}$ of $\pol@backgroundcolor$, the macro invokes \color to let it $\color=\pol@backgroundcolor@y$. Therefore $\pol@backgroundcolor@y$ is invoked in \color and it $\pol@backgroundcolor@v$ to let it have whatever $\color=\pol@backgroundcolor$ has.

```
2831 \def\pcol@backgroundcolor@x#1\@nil{\begingroup
2832 \let\set@color\pcol@backgroundcolor@y \color}
2833 \def\pcol@backgroundcolor@y{%
2834 \expandafter\xdef\csname pcol@bg@color@\pcol@bg@region\endcsname
2835 {\current@color}%
2836 \endgroup}
```

\pcol@backgroundcolor@z \pcol@backgroundcolor@w \pcol@backgroundcolor@wi \pcol@bg@color@xx The macro \pcol@backgroundcolor@z is invoked from \pcol@backgroundcolor@ii directly to work for \nobackgroundcolor to disable the background painting for a region $a' = \pcol@bg@region$, or from \pcol@backgroundcolor and \pcol@backgroundcolor@i through \pcol@backgroundcolor@e when they find an error in the argument $\langle region \rangle$ of \nobackgroundcolor. Similarly the macro \pcol@backgroundcolor@w is invoked from \pcol@backgroundcolor@ii directly when it finds no coloring packages have not been loaded, or \pcol@backgroundcolor@i through \pcol@backgroundcolor@e on error too but in the argument of \backgroundcolor@i through \pcol@backgroundcolor@e on error too but in the argument of \backgroundcolor. Both macros throw away whatever remains in $\langle region \rangle$ unprocessed and then invoke \pcol@backgroundcolor@wi, but \pcol@backgroundcolor@z gives it a dummy argument pair, while \pcol@backgroundcolor@w passes $[mode]\{color\}$ to it.

Then $\color@vi$ throw all arguments away and lets $\color@color@color@·a' = \color@vi the region <math>a'$ is untouched in background painting macros. Note that since a' = xx being an absolutely non-exsistent region when this macro is used for error recovery, undefining is not harmful.

```
2837 \def\pcol@backgroundcolor@z#1\@ni1{\pcol@backgroundcolor@wi[]{}}
2838 \def\pcol@backgroundcolor@w#1\@ni1{\@ifnextchar[%]}
2839 \pcol@backgroundcolor@wi{\pcol@backgroundcolor@wi[]}}
2840 \def\pcol@backgroundcolor@wi[#1]#2{%}
2841 \expandafter\global\expandafter\let
2842 \csname pcol@bg@color@\pcol@bg@region\endcsname\relax}
2843
```

\pcol@bg@mayhavecol@C \pcol@bg@mayhavecol@C \pcol@bg@mayhavecol@g \pcol@bg@mayhavecol@G

```
2844 \def\pcol@bg@mayhavecol@c{}
2845 \def\pcol@bg@mayhavecol@C{}
2846 \def\pcol@bg@mayhavecol@g{}
2847 \def\pcol@bg@mayhavecol@G{}
```

\pcol@bg@defext

The macro \pcol@bg@defext{d}{e} is used by \pcol@backgroundcolor@iii, \pcol@backgroundcolor@iv and \pcol@backgroundcolor@v to \define \pcol@bg@ext@·d·@·a' be e=0 for all $d \in \{1, r, t, b\}$ in the first, be $e=x_0$ for $d \in \{1, r\}$ and $e=y_0$ for $d \in \{t, b\}$ in the second, and be $e=x_0$, x_1 , y_0 and y_1 for d being 1, r, t, b respectively in the last. The macro at first lets \@tempdima have e to confirm e is a proper dimension and then \xdefines \pcol@bg@ext@·d·@·a' to let it have the integer representation of e followed by sp.

```
2849 \def\pcol@bg@defext#1#2{%

2850 \@tempdima#2\relax

2851 \expandafter\xdef\csname pcol@bg@ext@#1@\pcol@bg@region\endcsname{%

2852 \number\@tempdima sp}}

2853
```

\resetbackgroundcolor \pcol@resetbackgroundcolor \pcol@bg@defined

```
2854 \def\resetbackgroundcolor{{%
2855 \let\Qelt\pcol@resetbackgroundcolor \pcol@bg@defined
2856 \gdef\pcol@bgdefined{}}}
2857 \def\pcol@resetbackgroundcolor#1{%
2858 \expandafter\global\expandafter\let\csname pcol@bg@color@#1\endcsname\relax}
2859 \gdef\pcol@bg@defined{}
2860
```

23 Closing Environment

\endparacol \pcol@lastcol The macro \endparacol is invoked from \end{paracol} to close paracol environment. After making it sure to be in vertical mode by \pcol@par, we switch to the column 0 by \pcol@ switchcol to let local counter have the values for the column 0 so that they are referred to outside the environment, after saving the current column c in \pcol@lastcol to be referred to in \pcol@output@end so that $\kappa_c(\sigma)$ and $\kappa_c(\varepsilon)$ are passed to post-environment stuff.

Then we invoke \pcol@flushclear for pre-flushing column height check, turning \ifpcol@lastpage = true to tell \pcol@output@switch for the check that it works on the last page, and giving \bot to \pcol@flushclear as its argument, unless footnote typesetting is page-wise but not merged for which we give Φ to ensure all deferred footnotes are put in the checking process. Note that the argument for column-wise footnote typesetting is Φ but it is

definitely \bot in this mode. After that we make an \output request by \pcol@invokeoutput with \penalty = \pcol@op@end and still with \ifpcol@lastpage = true to build the last page.

Next, we let $\columnwidth = \text{textwidth}$ and $\column = false$ for single-column typesetting, and also let $\column = \color =$

```
2861 %% Closing Environment
2862
2863 \def\endparacol{\pcol@par
      \edef\pcol@lastcol{\number\pcol@currcol}%
2864
      \pcol@nextcol\z@ \pcol@switchcol
2865
      \pcol@lastpagetrue
2866
      \ifpcol@mgfnote \pcol@flushclear\voidb@x
2867
      \else \pcol@flushclear\pcol@topfnotes
2868
2869
2870
      \pcol@invokeoutput\pcol@op@end
2871
      \global\columnwidth\textwidth
      \global\@twocolumnfalse
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      \ifpcol@fncounteradjustment
2874
2875
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        \global\advance\c@footnote\pcol@nfootnotes
2876
2877
2878
```

\pcol@restoreeveryvbox

The macro \pcol@restoreeveryvbox is invoked just after \end{paracol} by \aftergroup mechanism activated by \pcol@zparacol. It examines if \pcol@everyvbox has tokens different from \pcol@dummytoken which \pcol@zparacol \globally assigned to the register. Since the dummy token cannot be assigned to \everyvbox²³⁵, the difference means the \everyvbox has been \globally updated with the value that \pcol@everyvbox has now. Therefore if so, we globally update \everyvbox with \pcol@everyvbox to refrect the global update in the environment.

```
2879 \def\pcol@restoreeveryvbox{%
2880 \expandafter\def\expandafter\reserved@a\expandafter{\the\pcol@everyvbox}%
2881 \def\reserved@b{\pcol@dummytoken}%
2882 \ifx\reserved@a\reserved@b\else \global\everyvbox\pcol@everyvbox \fi}
```

 $[\]overline{\ \ \ \ }^{235}$ Unless a very surprising coincidence happens or a user intentionally violates the coherence of the implementation.

Acknowledgments

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For the implementation of the style file, the author referred to the base implementations of Voutput and othe many macros of $\text{ETEX} 2_{\varepsilon}$ written by Leslie Lamport, Johannes Braams and other authors. The author also referred to color written by David Carlisle and marginnote written by Markus Kohm to make the package working well with them.

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Revision History

0.9	
General: The style paracol is born. (2005/01/28)	. 1
0.91	
General: The style is included in CTAN with a very small modification. $(2011/09/16)$. 1
1.0	
General: Add this document and fix the following problems on the author's 30th wedding	
anniversary. $(2011/10/10)$	
\pcol@toppage: Renamed from \pcol@maxpage	. 130
\ifpcol@nospan: Renamed from \pcol@textonly	
\ifpcol@sync: Add initialization to be false	. 131
\ifpcol@sptext: Introduced to restrict the broadcast of \if@nobreak and \everypar only	
when a column-switching is accompanied with spanning text	
\ifpcol@clear: Add initialization to be false	
\ifpcol@outputflt: Renamed from \ifpcol@stopoutput with the reversal	
\ifpcol@lastpage: Introduced for special operations in the last page	
\pcol@textfloatsep: Introduced for the bug fix of float space enlargement	. 137
\pcol@output: Replace \@makecol with \pcol@makecol for a special care for column-pages	
with synchronization points.	143
\pcol@makecol: Introduced for special float handling in a column-page with synchronization	
points.	145
\pcol@combinefloats: Introduced for special float handling in a column-page with	
synchronization points	146
\pcol@cflt: Introduced for special float handling in a column-page with synchronization	
points.	
\pcol@opcol: Remove unnecessary assignment of \@colht	
\pcol@opcol: Rename \pcol@maxpage as \pcol@toppage	
\pcol@setpnoelt: Rename \ifpcol@textonly as \ifpcol@nospan	
\pcol@getpinfo: Rename \ifpcol@textonly as \ifpcol@nospan	
\pcol@floatplacement: Add initialization of \pcol@textfloatsep	
\pcol@startpage: Add assignment of \pcol@firstprevdepth to be \relax	
\pcol@startpage: Rename \pcol@maxpage as \pcol@toppage	
\pcol@startpage: Rename \pcol@settextpage as \pcol@setordpage	
\pcol@outputcolumns: Rename \ifpcol@stopoutput as \ifpcol@outputflt	
\pcol@outputelt: Rename \ifpcol@stopoutput as \ifpcol@outputflt	
\pcol@outputelt: Rename \ifpcol@textonly as \ifpcol@nospan	
\pcol@specialoutput: Remove unnecessary \pcol@latex@specialoutput	
\pcol@output@start: Change the order of operations	
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	colorstack: Introduced to reestablish color context	
	est: Introduced to reestablish color context	
	prstack: Introduced to reestablish color context	
	colorstack@full was introduced to represent Γ^c but removed in v1.34 1	
	end: Add color resetting	
	.: Add redefinitions of \set@color and \reset@color	
· ·	Introduced to define the default color of a column	
	color: Introduced to implement \columncolor	
	color: Introduced to implement \columncolor	
	plor: Introduced to implement \columncolor	
	color: Introduced to define the default color of a column is \normalcolor 2	
	color: Introduced to implement \columncolor and \normalcolumncolor 2	
_	or@push: Introduced to work as \set@color	
_	plor@pop: Introduced to work as \reset@color 2	162
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	age-wise and merged footnote functions. (2013/05/11)	
	footnote mentioning page-wise footnotes	
	01 0	15
	010	15
	ne sub-section "Single-Columned Footnotes" to describe newly introducerd	0.4
	Troping and the second	24
	ne section "Numbering and Placement of Single-Columned Footnotes" to	00
1 0		30
		66
	9	68
	ebase: Introduced for page-wise footnotes	
	es: Introduced for page-wise footnotes	
	Add \pcol@switchcol and \pcol@flushclear to the macros turning the switch	
		.31
_	Add \pcol@flushclear to the macros turning the switch true due to the	a -
pre-flushing	column height check	.32

\ifpcol@flush: Add uses for page-wise footnote functions.	
\ifpcol@scfnote: Introduced for page-wise footnote functions.	
\ifpcol@mgfnote: Introduced for page-wise footnote functions	
\ifpcol@fncounteradjustment: Introduced for page-wise footnote functions	
\pcol@topfnotes: Introduced for page-wise footnote functions	
\pcol@ShowBox: Introduced for debugging page-wise footnote functions	
\pcol@LogLevel: Introduced for debugging page-wise footnote functions	
\pcol@iLogLevel: Introduced for debugging page-wise footnote functions	
\pcol@Log: Introduced for debugging page-wise footnote functions.	
\pcol@Log@iii: Introduced for debugging page-wise footnote functions	
\pcol@Log@ii: Introduced for debugging page-wise footnote functions	
\pcol@Log@i: Introduced for debugging page-wise footnote functions	
\pcol@Logstart: Introduced for debugging page-wise footnote functions	
\pcol@Logstart@ii: Introduced for debugging page-wise footnote functions	
\pcol@Logstart@i: Introduced for debugging page-wise footnote functions	
\pcol@Logend: Introduced for debugging page-wise footnote functions	
\pcol@Logend@ii: Introduced for debugging page-wise footnote functions	
\pcol@Logend@i: Introduced for debugging page-wise footnote functions	
\pcol@Logfn: Introduced for debugging page-wise footnote functions	
\pcol@Logfn@ii: Introduced for debugging page-wise footnote functions	
\pcol@Logfn@i: Introduced for debugging page-wise footnote functions	
\pcol@output: Add \pcol@Logstart and \pcol@Logend	143
\pcol@output: Add an argument \@ne to \pcol@startcolumn to distinguish it from the	
invocation in \pcol@freshpage	
\pcol@makecol: Add save/discard of page-wise footnotes	
\pcol@combinefloats: Remove the shrink of \textfloatsep because each column in the last	
page is now made not taller than \@colht definitely by the introduction of the pre-flushing	
column height check	
\pcol@setpnoelt: Completely recode reflecting the redesign of page context	149
\pcol@defcurrpage: Introduced by the redesign of page context, partly replacing	
\pcol@setordpage which once we call \pcol@settextpage	
\pcol@nextpelt: Revise reflecting the redesign of page context	
\pcol@getpelt: Revise reflecting the redesign of page context	
\pcol@getpinfo: Revise reflecting the redesign of page context	
\pcol@getcurrpinfo: Revise reflecting the redesign of page context	
\pcol@startpage: Revise reflecting the redesign of page context	
\pcol@outputelt: Revise reflecting the redesign of page context	
\pcol@outputelt: Add ship-out of page-wise footnote	
\pcol@trynextcolumn: No change in the code itself but its explanation is modified according to	
the drastic redesign of \pcol@startcolumn	
$\label{loging} $$ \operatorname{loging if \operatorname{logth}} = -10004. \ldots .$	174
$\protect\$ Add initialization of Φ and page-wise footnote output operations, and	
0 0 1 0	174
\pcol@output@start: Add insertion of \footins having footnotes to be merged if it is not	
	178
\pcol@makenormalcol: Replace the building operation of \@outputbox with footnotes with the	e.e
1 0	178
$\verb \pcol@output@switch : Add the case \verb \ifpcol@clear = \verb \ifpcol@sync = true for the invocation of the invocation of$	n
of \pcol@restartcolumn for pre-flushing column height check	182
\pcol@restartcolumn: Redesign the footnote insertion mechanism to cope with page-wise	
footnotes.	183
· •	186
General: Add the subsection "Footnote Handling" to describe newly introduced macros for	
name vijas faatnatas	100

\pcol@savefootins: Introduced to save footnotes in multiple occasions	192
\pcol@shrinkcolbyfn: Introduced to shrink \@colht temporarily by the height-plus-depth of	
page-wise footnotes and the natural size of the skip above them	192
\pcol@unvbox@cclv: Introduced to add stretch/shrink components of \skip\footins at the	
bottom of a column-page if the page has page-wise footnotes	192
\pcol@deferredfootins: Introduced to insert deferred footnotes	193
\pcol@combinefootins: Introduced to put footnotes into pre-environment stuff	193
\pcol@putfootins: Introduced to put page-wise footnotes to a page	193
\pcol@sync: Revise reflecting the redesign of page context	201
\pcol@sync: Add pre-flushing column height check taking page-wise footnotes into account.	201
\pcol@flushcolumn: Revise reflecting the redesign of \pcol@getcurrfoot	204
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\prol@flushcolumn: Add the examination of $\kappa_c(\rho) = \infty$ to cope with a rare-case interaction of	of
	204
\pcol@flushcolumn: Add \@colht shrinking by page-wise footnotes	206
\pcol@flushcolumn: Revise reflecting the redesign of page context	
\pcol@flushcolumn: Add \@colht shrinking by page-wise footnotes	
\pcol@makefcolumn: Encapsulate the float column in a \vbox of \@colht so that vertical skips	
at the top and bottom are not lost when the column is put back to the main vertical list,	
and makes the assignment to \@currbox global because the box is now referred to after	
	207
•	209
\pcol@synccolumn: Change code structure removing the case for overflown synchronized	
	211
\pcol@synccolumn: Remove \penalty-10000 made unnecessary by the redesign of overflow	
	211
\pcol@output@flush: Add \pcol@Logstart and \pcol@Logend	
\pcol@output@clear: Add \pcol@Logstart and \pcol@Logend	
\pcol@makeflushedpage: Revise reflecting the redesign of page context	
\pcol@makeflushedpage: Add \@colht shrinking by page-wise footnotes	
\pcol@makeflushedpage: Add incorporation of page-wise footnotes	
\pcol@imakeflushedpage: Revise reflecting the redesign of \pcol@getcurrfoot	
\pcol@freshpage: Add argument 0 for the invocations of \pcol@startcolumn to inhibit	
	221
\pcol@output@end: Add incorporation of page-wise footnotes in the last ordinary pages	221
	222
	225
	226
\pcol@zparacol: Add initialization of \pcol@footnotebase and \pcol@nfootnotes, and	220
redefinitions of \footnote, \footnotemark, \footnotetext and \@footnotetext	231
\pcol@zparacol: Add nullification of API macros of footnote typesetting definition	
\pcol@ignore: Introduced for nullification of API macros of footnote typesetting definition	
\pcol@switchcol: Add column-scanning and page-overflow check for synchronized	232
	247
0	247
\pcol@visitallcols: Introduced for column-scanning in synchronized column-switching and	0.40
1 0 0	248
\pcol@flushclear: Introduced for column-scanning in synchronized column-switching and page	
flushing.	252
General: Add the subsection "Commands for Footnotes" to describe newly introduced macros	
1 0	253
\multicolumnfootnotes: Introduced to delclare the defalut column-wise footnote typesetting	253
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~	notes: Introduced to delclare the page-wise but non-merged footnote	
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	Introduced to delclare the page-wise and merged footnote type setting. . 2	
	oduced for footnote encapsulation and deferring.	
	ntroduced for footnote encapsulation	
	: Introduced for footnote encapsulation and deferring	
-	Introduced for footnote encapsulation and height capping	254
	ent: Introduced to make footnote counter is consistent with its origin at	
	paracol and the number of footnotes given in the environment at its	
		255
	tment: Introduced to disable the footnote counter adjustment	
	e: Introduced to keep the original definition of \footnoterule	
	ntroduced to keep the original definition of \footnote	
-	rk: Introduced to keep the original definition of \footnotemark	
	xt: Introduced to keep the original definition of \footnotetext	
	troduced for \footnote* and footnote counter adjustment	
	ntroduced for \footnote* and footnote counter adjustment	
	k: Introduced for \footnotemark* and footnote counter adjustment	
	${\tt rk}$: Introduced for ${\tt ar mark*}$ and footnote counter adjustment	
	: Introduced for \footnote* and \footnotemark*	
	r: Introduced for \footnote* and \footnotemark*	
	ntroduced for \footnote*, \footnotemark* and \footnotetext*	
	t: Introduced for \footnotetext*	
-	xt: Introduced for \footnotetext*	
	ext: Introduced for \footnotetext*	
-	ore-flushing column height check and footnote counter adjustment	267
1.2-3		
	lem in synchronization. (2013/05/11)	
	roduced to fix the problem with a too-tall page at synchronization	
	the action on the page overflow to return from \output without flushing so	
	broken outside \output to place top floats above the synchronization point	
	page	201
71.2-4	(2012/27/11)	_
	n-swapping functions. (2013/05/11)	
	ption of \[no] swapcolumninevenpages	
	bsection "Column-Swapping"	
	n: Introduced for column-swapping in even pages.	
	Add column-swapping for even pages if specified	
	dpage: Add column-swapping for even pages if specified	
	: Add column-swapping for even pages if specified	
	odify the setting of \if@firstcolumn according to column-swapping	
	dd nullificaion of \[no]swapcolumninevenpages	
	oduced for nullification of \[no]swapcolumninevenpages	
	\pcol@swapcolumn for column-swapping	
	Add \pcol@swapcolumn for column-swapping to turn \if@firstcolumn 2	247
	ction "Column-Swapping" to describe newly introduced macros for	~
	9	257
	pages: Introduced to enable column-swapping	
	enpages: Introduced to disable column-swapping	
	Introduced to convert column ordinal and its position	258
1.2-5	(2010/07/54)	_
	racol environment is enclosed in list-like environments. (2013/05/11) m to show that paracol can be enclosed in a list-like environment	
/1 1 A 1 1 · · ·		

	General: Modify the description about \linewidth reflecting the fact that paracol may be	20
	included in a list-like environment.	
	\pcol@lrmargin: Introduced to let \linewidth for each column has the value according to w_c	
	and the list-like environment surrounding paracol environment.	
	\pcol@getcurrcol: Move assignment w_c to \hsize and \linewidth to \pcol@invokeoutput.	
	\pcol@invokeoutput: Move the setting of \linewidth and \hsize from \pcol@getcurrcol to	
	this macro and add \parshape	226
	\pcol@zparacol: Remove the setting \columnwidth, \hsize and \linewidth because they are	9
	properly set in and after \pcol@output@start	229
	\pcol@zparacol: Add the setting of \pcol@lrmargin	229
	\pcol@sptext: Add setting of \columnwidth, \linewidth and \parshape to have indented	
	spanning text with surrounding list-like environments.	246
	\endparacol: Remove \global assignment of \hsize and \linewidth because assignments of	
	them in paracol are now perfectly local.	267
v1	.2-6	
	General: Add \localcounter. (2013/05/11)	. 1
	\localcounter: Introduced to remove the argument counter from Θ^g	
	\pcol@remctrelt: Recode to use newly introduced \pcol@removecounter	
	\pcol@removecounter: Introduced for the counter removal operation in \localcounter and	
	\pcol@remctrelt	242
	\pcol@iremctrelt: Add the first argument Θ' as the counter list from which the second	
		242
v1	.2-7	
	General: Bug fixes and minor revisions as follows. (2013/05/11)	. 1
	General: Remove \nosv from verbatim example of Table 1 shown in the right column	
	General: Correct a few words in German and English libretti.	
	General: Add the section "Known and Unknown Problems" to summarize a few typesetting	
	issues and warn users of the possiblity of bugs.	59
	\ifpcol@output: Introduced to solve the \output request sneaking	
	\ifpcol@lastpagesave: Introduced to fix the bug that \@makecol and \pcol@makefcolumn in	
		132
	\pcol@output: Add the examination of \ifpcol@output and LATEX's original sequence for	102
	\output request sneaked from outside of paracol environment	143
	\pcol@output: Add the assignment of \@maxdepth to \maxdepth to nullify the temproary	110
	setting done by \Qaddtobot.	143
	\pcol@makecol: Introduced to cope with the careless implementation of \@makecol in	110
	pLTFX	144
	\pcol@makecol: Remove unnecessary check of \ifpcol@lastpage on the redefinition of	144
	\Quad \Quad \Quad	145
	\pcol@combinefloats: Add the assignment of \@maxdepth to \maxdepth to nullify the	140
	temproary setting done by \@addtobot	146
	\pcol@Combinefloats: Introduced to solve the \output request sneaking	
	• •	
	\pcol@nextpage: Remove unnecessary scan of $\pi(p_t)$.	
	\pcol@outputelt: Add \boxmaxdepth = \@maxdepth for depth capping	
	\pcol@output@start: Add \pcol@outputtrue to solve the \output request sneaking	
	\pcol@output@start: Include the effect of the separation of pre-environment bottom floats an	
	columns in the starting page into the check of too large pre-envronment stuff	
	\pcol@makenormalcol: Turn \ifpcol@lastpage be true temporarily for \pcol@combinefloats	S
	to separate bottom floats in pre-environment stuff and the multi-column stuff in paracol	1.50
	environment by \textfloatsep.	178
	\pcol@output@switch: Modify broadcasting of $\kappa_c(\sigma)$ so that \@afterindent is broadcasted with \Onobreak	189
	WILL AMIDITERS	100

	\pcol@flushcolumn: Save \ifpcol@lastpage into \ifpcol@lastpagesave and turn	
	\ifpcol@lastpage false temporarily during the macro works on non-top and thus non-last	
	pages to fix the bug that \@makecol and \pcol@makefcolumn misunderstand the page the	y
	work on is last.	204
	\pcol@flushcolumn: Replace \@makecol with \pcol@@makecol to cap the depth of	
	\Coutputbox by \Cmaxdepth even with pLATFX.	204
	\pcol@flushcolumn: Add the restore of \ifpcol@lastpage from \ifpcol@lastpagesave	206
	\pcol@makefcolumn: Replace the sequence of operations to make a usual float column with	
	\@toplist with the newly introduced \pcol@makefcolpage	207
	\pcol@makefcolpage: Introduced to implement the operations to make a float column	
	performed in three macros.	208
	\pcol@synccolumn: Add an shrink of 1/10000 fil to the bottom of flushed column pages to	_00
	cancel finite shrinks just below synchronization points.	211
	\pcol@output@flush: Add \boxmaxdepth = \@maxdepth for depth capping	
	\pcol@output@flush: Add \boxmaxdepth = \@maxdepth for depth capping	
	\pcol@output@clear: Add \boxmaxdepth = \@maxdepth for depth capping	
	\pcol@imakeflushedpage: Enclose the column-page building process in a group to fix the bug	
	which lets \topfigrule = \relax affecting to another column	220
	\pcol@imakeflushedpage: Replace the sequence of operations to make a usual float column	220
	with \Coplist with the newly introduced \pcolCmakefcolpage	220
		220
	\pcol@imakeflushedpage: Replace \@makecol with \pcol@@makecol to cap the depth of	220
	\Coutputbox by \Cmaxdepth even with pLATEX.	220
	\pcol@output@end: Add \pcol@outputfalse to solve the \output request sneaking	222
	\pcol@output@end: Add \boxmaxdepth = \@maxdepth for depth capping knowing it is	222
	redundant.	222
	\pcol@zparacol: Add the saving of \@combinefloats	
	\globalcounter: Examine if the argument counter is already in Θ^g to avoid the duplication in	
	the list which caused a bug	241
v1.	21	
	General: Fix the bug by which a column having empty column-pages followed by a	
	synchronization point is lost or placed in a wrong page. (2013/06/06)	
	\pcol@flushcolumn: Add page and column numbers to logging	204
	\pcol@flushcolumn: Fix the bug that $\kappa_c(\beta^p)$ is let have \pcol@page, which can be less than	
	$p_t = \protect\$ to cause the column c is lost or moved to a wrong page	206
	\pcol@invokeoutput: Add zero-clearing of \deadcycles	226
v1.	22	
	General: Fix the bug that \color and its relatives in a paragraph or around page top causes	
	inconsistency of color context. (2013/06/30)	
	General: Add the subsection "Coloring in Horizontal Mode"	71
	\ifpcol@output: Add a user \pcol@reset@color@pop to inhibit uncoloring if false	131
	\ifpcol@inner: Introduced to know if we are in a \vbox	134
	\pcol@everyvbox: Introduced to keep \everyvbox work as usual while having	
	\pcol@innertrue in it always	140
	\pcol@output: Add reset of \set@color	143
	General: \pcol@op@cpush was introduced for output request to push color stack but removed	
	v1.34	
	General: \pcol@op@cpop was introduced for output request to pop color stack but removed in	
	v1.34	173
	General: \pcol@op@cset was introduced for output request to set γ_0^c but removed in v1.34 .	
	\pcol@specialoutput: Add the invocation of \pcol@output@ f for $f \in \{\text{cpush}, \text{cpop}, \text{cset}\}$.	
	\pcol@output@start: Move emptying \pcol@colorstack to \pcol@zparacol	
	General: \pcol@output@cpush was introduced for color stack pushing but removed in v1.34.	187
	General: \pcol@output@icpush was introduced to implement \pcol@output@cpush but	
		187

	General: \pcol@output@cpop was introduced for color stack popping but removed in v1.34 General: \pcol@reset@color@elt was moved from the position where \pcol@reset@color@pc was defined because it became to be used only by \pcol@output@cpop, but removed in	
	v1.34	
	in v1.34	187
	General: $\pcol@return@from@color$ was introduced to implement $\pcol@output@cpush$, $\pcol@output@cpop$ and $\pcol@output@cset$ but removed in v1.34 \pcol@zparacol: Add a trick with $\ensuremath{\pcol@output@start}$ to $\pcol@zparacol$: Move initial emptying of $\prom \pcol@output@start$ to $\pcol@zparacol$.	187 230 230
	$\label{eq:color_problem} $$\operatorname{Columncolor}: Add initial emptying of $\hat{\varGamma}$ and χ $	230
	\pcol@icolumncolor: Add the definition of \pcol@colorcommand for warning in	259
	\pcol@icolumncolor. General: \pcol@getshadowcc was introduced for setting $\hat{\gamma}_0^c$ into γ_0^c locally, but removed in	259
	v1.34	259
	$ \begin{array}{c} \text{color stack.} \\ \text{\colorightarrow} \\ \c$	261
	$\label{lem:colored} $$ \operatorname{Colored}_{Colored}_{\operatorname{Colored}_{\operatorname{Colored}_{\operatorname{Colored}_{\operatorname{Colored}_{Color$	262
	removed in v1.34	263 263
	\pcol@restoreeveryvbox: Introduced to reflect \global updates on \everyvbox in paracol environments.	268
1.	23	
	General: Fix the problem that a colored text has a line break candidate at its end inappropriately. (2013/07/08)	
	\pcol@set@color@push: Add an argument of null \hskip to \pcol@color@invokeoutput so that the first word of a colored text is hyphenated.	261
	\pcol@reset@color@pop: Add an argument of \relax to \pcol@color@invokeoutput so that the last word of a colored text is not followed by a line break candidate	262
	General: \pcol@color@invokeoutput was modified to add second argument s to insert a null skip after \vadjust only when the macro is invoked from \pcol@set@color@push in horizontal mode	263
1.	24	
	General: Fix the problem caused by the concealment of \vadjust in math group. (2013/07/2' General: Add the subsection "Coloring in Math Mode"\pcol@mcid: Introduced for coloring specified in math mode	73
	\pcol@output: Add zero-clear of \pcol@mcid	143 n
	v1.34	174 174
	General: \pcol@op@mcpop was introduced for coloring specified in math mode but removed in v1.34	

General: \pcol@op@mcpop@pone was introduced for coloring specified in math mode but	
removed in v1.34.	174
\pcol@specialoutput: Add examination with P_{push} and P_{pop} and invocation of	
\pcol@output@mcpush and \pcol@output@mcpop	174
General: \pcol@output@mcpush was introduced for coloring specified in math mode but	
removed in v1.34	187
General: \pcol@output@imcpush was introduced for coloring specified in math mode but	105
removed in v1.34.	187
General: \pcol@output@mcpop was introduced for coloring specified in math mode but remove	
in v1.34	187
General: \pcol@output@mcpop@elt was introduced for coloring specified in math mode but	
removed in v1.34.	
\pcol@icolumncolor: Add math mode to the cases of ineffective use	
\pcol@mcpushlimit: Introduced for coloring specified in math mode	
\pcol@set@color@push: Add the mechanism special for math mode	
\pcol@reset@color@mpop: Introduced for coloring specified in math mode	262
v1.3-1	
General: Fix the known problem of the placement of page-crossing spanning texts.	
(2013/09/17)	1
General: Remove the problem description of the placement of page-crossing spanning texts	
because it has been solved	. 59
General: Change the section title from "Column-Swapping" to "Parallel-Paging,	
Column-Swapping, Column-Separating Rule Drawing and Background Painting" to discu	SS
related issues together"	. 74
\ifpcol@sptextstart: Introduced to capture the starting point of a spanning text so that the	ıe
text is split from other main vertical list stuff.	131
\ifpcol@sptext: Renamed from \ifpcol@mctext following the naming convention, and move	Э
the timing of turning <i>true</i> from the end of a spanning text to its beginning	
\pcol@prespan: Introduced to save pre-spanning-text stuff	
\pcol@output: Add \ifpcol@sptextstart = $false$ to the condition for the warning of too sm	
\vsize	
\pcol@makecol: Add a function to capture a broken spanning text, to combine it with	
pre-spanning-text stuff, and to shift it left on column-swapping.	145
\pcol@output@switch: Add the capture of a spanning text when it is closed	
\pcol@output@switch: Rename \ifpcol@mctext as \ifpcol@sptext	
\pcol@shiftspanning: Introduced to shift a spanning text to left if the column-0 is not	
leftmost due to column-swapping.	182
\pcol@restartcolumn: Rename \pcol@restorecst@restart as \pcol@putbackmvl	
\pcol@putbackmvl: Renamed from \pcol@restorecst@restart and the operations to save	100
pre-spanning-text stuff is added.	187
$\$ \pcol@sptext: Add \ifpcol@sptextstart = $true$ before first synchronized column-switching	
let \pcol@output@switch save pre-spanning-text stuff, move the timing of	10
\ifpcol@sptext = $true$ from the end of spanning text to the beginning so that \output	
routine for a page break in the text capture the pre-break portion, and remove the	
invocation of \pcol@swapcolumn because spanning texts are now always put into the	
column-0	246
v1.3-2	240
	1
General: Introduce parallel-paging. (2013/09/17)	
General: Add description of parallel-paging.	
General: Add descripting of the optional argument of \columnratio for parallel-paging	
General: Add descripting of \setcolumnwidth.	
General: Add the section "Two-Sided Typesetting and Parallel-Paging"	
General: Add comments about the limitaion of parallel-paging.	
General: Add overview description of parallel-paging.	. 74

	\pcol@ncolleft: Introduced to specify the number of columns in left parallel-pages	
	\ifpcol@output: Add a user \@outputpage for parallel-paging	131
	\ifpcol@paired: Introduced for parallel-paging which has paired and non-paired mode	135
	\pcol@rightpage: Introduced to have the ship-out image of a right parallel-page	138
	\pcol@opcol: Rename \pcol@outputpage as \pcol@outputcolumns	148
	$\polesize the problem of the parallel-paging $	149
	\pcol@startpage: Duplicate \stepcounter of \c@page if non-paired parallel-paging is in	
	effect.	152
	\pcol@outputcolumns: Rename \pcol@outputpage as \pcol@outputcolumns	154
	\pcol@outputelt: Add building a empty right parallel float page	
	\pcol@outputelt: Move the core of ship-out image building to \pcol@ioutputelt for parallel	
	pageing	
	\pcol@ioutputelt: Introduced for parallel-paging	
	\pcol@phantom: Introduced for parallel-paging	
	\pcol@coutputpage: Introduced keep the original definition of \@outputpage	
	\Coutputpage: Redefined for parallel-paging	
	\pcol@outputpage@1: Introduced for shipping out left parallel-pages	
	\pcol@outputpage@r: Introduced for shipping out right parallel-pages	
	\pcol@putfootins: Change users \pcol@outputelt to \pcol@ioutputelt	
	\pcol@output@flush: Add depth capping of \pcol@rightpage	
	\pcol@output@clear: Add depth capping of \pcol@rightpage and building an empty right	
	parallel-page for each page-wise float page.	214
	\pcol@makeflushedpage: Completely redesigned with new macro \pcol@imakeflushedpage.	215
	\pcol@imakeflushedpage: Introduced for parallel-paging	
	\pcol@flushfloats: Completely redesigned with new macro \pcol@iflushfloats	
	\pcol@iflushfloats: Introduced for parallel-paging	
	\pcol@output@end: Add parallel-paging operations	
	\paracol: Modify to add the optimal argument C_L and optimal '*' for parallel-paging \pcol@xparacol: Introduced to let $C_L = C$ if the optimal argument C_L is not given to	
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	\columnratio: Add optional second argument for fractions in right parallel-pages	
	\pcol@icolumnratio: Introduced to process the optional second argument of \columnratio.	
	\pcol@columnratioleft: Renamed from \pcol@columnratio to clarify it has fractions for left	
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	\pcol@setcolwidth@r: Add arguments C^0 , C^1 , $\langle ratio \rangle$ and $\langle spec \rangle$ for columns in right parallel-pages	235
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	General: Add the sub-section "Commands for Two-Sided Typesetting and Marginal Note	
	Placement".	
	General: Add description of \twosided	
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General: Add description of \backgroundcolor
General: Add description of \nobackgroundcolor and \nobackgroundcolor
General: Add description of \pagerim
General: Remove the problem description of the lack of column-separating rule drawing because
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General: Add comments about the imperfectnss of extention of backgroud painting regions 60
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\ifpcol@output: Add a user \@outputpage for background-painting
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\pcol@makecol
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\pcol@getcurrpinfo: Revise reflecting the new page context element $\pi^s(p)$, and add a invoker \pcol@makecol
\pcol@getcurrpinfo: Revise reflecting the new page context element $\pi^s(p)$, and add a invoker \pcol@makecol
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$\label{eq:colored} $$ \begin{array}{llll} $\operatorname{pcol@getcurrpinfo}:$ & Revise & reflecting & the & new & page & context & element & \pi^s(p), & and & add & a & invoker & pcol@makecol. &$
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$\label{eq:colored} $$\operatorname{pcol@makecol}$
$\label{eq:colored} $$\operatorname{pcolored}(p), and add a invoker $$pcolo$
$\label{eq:colored} $$\operatorname{pcolored}_{pcolored}$: Revise reflecting the new page context element $\pi^s(p)$, and add a invoker \operatorname{pcolored}_{pcolored}$: Revise reflecting the new page context element $\pi^s(p)$ $
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	eral: Change the subsection title from "Coloring" to "Text Coloring" to distinguish it from	
	background painting clearly.	
	ol@zparacol: Add new API inactivation for \footnotelayout	
	ecolumn: Introduced to let users know which column they are working in	
	ol@localcommands: Add \@elt{cleardoublepage} for \cleardoublepage	
-	ol@switchcol: Add setting $V_E = \text{QCol@ensurevspace}$ and reinitialization of	_00
		247
\en	surevspace: Introduced to declare the minimum space V_E below a synchronization point to	
	let it stay in a page	
	ol@ensurevspace: Introduced to keep V_E declared by \ensurevspace	
	ol@@ensurevspace: Introduced to pass V_E declared by \ensurevspace to \output	100
		250
	eardoublepage: Added as a member of local commands and made \let-equal to	200
		252
	ol@com@cleardoublepage: Introduced as the implementation of \cleardoulbepage 2	-
	otnotelayout: Introduced for easier declaration of footnote layout	
	ol@fnlayout@c: Introduced for easier declaration of column-wise footnotes	
	ol@fnlayout@m: Introduced for easier declaration of merged footnotes	
Gen	eral: Rename the section title from "Column-Swapping" to "Two-Sided Typesetting" 2	1 G2

\twosided: Introduced as an easier API for various two-sided typesetting
\pcol@twosided: Introduced to implement \twosided
\pcol@twosided@p: Introduced to implement \twosided with [p]
\pcol@twosided@c: Introduced to implement \twosided with [c]
\pcol@twosided@m: Introduced to implement \twosided with [m]
\pcol@twosided@b: Introduced to implement \twosided with [b]
v1.3-6
General: Fix a few problems mainly related to synchronization and ordinary footnotes.
$(2013/09/17) \dots \dots \dots \dots \dots \dots \dots \dots \dots $
General: Add comments about usage of \paragraph etc. in spanning texts 60
General: Change the title from "Single-Columned and Merged Footnotes" to "Page-Wise and
Merged Footnotes" according to the new naming
\ifpcol@bfbottom: Introduced to know which column-wise footnotes or bottom floats are put
at the bottom of a column
\ifpcol@dfloats: Introduced to know if the last page has deferred column-wise floats 136
\pcol@ShowBox: Change \unvcopy to \copy to make sure the argument box causes overfull if its
height is positive and even if it has nothing
$\colored{colored}$ Add an argument d to be assigned to $\colored{colored}$ to let it have 0 rather
than \Cmaxdepth for last page 144
\pcol@combinefloats: Add special operations for columns having synchronization point to
move the infinite stretch and shrink to let it follow bottom floats ratehr than preceding
them
\pcol@nextpelt: Fix the bug that $\pi^h(q)$ is not referred correctly
\pcol@output@start: Change the page builder for too tall pre-environment stuff from
\pcol@makenormalcol to \@makecol because the page should be built by the ordinary
mechanism
\pcol@output@start: Delete the argument of \pcol@makenormalcol because now it is not used
too tall pre-environment stuff
\pcol@makenormalcol: Completely redesigned to use \@makecol if pre-environment stuff has
bottom floats
\pcol@output@switch: Modify the condition of broadcasting $\kappa_0(\sigma)$ and $\kappa_0(\varepsilon)$ accompanied
with \ifpcol@sptext from \ifpcol@sync to $c = 0$ so that the broadcast is made in the first
column-switching in column-scanning
modification of the broadcast of $\kappa_0(\sigma)$ and $\kappa_0(\varepsilon)$
\pcol@restartcolumn: Change the code structure to move the insertion of page break penalty
for ordinary column-wise footnotes from below the main text to below the footnotes 183
General: Move commands outside \output routine to the newly introduced section "Commands
for Text Coloring" to distinguish macros inside and outside \output routine 187
\pcol@shrinkcolbyfn: Add the third argument $\langle skip \rangle$ to avoid accidental destruction of
\Qtempdimb which was modified unconditionally
\pcol@deferredfootins: Fix the bug that the height cap was underestimated by the duplicated
subtraction of \skip\footins if the page has already have non-deferred footnotes 195
\pcol@putfootins: Remove \pcol@output@end from users 193
\pcol@sync: Add the initialization of \ifpcol@dfloats = false before invoking
\pcol@measurecolumn
\pcol@sync: Modify the flushing condition of synchronized column switching from $V > \pi^h(p)$
to $\max(V, V - D_T + V_E) > \pi^h(p)$ to avoid page break just below the synchronization point
as much as possible
\pcol@flushcolumn: Fix the problem that a flushed column in a non-top page causes overfull
due to its hight-plus-depth greater than $\pi^h(p)$
\pcol@flushcolumn: Add \@maxdepth as the first argument of \pcol@@makecol

\pcol@measurecolumn: Revise the mechanism to tell \pcol@makeflushedpage and	
\pcol@output@end that a column in a last page has deferred column-wise floats with ne	ewly
introduced \ifpcol@dfloats	. 210
\pcol@makeflushedpage: Revise the mechanism of special care about last page introducing	
\ifpcol@dfloats	
\pcol@makeflushedpage: Revise the condition of leaving page-wise floats as ordinary	
post-environment floats using \if@tempswa with \ifpcol@dfloats	. 217
\pcol@makeflushedpage: Remove empty column scan for \if@fcolmade because it is now	. 211
unnecessary thanks to \ifpcol@dfloats	. 217
\pcol@makeflushedpage: Revise the condition of column-page building and setting of	. 211
	. 217
\@colht.	
\pcol@makeflushedpage: page-wise footnotes for the last page followed by pages for deferred	
column-wise floats are now put by this macro.	
\pcol@imakeflushedpage: Add \@maxdepth or 0 as the argument of \pcol@makecol to fix	
problem that the last page is too large due to \@maxdepth, by the latter	
\pcol@imakeflushedpage: Remove the examination of $\kappa_c(\lambda_d)$ for \if@fcolmade because it	
made unnecesary now by \ifpcol@dfloats	. 220
\pcol@output@end: Simplify the case with deferred floats thanks to \ifpcol@dfloats and	
redesign of \pcol@makeflushedpage	
\pcol@output@end: Remove \unskip from the operation to let page-wise floats be ordinary	
ones because \pcol@makeflushedpage does it	. 224
\pcol@zparacol: Add operations for the vertical skips at the beginning of a list-like	
environment.	. 228
\pcol@sptext: Add globalization of \@svsechd and \@svsec	246
General: Add the section "Commands for Text Coloring" to distinguish macros inside and	
outside \output routine and describe latters in this section	. 259
\pcol@set@color@push: Change the second argument of \pcol@color@invokeoutput from	
\hskip\z@ to \pcol@fcwhyphenate to make null skip insertion conditional	. 261
\coloredwordhyphenated: Introduced to enable null skip insertion before the first word after	
coloring command not always but conditionally.	
\nocoloredwordhyphenated: Introduced to disable null skip insertion before the first word a	
a coloring command	
\pcol@fcwhyphenate: Introduced to enable null skip insertion before the first word after a	. 200
coloring command not always but conditionally.	. 263
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General: Add passing parameters related sectioning commands beyond \end{paracol} a	
fix misspells in error messages. (2013/10/10)	
\pcol@output@end: Add \pcol@getcurrcol for the column specified by \pcol@lastcol to p	
\if@nobreak, \if@afterindent and \everypar of the column to post-environment stuff	
\pcol@setcw@calcf: Capitalize the first word of the error message for consistency	
\pcol@switchcolumn: Add a space before the number of columns in the error message	245
\pcol@switchenv: Fix the misspell "switching" in the error message.	
\pcol@twosided: Fix spelling "twosiding" replacing it with "two-siding" in the error messag	
\pcol@backgroundcolor: Fix the mispell "colorling" in the error message	
$\verb \endparacol : Add saving c into \verb \endparacol : Add saving c into $$	
visited last	. 267
\pcol@lastcol: Introduced to keep the column visited last to pass its typesetting parameter	ers
to post-environment	. 267
v1.32-1	
General: Add \globalcounter* to make all counters global. (2015/10/10)	1
General: Add descriptions of \globalcounter*	
\globalcounter: Modified according to the introduction of \globalcounter*	
\pcol@globalcounter@s: Added for \globalcounter*	
· · · · · · · · · · · · · · · · · · ·	

\pcol@globalcounter: Renamed from \globalcounter according to the introduction of
\globalcounter*
v1.32-2
General: Fix a memory leak in \pcol@startcolumn. (2015/10/10)
\pcol@F@write: Introduced for debugging memory leak problems
\pcol@F: Introduced for debugging memory leak problems
\pcol@FF: Introduced for debugging memory leak problems
\pcol@F@count: Introduced for debugging memory leak problems
\pcol@F@n: Introduced for debugging memory leak problems
\pcol@Fb: Introduced for debugging memory leak problems
\pcol@Fe: Introduced for debugging memory leak problems
\pcol@makecol: Add \pcol@Fb/\pcol@Fe pair(s) 148
\pcol@cflt: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@opcol: Add \pcol@Fb/\pcol@Fe pair(s)
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\pcol@outputelt: Add \pcol@Fb/\pcol@Fe pair(s) 158
\pcol@ioutputelt: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@ioutputelt: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@ioutputelt: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@startcolumn: Fix the memory leak caused by mistakingly preserving $\pi^f(p)$ when
$p = p_t \dots \dots$
\pcol@startcolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@start: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@start: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@start: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@makenormalcol: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@switch: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@restartcolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@restartcolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@flushcolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@flushcolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@flushcolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@makefcolpage: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@synccolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@makeflushedpage: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@makeflushedpage: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@imakeflushedpage: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@end: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@end: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@output@end: Add \pcol@Fb/\pcol@Fe pair(s)
v1.32-3
General: Fix a page-wise float problem. (2015/10/10)
General: Add footnote to mention the page-wise float problem
General: Add comments about the out-of-order appearance of page-wise floats even with
ETFX-2015/01/10 or later
General: Add the section "Page-wise Float Placement" to discuss the page-wise float problem. 79
\pcol@startpage: Add \f@depth = 0 to override \f@depth = 1sp done by
\@dblfloatplacement 152
\pcol@startpage: Modify the code to apply \@sdblcolelt to \@dbldeferlist so as to work
with both 2015 (or newer) and 2014 (or older) versions of LATEX
\pcol@output@start: Add depth clearing of imported deferred floats in case that some of them
has 1sp
\pcol@output@clear: Add \f@depth = 0 to override \f@depth = 1sp done by
\projection \frac{1}{2} \text{correct} \text{ Add \frac{1}{2} \text{depth} = 0 to overfide \frac{1}{2} \text{depth} = 1 \text{sp done by}

	\pcol@zparacol: Add replacement of \end@dblfloat with \pcol@end@dblfloat 229
	\@dbldeferlist: Add top-level definition in case that future LATEX removes it at all 233
	\pcol@end@dblfloat: Added to go back to old mechanism 233
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	General: Fix a marginal note problem. (2016/11/19)
	\pcol@getmpbelt: Fix the bug by which t_k such that $t_k \geq t$ and $t_k - t \geq h$ but $t_k - b_{k-1} < h$ is
	found
v1.	33-2
	General: Non-logical modifications to obey the coding convention, for clarification, etc (2016/11/19)
	\pcol@output: Add a space after \@opcol to obey the coding convention
	\pcol@makecol: Move down the \definition of \pcol@currfoot with \property to place it just before
	the \ifpcol@scfnote/\fi construct to make it clear how \pcol@currfoot is \defined. 145
	\pcol@cflt: Add % to the end of the line to open \vbox for \@outputbox to obey the coding
	convention
	\pcol@opcol: Add % to the end of the line to open \vbox for \@currbox to obey the coding
	convention
	\pcol@setpageno: Add \let\@elt\relax before \edef of \reserved@a for the sake of clarity. 149 \pcol@output@switch: Let \dimen@ have the height of \pcol@prespan if it is not \bot , or 0 if \bot
	for the sake of clarity
	\pcol@putbackmvl: Add % to the end of the line to open \vbox for \pcol@prespan to obey the
	coding convention.
	\pcol@makefcolumn: Remove a space after the \vbox to be assigned to \@currbox to obey the
	coding convention
	\pcol@makefcolpage: Add % to the end of the line to open \vbox to obey the coding
	convention
	\pcol@synccolumn: Add % to the end of the line to open \vbox for \pcol@float to obey the
	coding convention. 212
	\pcol@synccolumn: Add % to the end of the line to open \vbox for \@currbox and two lines for
	\vboxes in it to obey the coding convention
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	General: Fix a text coloring problem in non-breakable sequences of vertical items. (2018/05/07) 1
	General: Revise the description of §1.6.1 according to the new implementation with \insert. 70
	General: Revise the description of §1.6.2 according to the new implementation with \insert. 71
	General: Split the description of \columncolor from \\$1.6.2 to have new \\$1.6.3 "Changing
	Default Column Color" because we have serveral new issues in the new implementation
	with \insert
	General: Revise the description of §1.6.4 according to the new implementation with \insert. 73 \pcol@mcid: Change its meaning and operations with it a little bit according to the new text
	coloring with \insert 130
	\pcol@colorstack@saved: Introduced as Γ_s to keep the color stack Γ^c until a column-page of c
	becomes non-empty
	\pcol@tempboxa: Renamed from \pcol@tempbox because its relative \pcol@tempboxb is
	introduced
	\pcol@tempboxa: Add ussage in \pcol@scancst and \pcol@iscancst
	\pcol@tempboxb: Introduced to extract the top of color stack Γ , Γ_r or Γ_s
	General: Add §3.6 "\insert Register Set" for \pcol@colorins
	\pcol@colorins: Introduced to present text-coloring operations to \output synchronously with
	column-pages
	of 1 pt if $\langle b \rangle$'s height is 0 to ensure overfull too
	\pcol@buildcolseprule: Rename \pcol@tempbox as \pcol@tempboxa
	\pcol@buildcselt: Rename \pcol@tempbox as \pcol@tempboxa 158
	\pcol@hfil: Rename \pcol@tempbox as \pcol@tempboxa 160

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General: \pcol@op@cpush is removed according to the change of text coloring from \output to	
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$General: \verb \pcol@op@mcpop is removed according to the change of text coloring from \verb \output to the change of text $	
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$\verb \problem= \text{ $$ related to } f \in \{\texttt{cpush}, \texttt{cpop}, \texttt{mcpush}, \texttt{mcpop}\}. \end{magnetically} .$	174
$\verb \prool@output@start : Add initialization of $\gamma_0^c = \prool@columncolor@box \cdot c. \qquad$	178
\pcol@putbackmvl: Change nullification of $\Gamma_s = \pcol@colorstack@saved$ from \gdef to	
\box-assignment of ⊥ because it is now a \vbox	187
General: \pcol@output@cpush is removed according to the change of text coloring from	
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\pcol@clearcolorstack: Completely change its definition according to the new text coloring	100
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General: \pcol@set@color@elt is removed according to the change of text coloring from	1.00
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\pcol@restorecolorstack: Completely change its definition according to the new text coloring its terms of the new text coloring its definition according to the new text coloring text color	_
with \insert.	189
\pcol@restorecst: Completely change its definition according to the new text coloring with	
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\pcol@scancst: Introduced to implement new text coloring with \insert	189
\pcol@iscancst: Introduced to implement new text coloring with \insert	189
\pcol@savecolorstack: Completely change its definition according to the new text coloring	
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\output to \insert	
\pcol@ccuse: Introduced to implement new text coloring with \insert	
\pcol@ifccdefined: Introduced to implement new text coloring with \insert	
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\pcol@output@end: Remove nullification of γ_0^0 because it is not meaningless now, add rele	
$\gamma_0^c \neq \bot$ and then nullification of it for all c, move color stack reestablishment down to	
loop with c to ensure $\gamma_0^0 = \bot$, and add nullification of Γ	
\pcol@zparacol: Remove the initializations of \pcol@colorstack and \pcol@colorstack because they no longer exist.	
General: \pcol@getshadowcc is removed according to the change of text coloring from \oto \insert.	
\pcol@icolumncolor: Remove the invocations of \pcol@iicolumncolor for	
$\protect\$ \pcol@columncolor@shadow $\cdot c$ because it no longer exists, completly change the	
opearations in the case the target column c is the current one according to the new m	ethod
with \insert, and add immediate setting of γ_0^c in the case c is not current	
\pcol@iicolumncolor: Remove the third argument, change the second argument from a c	
sequence name to the target column, add a grouping to surround the entire body of the	
macro, and change the body of γ_0^c so that it only has the color information	259
\pcol@scancst@shadow: Introduced to rewind or establish the color stack $\hat{\Gamma}^c$	
\pcol@mcpushlimit: Move down to place it just before the \definition of	
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\pcol@set@color@push: Completely change its definition according to the new text colori	_
with \insert.	
\pcol@reset@color@pop: Completely change its definition according to the new text color	
with \insert	
• • • • • • • • • • • • • • • • • • • •	_
with \insert.	
General: \pcol@color@invokeoutput is removed according to the change of text coloring	
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General: \pcol@color@invokeoutput@v is removed according to the change of text coloring from \output to \insert	
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$(2018/12/31) \dots \dots \dots \dots \dots \dots \dots \dots \dots $	
$\label{lem:condition} $$\operatorname{Condition} to perform operations for first $$ v1.35-3 $$$	
General: Fix a bug in \pcol@addmarginpar and add emulation of \marginnnote. (2018/1)	
General: Add description of \marginnote	
\pcol@addmarginpar: Fix the bug referring to \@marbox inappropriately	194
\pcol@addmarginpar: Add vertical shifting of marginal note to emulate of \marginnote. \pcol@zparacol: Add local modifications of \marginpar, \@mn@@marginnote and \@xympa	
the emulation of \marginnote	
General: Add the section "Commands for Marginal Notes" to describe newly introduced	
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\pcol@marginpar: Introduced as the in-paracol version of \marginpar for the emulation	
\marginnote	

\pcol@marginpar: Introduced to keep the orignal version of \marginpar for the emulation of	
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	256
\pcol@marginnote: Introduced as the in-paracol version of \@mn@@marginnote for the	
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	256
\@xympar: Locally modified in \pcol@zparacol for the emulation of \marginnote	256
\pcol@xympar: Introduced as the in-paracol version of \@xympar for the emulation of	
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\pcol@@xympar: Introduced to keep the orignal version of \@xympar for the emulation of	
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\pcol@mparoffset: Introduced to have the vertical offset for the emulation of \marginnote.	256
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General: Add \belowfootnoteskip for the additional space below the non-merged	
pre-environment footnotes. (2018/12/31)	1
* · · · · · · · · · · · · · · · · · · ·	15
General: Add description of \belowfootnoteskip.	25
\belowfootnoteskip: Introduced to specify the additional space below the non-merged	
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$\protect\$ Add $\protect\$ to H_f being the space for the non-merged	
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\pcol@combinefootins: Add the insertion of vertical skip \belowfootnoteskip 1	193
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General: Add \definecolumnpreamble. (2018/12/31)	
General: Add description of \definecolumnpreamble.	
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$\protect\$ Add the invocation of $\protect\$	
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General: Add error check if paracol environment is not in outer par mode and is with ordinary	
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\pcol@zparacol: Add error check with \ifinner and \if@twocolumn	228