Package 'RobLox'

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Title Optimally Robust Influence Curves and Estimators for Location and Scale

Description Functions for the determination of optimally robust influence curves and estimators in case of normal location and/or scale (see Chapter 8 in Kohl (2005) <https://epub.uni-bayreuth.de/839/2/DissMKohl.pdf>).

Depends R(>= 3.4), stats, distrMod(>= 2.8.0), RobAStBase(>= 1.2.0)

Imports methods, lattice, RColorBrewer, Biobase, RandVar(>= 1.2.0), distr(>= 2.8.0)

Suggests MASS

Enhances ROptEst

ByteCompile yes

License LGPL-3

URL http://robast.r-forge.r-project.org/

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Contents

`RobLox-package` *Optimally robust influence curves and estimators for location and scale*

Description

Functions for the determination of optimally robust influence curves and estimators in case of normal location and/or scale (see Chapter 8 in Kohl (2005) <https://epub.uni-bayreuth.de/839/2/DissMKohl.pdf>).

Package versions

Note: The first two numbers of package versions do not necessarily reflect package-individual development, but rather are chosen for the RobAStXXX family as a whole in order to ease updating "depends" information.

Author(s)

Matthias Kohl <matthias.kohl@stamats.de>

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

H. Rieder (1994): Robust Asymptotic Statistics. Springer. doi:10.1007/9781468406245

H. Rieder, M. Kohl, and P. Ruckdeschel (2008). The Costs of Not Knowing the Radius. Statistical Methods and Applications *17*(1): 13-40. doi:10.1007/s1026000700477 M. Kohl, P. Ruckdeschel, and H. Rieder (2010). Infinitesimally Robust Estimation in General Smoothly Parametrized Models. Statistical Methods and Applications *19*(3): 333-354. doi:10.1007/s1026001001330.

M. Kohl and H.P. Deigner (2010). Preprocessing of gene expression data by optimally robust estimators. BMC Bioinformatics *11*, 583. doi:10.1186/1471210511583.

M. Kohl (2012). Bounded influence estimation for regression and scale. Statistics, **46**(4): 437-488. doi:10.1080/02331888.2010.540668

See Also

RobAStBase-package

Examples

```
library(RobLox)
ind <- rbinom(100, size=1, prob=0.05)
x <- rnorm(100, mean=ind*3, sd=(1-ind) + ind*9)
roblox(x)
res <- roblox(x, eps.lower = 0.01, eps.upper = 0.1, returnIC = TRUE)
estimate(res)
confint(res)
confint(res, method = symmetricBias())
pIC(res)
## don't run to reduce check time on CRAN
## Not run:
checkIC(pIC(res))
Risks(pIC(res))
Infos(pIC(res))
plot(pIC(res))
infoPlot(pIC(res))

## End(Not run)
## row-wise application
ind <- rbinom(200, size=1, prob=0.05)
X <- matrix(rnorm(200, mean=ind*3, sd=(1-ind) + ind*9), nrow = 2)
rowRoblox(X)
```

`finiteSampleCorrection` *Function to compute finite-sample corrected radii*

Description

Given some radius and some sample size the function computes the corresponding finite-sample corrected radius.

Usage

```
finiteSampleCorrection(r, n, model = "locsc")
```

Arguments

r	asymptotic radius (non-negative numeric)
n	sample size
model	has to be "locsc" (for location and scale), "loc" (for location) or "sc" (for scale), respectively.

Details

The finite-sample correction is based on empirical results obtained via simulation studies.

Given some radius of a shrinking contamination neighborhood which leads to an asymptotically optimal robust estimator, the finite-sample empirical MSE based on contaminated samples was minimized for this class of asymptotically optimal estimators and the corresponding finite-sample radius determined and saved.

The computation is based on the saved results of these Monte-Carlo simulations.

Value

Finite-sample corrected radius.

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

H. Rieder (1994): Robust Asymptotic Statistics. Springer. doi:10.1007/9781468406245

M. Kohl and H.P. Deigner (2010). Preprocessing of gene expression data by optimally robust estimators. BMC Bioinformatics *11*, 583. doi:10.1186/1471210511583.

See Also

roblox, rowRoblox, colRoblox

Examples

```
finiteSampleCorrection(n = 3, r = 0.001, model = "locsc")
finiteSampleCorrection(n = 10, r = 0.02, model = "loc")
finiteSampleCorrection(n = 250, r = 0.15, model = "sc")
```

`rlOptIC` *Computation of the optimally robust IC for AL estimators*

Description

The function `rlOptIC` computes the optimally robust IC for AL estimators in case of normal location and (convex) contamination neighborhoods. The definition of these estimators can be found in Rieder (1994) or Kohl (2005), respectively.

Usage

```
rlOptIC(r, mean = 0, sd = 1, bUp = 1000, computeIC = TRUE)
```

Arguments

`r`	non-negative real: neighborhood radius.
`mean`	specified mean.
`sd`	specified standard deviation.
`bUp`	positive real: the upper end point of the interval to be searched for the clipping bound b.
`computeIC`	logical: should IC be computed. See details below.

Details

If 'computeIC' is 'FALSE' only the Lagrange multipliers 'A', 'a', and 'b' contained in the optimally robust IC are computed.

Value

If 'computeIC' is 'TRUE' an object of class `"ContIC"` is returned, otherwise a list of Lagrange multipliers

`A`	standardizing constant
`a`	centering constant; always '= 0' is this symmetric setup
`b`	optimal clipping bound

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

H. Rieder (1994): Robust Asymptotic Statistics. Springer. doi:10.1007/9781468406245

M. Kohl, P. Ruckdeschel, and H. Rieder (2010). Infinitesimally Robust Estimation in General Smoothly Parametrized Models. Statistical Methods and Applications *19*(3): 333-354. doi:10.1007/s1026001001330.

See Also

ContIC-class, roblox

Examples

```
IC1 <- rlOptIC(r = 0.1)
distrExOptions("ErelativeTolerance" = 1e-12)
checkIC(IC1)
distrExOptions("ErelativeTolerance" = .Machine$double.eps^0.25) # default
Risks(IC1)
cent(IC1)
clip(IC1)
stand(IC1)
plot(IC1)
```

---

rlsOptIC.AL *Computation of the optimally robust IC for AL estimators*

Description

The function rlsOptIC.AL computes the optimally robust IC for AL estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Section 8.2 of Kohl (2005).

Usage

```
rlsOptIC.AL(r, mean = 0, sd = 1, A.loc.start = 1, a.sc.start = 0,
            A.sc.start = 0.5, bUp = 1000, delta = 1e-6, itmax = 100,
            check = FALSE, computeIC = TRUE)
```

Arguments

r	non-negative real: neighborhood radius.
mean	specified mean.
sd	specified standard deviation.
A.loc.start	positive real: starting value for the standardizing constant of the location part.
a.sc.start	real: starting value for centering constant of the scale part.
A.sc.start	positive real: starting value for the standardizing constant of the scale part.
bUp	positive real: the upper end point of the interval to be searched for the clipping bound b.
delta	the desired accuracy (convergence tolerance).
itmax	the maximum number of iterations.
check	logical: should constraints be checked.
computeIC	logical: should IC be computed. See details below.

Details

The Lagrange multipliers contained in the expression of the optimally robust IC can be accessed via the accessor functions `cent`, `clip` and `stand`. If 'computeIC' is 'FALSE' only the Lagrange multipliers 'A', 'a', and 'b' contained in the optimally robust IC are computed.

Value

If 'computeIC' is 'TRUE' an object of class `"ContIC"` is returned, otherwise a list of Lagrange multipliers

`A`	standardizing matrix
`a`	centering vector
`b`	optimal clipping bound

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

H. Rieder (1994): Robust Asymptotic Statistics. Springer. doi:10.1007/9781468406245

M. Kohl, P. Ruckdeschel, and H. Rieder (2010). Infinitesimally Robust Estimation in General Smoothly Parametrized Models. Statistical Methods and Applications *19*(3): 333-354. doi:10.1007/s1026001001330.

See Also

ContIC-class, roblox

Examples

```
IC1 <- rlsOptIC.AL(r = 0.1, check = TRUE)
distrExOptions("ErelativeTolerance" = 1e-12)
checkIC(IC1)
distrExOptions("ErelativeTolerance" = .Machine$double.eps^0.25) # default
Risks(IC1)
cent(IC1)
clip(IC1)
stand(IC1)

## don't run to reduce check time on CRAN
## Not run:
plot(IC1)
infoPlot(IC1)

## k-step estimation
## better use function roblox (see ?roblox)
```

```
## 1. data: random sample
ind <- rbinom(100, size=1, prob=0.05)
x <- rnorm(100, mean=0, sd=(1-ind) + ind*9)
mean(x)
sd(x)
median(x)
mad(x)

## 2. Kolmogorov(-Smirnov) minimum distance estimator (default)
## -> we use it as initial estimate for one-step construction
(est0 <- MDEstimator(x, ParamFamily = NormLocationScaleFamily()))

## 3.1 one-step estimation: radius known
IC1 <- rlsOptIC.AL(r = 0.5, mean = estimate(est0)[1], sd = estimate(est0)[2])
(est1 <- oneStepEstimator(x, IC1, est0))

## 3.2 k-step estimation: radius known
## Choose k = 3
(est2 <- kStepEstimator(x, IC1, est0, steps = 3L))

## 4.1 one-step estimation: radius unknown
## take least favorable radius r = 0.579
## cf. Table 8.1 in Kohl(2005)
IC2 <- rlsOptIC.AL(r = 0.579, mean = estimate(est0)[1], sd = estimate(est0)[2])
(est3 <- oneStepEstimator(x, IC2, est0))

## 4.2 k-step estimation: radius unknown
## take least favorable radius r = 0.579
## cf. Table 8.1 in Kohl(2005)
## choose k = 3
(est4 <- kStepEstimator(x, IC2, est0, steps = 3L))

## End(Not run)
```

`rlsOptIC.An1` *Computation of the optimally robust IC for An1 estimators*

Description

The function `rlsOptIC.An1` computes the optimally robust IC for An1 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.3 of Kohl (2005).

Usage

```
rlsOptIC.An1(r, aUp = 2.5, delta = 1e-06)
```

Arguments

r	non-negative real: neighborhood radius.
aUp	positive real: the upper end point of the interval to be searched for a.
delta	the desired accuracy (convergence tolerance).

Details

The optimal value of the tuning constant a can be read off from the slot Infos of the resulting IC.

Value

Object of class "IC"

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Andrews, D.F., Bickel, P.J., Hampel, F.R., Huber, P.J., Rogers, W.H. and Tukey, J.W. (1972) *Robust estimates of location*. Princeton University Press.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.An1(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
## don't run to reduce check time on CRAN
## Not run:
plot(IC1)
infoPlot(IC1)

## End(Not run)
```

`rlsOptIC.An2` *Computation of the optimally robust IC for An2 estimators*

Description

The function `rlsOptIC.An2` computes the optimally robust IC for An2 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.3 of Kohl (2005).

Usage

```
rlsOptIC.An2(r, a.start = 1.5, k.start = 1.5, delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`a.start`	positive real: starting value for a.
`k.start`	positive real: starting value for k.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if a or k are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for An2 estimators is based on `optim` where `MAX` is used to control the constraints on a and k. The optimal values of the tuning constants a and k can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

Andrews, D.F., Bickel, P.J., Hampel, F.R., Huber, P.J., Rogers, W.H. and Tukey, J.W. (1972) *Robust estimates of location*. Princeton University Press.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

`IC-class`

Examples

```
IC1 <- rlsOptIC.An2(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

---

rlsOptIC.AnMad *Computation of the optimally robust IC for AnMad estimators*

Description

The function `rlsOptIC.AnMad` computes the optimally robust IC for AnMad estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators were considered in Andrews et al. (1972). A definition of these estimators can also be found in Subsection 8.5.3 of Kohl (2005).

Usage

```
rlsOptIC.AnMad(r, aUp = 2.5, delta = 1e-06)
```

Arguments

`r`	non-negative real: neighborhood radius.
`aUp`	positive real: the upper end point of the interval to be searched for a.
`delta`	the desired accuracy (convergence tolerance).

Details

The optimal value of the tuning constant a can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

Andrews, D.F., Bickel, P.J., Hampel, F.R., Huber, P.J., Rogers, W.H. and Tukey, J.W. (1972) *Robust estimates of location*. Princeton University Press.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.AnMad(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.BM` *Computation of the optimally robust IC for BM estimators*

Description

The function `rlsOptIC.BM` computes the optimally robust IC for BM estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators were proposed by Bednarski and Mueller (2001). A definition of these estimators can also be found in Section 8.4 of Kohl (2005).

Usage

```
rlsOptIC.BM(r, bL.start = 2, bS.start = 1.5, delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`bL.start`	positive real: starting value for b_{loc}.
`bS.start`	positive real: starting value for $b_{\mathrm{sc},0}$.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if b_{loc} or $b_{\mathrm{sc},0}$ are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for BM estimators is based on `optim` where `MAX` is used to control the constraints on b_{loc} and $b_{\mathrm{sc},0}$. The optimal values of the tuning constants b_{loc}, $b_{\mathrm{sc},0}$, α and γ can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Bednarski, T and Mueller, C.H. (2001) Optimal bounded influence regression and scale M-estimators in the context of experimental design. Statistics, **35**(4): 349-369.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

M. Kohl (2012). Bounded influence estimation for regression and scale. Statistics, **46**(4): 437-488. doi:10.1080/02331888.2010.540668

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.BM(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.Ha3` *Computation of the optimally robust IC for Ha3 estimators*

Description

The function `rlsOptIC.Ha3` computes the optimally robust IC for Ha3 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.2 of Kohl (2005).

Usage

```
rlsOptIC.Ha3(r, a.start = 0.25, b.start = 2.5, c.start = 5,
             delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`a.start`	positive real: starting value for a.
`b.start`	positive real: starting value for b.
`c.start`	positive real: starting value for c.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if a or b or c are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for Ha3 estimators is based on `optim` where `MAX` is used to control the constraints on a, b and c. The optimal values of the tuning constants a, b and c can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Ha3(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
## don't run to reduce check time on CRAN
## Not run:
plot(IC1)
infoPlot(IC1)

## End(Not run)
```

---

rlsOptIC.Ha4 *Computation of the optimally robust IC for Ha4 estimators*

Description

The function `rlsOptIC.Ha4` computes the optimally robust IC for Ha4 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.2 of Kohl (2005).

Usage

```
rlsOptIC.Ha4(r, a.start = 0.25, b.start = 2.5, c.start = 5,
             k.start = 1, delta = 1e-06, MAX = 100)
```

Arguments

r	non-negative real: neighborhood radius.
a.start	positive real: starting value for a.
b.start	positive real: starting value for b.
c.start	positive real: starting value for c.
k.start	positive real: starting value for k.
delta	the desired accuracy (convergence tolerance).
MAX	if a or b or c or k are beyond the admitted values, MAX is returned.

Details

The computation of the optimally robust IC for Ha4 estimators is based on optim where MAX is used to control the constraints on a, b, c and k. The optimal values of the tuning constants a, b, c and k can be read off from the slot Infos of the resulting IC.

Value

Object of class "IC"

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Marazzi, A. (1993) *Algorithms, routines, and S functions for robust statistics*. Wadsworth and Brooks / Cole.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Ha4(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.HaMad` *Computation of the optimally robust IC for HuMad estimators*

Description

The function `rlsOptIC.HuMad` computes the optimally robust IC for HuMad estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators were considered in Andrews et al. (1972). A definition of these estimators can also be found in Subsection 8.5.2 of Kohl (2005).

Usage

```
rlsOptIC.HaMad(r, a.start = 0.25, b.start = 2.5, c.start = 5,
               delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`a.start`	positive real: starting value for a.
`b.start`	positive real: starting value for b.
`c.start`	positive real: starting value for c.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if a or b or c are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for HaMad estimators is based on `optim` where `MAX` is used to control the constraints on a, b and c. The optimal values of the tuning constants a, b, and c can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

Andrews, D.F., Bickel, P.J., Hampel, F.R., Huber, P.J., Rogers, W.H. and Tukey, J.W. (1972) *Robust estimates of location*. Princeton University Press.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.HaMad(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.Hu1` *Computation of the optimally robust IC for Hu1 estimators*

Description

The function `rlsOptIC.Hu1` computes the optimally robust IC for Hu1 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators were proposed by Huber (1964), Proposal 2. A definition of these estimators can also be found in Subsection 8.5.1 of Kohl (2005).

Usage

```
rlsOptIC.Hu1(r, kUp = 2.5, delta = 1e-06)
```

Arguments

`r`	non-negative real: neighborhood radius.
`kUp`	positive real: the upper end point of the interval to be searched for k.
`delta`	the desired accuracy (convergence tolerance).

Details

The optimal value of the tuning constant k can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

Huber, P.J. (1964) Robust estimation of a location parameter. Ann. Math. Stat. **35**: 73–101.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Hu1(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.Hu2` *Computation of the optimally robust IC for Hu2 estimators*

Description

The function `rlsOptIC.Hu2` computes the optimally robust IC for Hu2 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators were proposed in Example 6.4.1 of Huber (1981). A definition of these estimators can also be found in Subsection 8.5.1 of Kohl (2005).

Usage

```
rlsOptIC.Hu2(r, k.start = 1.5, c.start = 1.5, delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`k.start`	positive real: starting value for k.
`c.start`	positive real: starting value for c.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if k1 or k2 are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for Hu2 estimators is based on `optim` where `MAX` is used to control the constraints on k and c. The optimal values of the tuning constants k and c can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Hu2(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.Hu2a` *Computation of the optimally robust IC for Hu2a estimators*

Description

The function `rlsOptIC.Hu2a` computes the optimally robust IC for Hu2a estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators are a simple modification of Huber (1964), Proposal 2 where we, in addition, admit a clipping from below. The definition of these estimators can be found in Subsection 8.5.1 of Kohl (2005).

Usage

```
rlsOptIC.Hu2a(r, k1.start = 0.25, k2.start = 2.5, delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`k1.start`	positive real: starting value for k1.
`k2.start`	positive real: starting value for k2.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if k1 or k2 are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for Hu2a estimators is based on `optim` where `MAX` is used to control the constraints on k1 and k2. The optimal values of the tuning constants k1 and k2 can be read off from the slot `Infos` of the resulting IC.

Value

Object of class "IC"

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Huber, P.J. (1964) Robust estimation of a location parameter. Ann. Math. Stat. **35**: 73–101.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Hu2a(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

---

rlsOptIC.Hu3 *Computation of the optimally robust IC for Hu3 estimators*

Description

The function rlsOptIC.Hu3 computes the optimally robust IC for Hu3 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.1 of Kohl (2005).

Usage

```
rlsOptIC.Hu3(r, k.start = 1, c1.start = 0.1, c2.start = 0.5,
             delta = 1e-06, MAX = 100)
```

Arguments

r	non-negative real: neighborhood radius.
k.start	positive real: starting value for k.
c1.start	positive real: starting value for c1.
c2.start	positive real: starting value for c2.
delta	the desired accuracy (convergence tolerance).
MAX	if k or c1 or c2 are beyond the admitted values, MAX is returned.

Details

The computation of the optimally robust IC for Hu2 estimators is based on `optim` where `MAX` is used to control the constraints on k, c1 and c2. The optimal values of the tuning constants k, c1 and c2 can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Hu3(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.HuMad` *Computation of the optimally robust IC for HuMad estimators*

Description

The function `rlsOptIC.HuMad` computes the optimally robust IC for HuMad estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators were proposed by Andrews et al. (1972), p. 12. A definition of these estimators can also be found in Subsection 8.5.1 of Kohl (2005).

Usage

```
rlsOptIC.HuMad(r, kUp = 2.5, delta = 1e-06)
```

Arguments

r	non-negative real: neighborhood radius.
kUp	positive real: the upper end point of the interval to be searched for k.
delta	the desired accuracy (convergence tolerance).

Details

The optimal value of the tuning constant k can be read off from the slot Infos of the resulting IC.

Value

Object of class "IC"

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Andrews, D.F., Bickel, P.J., Hampel, F.R., Huber, P.J., Rogers, W.H. and Tukey, J.W. (1972) *Robust estimates of location*. Princeton University Press.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.HuMad(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

---

rlsOptIC.M *Computation of the optimally robust IC for M estimators*

Description

The function rlsOptIC.M computes the optimally robust IC for M estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Section 8.3 of Kohl (2005).

Usage

```
rlsOptIC.M(r, ggLo = 0.5, ggUp = 1.5, a1.start = 0.75, a3.start = 0.25,
           bUp = 1000, delta = 1e-05, itmax = 100, check = FALSE)
```

Arguments

r	non-negative real: neighborhood radius.
ggLo	non-negative real: the lower end point of the interval to be searched for γ.
ggUp	positive real: the upper end point of the interval to be searched for γ.
a1.start	real: starting value for α_1.
a3.start	real: starting value for α_3.
bUp	positive real: upper bound used in the computation of the optimal clipping bound b.
delta	the desired accuracy (convergence tolerance).
itmax	the maximum number of iterations.
check	logical. Should constraints be checked.

Details

The optimal values of the tuning constants α_1, α_3, b and γ can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Huber, P.J. (1981) *Robust Statistics*. New York: Wiley.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.M(r = 0.1, check = TRUE)
distrExOptions("ErelativeTolerance" = 1e-12)
checkIC(IC1, NormLocationScaleFamily())
distrExOptions("ErelativeTolerance" = .Machine$double.eps^0.25)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.MM2` *Computation of the optimally robust IC for MM2 estimators*

Description

The function `rlsOptIC.MM2` computes the optimally robust IC for MM2 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. These estimators are based on a proposal of Fraiman et al. (2001), p. 206. A definition of these estimators can also be found in Section 8.6 of Kohl (2005).

Usage

```
rlsOptIC.MM2(r, c.start = 1.5, d.start = 2, delta = 1e-06, MAX = 100)
```

Arguments

`r`	non-negative real: neighborhood radius.
`c.start`	positive real: starting value for c.
`d.start`	positive real: starting value for d.
`delta`	the desired accuracy (convergence tolerance).
`MAX`	if a or k are beyond the admitted values, `MAX` is returned.

Details

The computation of the optimally robust IC for MM2 estimators is based on `optim` where `MAX` is used to control the constraints on c and d. The optimal values of the tuning constants c and d can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl `<Matthias.Kohl@stamats.de>`

References

Fraiman, R., Yohai, V.J. and Zamar, R.H. (2001) Optimal robust M-estimates of location. Ann. Stat. **29**(1): 194-223.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.MM2(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

`rlsOptIC.Tu1` *Computation of the optimally robust IC for Tu1 estimators*

Description

The function `rlsOptIC.Tu1` computes the optimally robust IC for Tu1 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.4 of Kohl (2005).

Usage

```
rlsOptIC.Tu1(r, aUp = 10, delta = 1e-06)
```

Arguments

`r`	non-negative real: neighborhood radius.
`aUp`	positive real: the upper end point of the interval to be searched for a.
`delta`	the desired accuracy (convergence tolerance).

Details

The optimal value of the tuning constant a can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Beaton, A.E. and Tukey, J.W. (1974) The fitting of power series, meaning polynomials, illustrated on band-spectroscopic data. Discussions. Technometrics **16**: 147–185.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Tu1(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

---

rlsOptIC.Tu2 *Computation of the optimally robust IC for Tu2 estimators*

Description

The function rlsOptIC.Tu2 computes the optimally robust IC for Tu2 estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.4 of Kohl (2005).

Usage

```
rlsOptIC.Tu2(r, a.start = 5, k.start = 1.5, delta = 1e-06, MAX = 100)
```

Arguments

r	non-negative real: neighborhood radius.
a.start	positive real: starting value for a.
k.start	positive real: starting value for k.
delta	the desired accuracy (convergence tolerance).
MAX	if a or k are beyond the admitted values, MAX is returned.

Details

The computation of the optimally robust IC for Tu2 estimators is based on `optim` where `MAX` is used to control the constraints on a and k. The optimal values of the tuning constant a and k can be read off from the slot `Infos` of the resulting IC.

Value

Object of class `"IC"`

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Beaton, A.E. and Tukey, J.W. (1974) The fitting of power series, meaning polynomials, illustrated on band-spectroscopic data. Discussions. Technometrics **16**: 147–185.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.Tu2(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

---

rlsOptIC.TuMad *Computation of the optimally robust IC for TuMad estimators*

Description

The function `rlsOptIC.TuMad` computes the optimally robust IC for TuMad estimators in case of normal location with unknown scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Subsection 8.5.4 of Kohl (2005).

Usage

```
rlsOptIC.TuMad(r, aUp = 10, delta = 1e-06)
```

Arguments

r	non-negative real: neighborhood radius.
aUp	positive real: the upper end point of the interval to be searched for a.
delta	the desired accuracy (convergence tolerance).

Details

The optimal value of the tuning constant a can be read off from the slot Infos of the resulting IC.

Value

Object of class "IC"

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Beaton, A.E. and Tukey, J.W. (1974) The fitting of power series, meaning polynomials, illustrated on band-spectroscopic data. Discussions. Technometrics **16**: 147–185.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

IC-class

Examples

```
IC1 <- rlsOptIC.TuMad(r = 0.1)
checkIC(IC1)
Risks(IC1)
Infos(IC1)
plot(IC1)
infoPlot(IC1)
```

---

roblox *Optimally robust estimator for location and/or scale*

Description

The function roblox computes the optimally robust estimator and corresponding IC for normal location und/or scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Rieder (1994) or Kohl (2005), respectively.

Usage

```
roblox(x, mean, sd, eps, eps.lower, eps.upper, initial.est, k = 1L,
       fsCor = TRUE, returnIC = FALSE, mad0 = 1e-4, na.rm = TRUE)
```

Arguments

x	vector x of data values, may also be a matrix or data.frame with one row, respectively one column/(numeric) variable.
mean	specified mean.
sd	specified standard deviation which has to be positive.
eps	positive real (0 < eps <= 0.5): amount of gross errors. See details below.
eps.lower	positive real (0 <= eps.lower <= eps.upper): lower bound for the amount of gross errors. See details below.
eps.upper	positive real (eps.lower <= eps.upper <= 0.5): upper bound for the amount of gross errors. See details below.
initial.est	initial estimate for mean and/or sd. If missing median and/or MAD are used.
k	positive integer. k-step is used to compute the optimally robust estimator.
fsCor	logical: perform finite-sample correction. See function finiteSampleCorrection.
returnIC	logical: should IC be returned. See details below.
mad0	scale estimate used if computed MAD is equal to zero
na.rm	logical: if TRUE, the estimator is evaluated at complete.cases(x).

Details

Computes the optimally robust estimator for location with scale specified, scale with location specified, or both if neither is specified. The computation uses a k-step construction with an appropriate initial estimate for location or scale or location and scale, respectively. Valid candidates are e.g. median and/or MAD (default) as well as Kolmogorov(-Smirnov) or von Mises minimum distance estimators; cf. Rieder (1994) and Kohl (2005).

If the amount of gross errors (contamination) is known, it can be specified by eps. The radius of the corresponding infinitesimal contamination neighborhood is obtained by multiplying eps by the square root of the sample size.

If the amount of gross errors (contamination) is unknown, try to find a rough estimate for the amount of gross errors, such that it lies between eps.lower and eps.upper.

In case eps.lower is specified and eps.upper is missing, eps.upper is set to 0.5. In case eps.upper is specified and eps.lower is missing, eps.lower is set to 0.

If neither eps nor eps.lower and/or eps.upper is specified, eps.lower and eps.upper are set to 0 and 0.5, respectively.

If eps is missing, the radius-minimax estimator in sense of Rieder et al. (2008), respectively Section 2.2 of Kohl (2005) is returned.

In case of location, respectively scale one additionally has to specify sd, respectively mean where sd and mean have to be a single number.

For sample size <= 2, median and/or MAD are used for estimation.

If eps = 0, mean and/or sd are computed. In this situation it's better to use function MLEstimator.

Value

Object of class "kStepEstimate".

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

H. Rieder (1994): Robust Asymptotic Statistics. Springer. doi:10.1007/9781468406245

H. Rieder, M. Kohl, and P. Ruckdeschel (2008). The Costs of Not Knowing the Radius. Statistical Methods and Applications *17*(1): 13-40. doi:10.1007/s1026000700477

M. Kohl, P. Ruckdeschel, and H. Rieder (2010). Infinitesimally Robust Estimation in General Smoothly Parametrized Models. Statistical Methods and Applications *19*(3): 333-354. doi:10.1007/s1026001001330.

M. Kohl and H.P. Deigner (2010). Preprocessing of gene expression data by optimally robust estimators. BMC Bioinformatics *11*, 583. doi:10.1186/1471210511583.

See Also

ContIC-class, rlOptIC, rsOptIC, rlsOptIC.AL, kStepEstimate-class, roptest

Examples

```
ind <- rbinom(100, size=1, prob=0.05)
x <- rnorm(100, mean=ind*3, sd=(1-ind) + ind*9)

## amount of gross errors known
res1 <- roblox(x, eps = 0.05, returnIC = TRUE)
estimate(res1)
## don't run to reduce check time on CRAN
## Not run:
confint(res1)
confint(res1, method = symmetricBias())
pIC(res1)
checkIC(pIC(res1))
Risks(pIC(res1))
Infos(pIC(res1))
plot(pIC(res1))
infoPlot(pIC(res1))

## End(Not run)

## amount of gross errors unknown
res2 <- roblox(x, eps.lower = 0.01, eps.upper = 0.1, returnIC = TRUE)
estimate(res2)
## don't run to reduce check time on CRAN
```

```
## Not run:
confint(res2)
confint(res2, method = symmetricBias())
pIC(res2)
checkIC(pIC(res2))
Risks(pIC(res2))
Infos(pIC(res2))
plot(pIC(res2))
infoPlot(pIC(res2))

## End(Not run)

## estimator comparison
# classical optimal (non-robust)
c(mean(x), sd(x))

# most robust
c(median(x), mad(x))

# optimally robust (amount of gross errors known)
estimate(res1)

# optimally robust (amount of gross errors unknown)
estimate(res2)

# Kolmogorov(-Smirnov) minimum distance estimator (robust)
(ks.est <- MDEstimator(x, ParamFamily = NormLocationScaleFamily()))

# optimally robust (amount of gross errors known)
roblox(x, eps = 0.05, initial.est = estimate(ks.est))

# Cramer von Mises minimum distance estimator (robust)
(CvM.est <- MDEstimator(x, ParamFamily = NormLocationScaleFamily(), distance = CvMDist))

# optimally robust (amount of gross errors known)
roblox(x, eps = 0.05, initial.est = estimate(CvM.est))
```

`rowRoblox and colRoblox`

Optimally robust estimation for location and/or scale

Description

The functions `rowRoblox` and `colRoblox` compute optimally robust estimates for normal location und/or scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Rieder (1994) or Kohl (2005), respectively.

Usage

```
rowRoblox(x, mean, sd, eps, eps.lower, eps.upper, initial.est, k = 1L,
```

```
          fsCor = TRUE, mad0 = 1e-4, na.rm = TRUE)
colRoblox(x, mean, sd, eps, eps.lower, eps.upper, initial.est, k = 1L,
          fsCor = TRUE, mad0 = 1e-4, na.rm = TRUE)
```

Arguments

x	matrix or data.frame of (numeric) data values.
mean	specified mean. See details below.
sd	specified standard deviation which has to be positive. See also details below.
eps	positive real (0 < eps <= 0.5): amount of gross errors. See details below.
eps.lower	positive real (0 <= eps.lower <= eps.upper): lower bound for the amount of gross errors. See details below.
eps.upper	positive real (eps.lower <= eps.upper <= 0.5): upper bound for the amount of gross errors. See details below.
initial.est	initial estimate for mean and/or sd. If missing median and/or MAD are used.
k	positive integer. k-step is used to compute the optimally robust estimator.
fsCor	logical: perform finite-sample correction. See function finiteSampleCorrection.
mad0	scale estimate used if computed MAD is equal to zero
na.rm	logical: if TRUE, the estimator is evaluated at complete.cases(x).

Details

Computes the optimally robust estimator for location with scale specified, scale with location specified, or both if neither is specified. The computation uses a k-step construction with an appropriate initial estimate for location or scale or location and scale, respectively. Valid candidates are e.g. median and/or MAD (default) as well as Kolmogorov(-Smirnov) or Cram\'er von Mises minimum distance estimators; cf. Rieder (1994) and Kohl (2005). In case package Biobase from Bioconductor is installed as is suggested, median and/or MAD are computed using function rowMedians.

These functions are optimized for the situation where one has a matrix and wants to compute the optimally robust estimator for every row, respectively column of this matrix. In particular, the amount of cross errors is assumed to be constant for all rows, respectively columns.

If the amount of gross errors (contamination) is known, it can be specified by eps. The radius of the corresponding infinitesimal contamination neighborhood is obtained by multiplying eps by the square root of the sample size.

If the amount of gross errors (contamination) is unknown, try to find a rough estimate for the amount of gross errors, such that it lies between eps.lower and eps.upper.

In case eps.lower is specified and eps.upper is missing, eps.upper is set to 0.5. In case eps.upper is specified and eps.lower is missing, eps.lower is set to 0.

If neither eps nor eps.lower and/or eps.upper is specified, eps.lower and eps.upper are set to 0 and 0.5, respectively.

If eps is missing, the radius-minimax estimator in sense of Rieder et al. (2008), respectively Section 2.2 of Kohl (2005) is returned.

In case of location, respectively scale one additionally has to specify sd, respectively mean where sd and mean can be a single number, i.e., identical for all rows, respectively columns, or a vector with length identical to the number of rows, respectively columns.

For sample size <= 2, median and/or MAD are used for estimation.

If eps = 0, mean and/or sd are computed.

Value

Object of class "kStepEstimate".

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

H. Rieder (1994): Robust Asymptotic Statistics. Springer. doi:10.1007/9781468406245

H. Rieder, M. Kohl, and P. Ruckdeschel (2008). The Costs of Not Knowing the Radius. Statistical Methods and Applications *17*(1): 13-40. doi:10.1007/s1026000700477

M. Kohl, P. Ruckdeschel, and H. Rieder (2010). Infinitesimally Robust Estimation in General Smoothly Parametrized Models. Statistical Methods and Applications *19*(3): 333-354. doi:10.1007/s1026001001330.

M. Kohl and H.P. Deigner (2010). Preprocessing of gene expression data by optimally robust estimators. BMC Bioinformatics *11*, 583. doi:10.1186/1471210511583.

See Also

roblox, kStepEstimate-class

Examples

```
ind <- rbinom(200, size=1, prob=0.05)
X <- matrix(rnorm(200, mean=ind*3, sd=(1-ind) + ind*9), nrow = 2)
rowRoblox(X)
rowRoblox(X, k = 3)
rowRoblox(X, eps = 0.05)
rowRoblox(X, eps = 0.05, k = 3)

X1 <- t(X)
colRoblox(X1)
colRoblox(X1, k = 3)
colRoblox(X1, eps = 0.05)
colRoblox(X1, eps = 0.05, k = 3)

X2 <- rbind(rnorm(100, mean = -2, sd = 3), rnorm(100, mean = -1, sd = 4))
rowRoblox(X2, sd = c(3, 4))
rowRoblox(X2, eps = 0.03, sd = c(3, 4))
```

```
rowRoblox(X2, sd = c(3, 4), k = 4)
rowRoblox(X2, eps = 0.03, sd = c(3, 4), k = 4)

X3 <- cbind(rnorm(100, mean = -2, sd = 3), rnorm(100, mean = 1, sd = 2))
colRoblox(X3, mean = c(-2, 1))
colRoblox(X3, eps = 0.02, mean = c(-2, 1))
colRoblox(X3, mean = c(-2, 1), k = 4)
colRoblox(X3, eps = 0.02, mean = c(-2, 1), k = 4)
```

`rsOptIC` *Computation of the optimally robust IC for AL estimators*

Description

The function `rsOptIC` computes the optimally robust IC for AL estimators in case of normal scale and (convex) contamination neighborhoods. The definition of these estimators can be found in Rieder (1994) or Kohl (2005), respectively.

Usage

```
rsOptIC(r, mean = 0, sd = 1, bUp = 1000, delta = 1e-06, itmax = 100, computeIC = TRUE)
```

Arguments

`r`	non-negative real: neighborhood radius.
`mean`	specified mean.
`sd`	specified standard deviation.
`bUp`	positive real: the upper end point of the interval to be searched for the clipping bound b.
`delta`	the desired accuracy (convergence tolerance).
`itmax`	the maximum number of iterations.
`computeIC`	logical: should IC be computed. See details below.

Details

If 'computeIC' is 'FALSE' only the Lagrange multipliers 'A', 'a', and 'b' contained in the optimally robust IC are computed.

Value

If 'computeIC' is 'TRUE' an object of class `"ContIC"` is returned, otherwise a list of Lagrange multipliers

`A`	standardizing constant
`a`	centering constant
`b`	optimal clipping bound

Author(s)

Matthias Kohl <Matthias.Kohl@stamats.de>

References

Rieder, H. (1994) *Robust Asymptotic Statistics*. New York: Springer.

M. Kohl (2005). Numerical Contributions to the Asymptotic Theory of Robustness. Dissertation. University of Bayreuth. https://epub.uni-bayreuth.de/id/eprint/839/2/DissMKohl.pdf.

See Also

ContIC-class, roblox

Examples

```
IC1 <- rsOptIC(r = 0.1)
distrExOptions("ErelativeTolerance" = 1e-12)
checkIC(IC1)
distrExOptions("ErelativeTolerance" = .Machine$double.eps^0.25) # default
Risks(IC1)
cent(IC1)
clip(IC1)
stand(IC1)
plot(IC1)
```

---

showdown *Estimator Showdown by Monte-Carlo Study.*

Description

The function showdown can be used to perform Monte-Carlo studies comparing a competitor with rmx estimators in case of normal location and scale. In addition, maximum likelihood (ML) estimators (mean and sd) and median and MAD are computed. The comparison is based on the empirical MSE.

Usage

```
showdown(n, M, eps, contD, seed = 123, estfun, estMean, estSd,
         eps.lower = 0, eps.upper = 0.05, steps = 3L, fsCor = TRUE,
         plot1 = FALSE, plot2 = FALSE, plot3 = FALSE)
```

Arguments

n	integer; sample size, should be at least 3.
M	integer; Monte-Carlo replications.
eps	amount of contamination in [0, 0.5].
contD	object of class "UnivariateDistribution"; contaminating distribution.

seed	random seed.
estfun	function to compute location and scale estimator; see details below.
estMean	function to compute location estimator; see details below.
estSd	function to compute scale estimator; see details below.
eps.lower	used by rmx estimator.
eps.upper	used by rmx estimator.
steps	integer; steps used for estimator construction.
fsCor	logical; use finite-sample correction.
plot1	logical; plot cdf of ideal and real distribution.
plot2	logical; plot 20 (or M if M < 20) randomly selected samples.
plot3	logical; generate boxplots of the results.

Details

Normal location and scale with mean = 0 and sd = 1 is used as ideal model (without restriction due to equivariance).

Since there is no estimator which yields reliable results if 50 percent or more of the observations are contaminated, we use a modification where we re-simulate all samples including at least 50 percent contaminated data.

If `estfun` is specified it has to compute and return a location and scale estimate (vector of length 2). One can also specify the location and scale estimator separately by using `estMean` and `estSd` where `estMean` computes and returns the location estimate and `estSd` the scale estimate.

We use funtion `rowRoblox` for the computation of the rmx estimator.

Value

Data.frame including empirical MSE (standardized by sample size n) and relMSE with respect to the rmx estimator.

Author(s)

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References

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See Also

rowRoblox

Examples

```
library(MASS)
## compare with Huber's Proposal 2
showdown(n = 20, M = 100, eps = 0.02, contD = Norm(mean = 3, sd = 3),
         estfun = function(x){ unlist(hubers(x)) },
         plot1 = TRUE, plot2 = TRUE, plot3 = TRUE)

## compare with Huber M estimator with MAD scale
showdown(n = 20, M = 100, eps = 0.02, contD = Norm(mean = 3, sd = 3),
         estfun = function(x){ unlist(huber(x)) },
         plot1 = TRUE, plot2 = TRUE, plot3 = TRUE)
```

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