

# Package ‘prettyglm’

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**Type** Package

**Title** Pretty Summaries of Generalized Linear Model Coefficients

**Version** 1.0.1

**Maintainer** Jared Fowler <jared.fowler8@gmail.com>

**Description** One of the main advantages of using Generalised Linear Models is their interpretability. The goal of 'prettyglm' is to provide a set of functions which easily create beautiful coefficient summaries which can readily be shared and explained. 'prettyglm' helps users create coefficient summaries which include categorical base levels, variable importance and type III p.values. 'prettyglm' also creates beautiful relativity plots for categorical, continuous and splined coefficients.

**License** GPL-3

**URL** <https://jared-fowler.github.io/prettyglm/>

**Depends** R (>= 4.1.0)

**Imports** broom, car, dplyr, forcats, kableExtra, knitr, methods, plotly, RColorBrewer, stringr, tibble, tidycat, tidyr, tidyselect, vip

**Suggests** rmarkdown, testthat

**VignetteBuilder** knitr

**Encoding** UTF-8

**LazyData** true

**RoxygenNote** 7.2.3

**NeedsCompilation** no

**Author** Jared Fowler [cre, aut]

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**R topics documented:**

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actual\_expected\_bucketed  
*actual\_expected\_bucketed*

---

**Description**

Provides a rank plot of the actual and predicted.

**Usage**

```
actual_expected_bucketed(
  target_variable,
  model_object,
  data_set = NULL,
  number_of_buckets = 25,
  ylab = "Target",
  width = 800,
  height = 500,
  first_colour = "black",
  second_colour = "#cc4678",
  facetby = NULL,
  prediction_type = "response",
  predict_function = NULL,
  return_data = F
)
```

**Arguments**

target\_variable      String of target variable name.

model\_object        GLM model object.

<code>data_set</code>	Data to score the model on. This can be training or test data, as long as the data is in a form where the model object can make predictions. Currently developing ability to provide custom prediction functions, currently implementation defaults to 'stats::predict'
<code>number_of_buckets</code>	number of buckets for percentile
<code>ylab</code>	Y-axis label.
<code>width</code>	plotly plot width in pixels.
<code>height</code>	plotly plot height in pixels.
<code>first_colour</code>	First colour to plot, usually the colour of actual.
<code>second_colour</code>	Second colour to plot, usually the colour of predicted.
<code>facetby</code>	variable user wants to facet by.
<code>prediction_type</code>	Prediction type to be pasted to predict.glm if predict_function is NULL. Defaults to "response".
<code>predict_function</code>	prediction function to use. Still in development.
<code>return_data</code>	Logical to return cleaned data set instead of plot.

**Value**

plot Plotly plot by default. ggplot if plotlyplot = F. Tibble if return\_data = T.

**Examples**

```
library(dplyr)
library(prettyglm)

data('titanic')

columns_to_factor <- c('Pclass',
                      'Sex',
                      'Cabin',
                      'Embarked',
                      'Cabintype',
                      'Survived')

meanage <- base::mean(titanic$Age, na.rm=TRUE)

titanic <- titanic %>%
  dplyr::mutate_at(columns_to_factor, list(~factor(.))) %>%
  dplyr::mutate(Age =base::ifelse(is.na(Age)==TRUE,meanage,Age)) %>%
  dplyr::mutate(Age_0_25 = prettyglm::splineit(Age,0,25),
               Age_25_50 = prettyglm::splineit(Age,25,50),
               Age_50_120 = prettyglm::splineit(Age,50,120)) %>%
  dplyr::mutate(Fare_0_250 = prettyglm::splineit(Fare,0,250),
               Fare_250_600 = prettyglm::splineit(Fare,250,600))
```

```
survival_model <- stats::glm(Survived ~
                             Sex:Age +
                             Fare +
                             Embarked +
                             SibSp +
                             Parch +
                             Cabintype,
                             data = titanic,
                             family = binomial(link = 'logit'))

prettyglm::actual_expected_bucketed(target_variable = 'Survived',
                                    model_object = survival_model,
                                    data_set = titanic)
```

---

bank\_data

*Bank marketing campaigns data set analysis*

---

## Description

It is a dataset that describing Portugal bank marketing campaigns results. Conducted campaigns were based mostly on direct phone calls, offering bank client to place a term deposit. If after all marking efforts client had agreed to place deposit - target variable marked 'yes', otherwise 'no'

## Usage

```
data(bank)
```

## Format

An object of class "data.frame"

**job** Type of job

**marital** marital status

**education** education

**default** has credit in default?

**housing** has housing loan?

**loan** has personal loan?

**age** age

**y** has the client subscribed a term deposit? (binary: "yes","no")

## Details

Source of the data <https://archive.ics.uci.edu/ml/datasets/bank+marketing>

## References

This dataset is public available for research. The details are described in S. Moro, P. Cortez and P. Rita. A Data-Driven Approach to Predict the Success of Bank Telemarketing. Decision Support Systems, Elsevier, 62:22-31, June 2014

## Examples

```
data(bank)
head(bank_data)
```

---

```
clean_coefficients    clean_coefficients
```

---

## Description

Processing to split out base levels and add variable importance to each term. Inspired by 'tidy-cat::tidy\_categorical()', modified for use in prettyglm..

## Usage

```
clean_coefficients(
  d = NULL,
  m = NULL,
  vimethod = "model",
  spline_seperator = NULL,
  ...
)
```

## Arguments

d	Data frame <a href="#">tibble</a> output from <a href="#">tidy.lm</a> ; with one row for each term in the regression, including column 'term'
m	Model object <a href="#">glm</a>
vimethod	Variable importance method. Still in development
spline_seperator	Sting of the spline separator. For example AGE_0_25 would be "_"
...	Any additional parameters to be past to <a href="#">vi</a>

## Value

Expanded [tibble](#) from the version passed to 'd' including additional columns:

variable	The name of the variable that the regression term belongs to.
level	The level of the categorical variable that the regression term belongs to. Will be an the term name for numeric variables.

**Author(s)**

Jared Fowler, Guy J. Abel

**See Also**

[tidy.lm](#)

---

cut3

*cut3*

---

**Description**

Hmisc::cut2 bones repackaged to remove errors with importing Hmisc

**Usage**

```
cut3(
  x,
  cuts,
  m = 150,
  g,
  digits,
  minmax = TRUE,
  oneval = TRUE,
  onlycuts = FALSE,
  formatfun = format,
  ...
)
```

**Arguments**

x	numeric vector to classify into intervals.
cuts	cut points.
m	desired minimum number of observations in a group. The algorithm does not guarantee that all groups will have at least m observations.
g	number of quantile groups
digits	number of significant digits to use in constructing levels.
minmax	if cuts is specified but $\min(x) < \min(\text{cuts})$ or $\max(x) > \max(\text{cuts})$ , augments cuts to include min and max x
oneval	if an interval contains only one unique value, the interval will be labeled with the formatted version of that value instead of the interval endpoints, unless oneval=FALSE
onlycuts	set to TRUE to only return the vector of computed cuts. This consists of the interior values plus outer ranges.
formatfun	format function
...	additional arguments passed to formatfun

**Value**

vector of cut

---

one_way_ave	<i>one_way_ave</i>
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---

**Description**

Creates a pretty html plot of one way actual vs expected by specified predictor.

**Usage**

```
one_way_ave(
  feature_to_plot,
  model_object,
  target_variable,
  data_set,
  plot_type = "predictions",
  plot_factor_as_numeric = FALSE,
  ordering = NULL,
  width = 800,
  height = 500,
  number_of_buckets = 30,
  first_colour = "black",
  second_colour = "#cc4678",
  facetby = NULL,
  prediction_type = "response",
  predict_function = NULL,
  upper_percentile_to_cut = 0.01,
  lower_percentile_to_cut = 0
)
```

**Arguments**

feature_to_plot	A string of the variable to plot.
model_object	Model object to create coefficient table for. Must be of type: <a href="#">glm</a> , <a href="#">lm</a>
target_variable	String of target variable name in dataset.
data_set	Data set to calculate the actual vs expected for. If no input default is to try and extract training data from model object.
plot_type	one of "Residual", "predictions" or "actuals" defaults to "predictions"
plot_factor_as_numeric	Set to TRUE to return <a href="#">data.frame</a> instead of creating <a href="#">kable</a> .

ordering	Option to change the ordering of categories on the x axis, only for discrete categories. Default to the ordering of the factor. Other options are: 'alphabetical', 'Number of records', 'Average Value'
width	Width of plot
height	Height of plot
number_of_buckets	Number of buckets for continuous variable plots
first_colour	First colour to plot, usually the colour of actual.
second_colour	Second colour to plot, usually the colour of predicted.
facetby	Variable to facet the actual vs expect plots by.
prediction_type	Prediction type to be pasted to predict.glm if predict_function is NULL. Defaults to "response".
predict_function	A custom prediction function can be provided here. It must return a <a href="#">data.frame</a> with an "Actual_Values" column, and a "Predicted_Values" column.
upper_percentile_to_cut	For continuous variables this is what percentile to exclude from the upper end of the distribution. Defaults to 0.01, so the maximum percentile of the variable in the plot will be 0.99. Cutting off some of the distribution can help the views if outlier's are present in the data.
lower_percentile_to_cut	For continuous variables this is what percentile to exclude from the lower end of the distribution. Defaults to 0.01, so the minimum percentile of the variable in the plot will be 0.01. Cutting off some of the distribution can help the views if outlier's are present in the data.

## Value

plotly plot of one way actual vs expected.

## Examples

```
library(dplyr)
library(prettyglm)
data('titanic')
columns_to_factor <- c('Pclass',
                       'Sex',
                       'Cabin',
                       'Embarked',
                       'Cabintype',
                       'Survived')
meanage <- base::mean(titanic$Age, na.rm=TRUE)

titanic <- titanic %>%
  dplyr::mutate_at(columns_to_factor, list(~factor(.))) %>%
  dplyr::mutate(Age =base::ifelse(is.na(Age)==TRUE,meanage,Age)) %>%
  dplyr::mutate(Age_0_25 = prettyglm::splineit(Age,0,25),
```

```

    Age_25_50 = prettyglm::splineit(Age,25,50),
    Age_50_120 = prettyglm::splineit(Age,50,120)) %>%
dplyr::mutate(Fare_0_250 = prettyglm::splineit(Fare,0,250),
    Fare_250_600 = prettyglm::splineit(Fare,250,600))

survival_model <- stats::glm(Survived ~
    Sex:Age +
    Fare +
    Embarked +
    SibSp +
    Parch +
    Cabintype,
    data = titanic,
    family = binomial(link = 'logit'))

# Continuous Variable Example
one_way_ave(feature_to_plot = 'Age',
    model_object = survival_model,
    target_variable = 'Survived',
    data_set = titanic,
    number_of_buckets = 20,
    upper_percentile_to_cut = 0.1,
    lower_percentile_to_cut = 0.1)

# Discrete Variable Example
one_way_ave(feature_to_plot = 'Pclass',
    model_object = survival_model,
    target_variable = 'Survived',
    data_set = titanic)

# Custom Predict Function and facet
a_custom_predict_function <- function(target, model_object, dataset){
  dataset <- base::as.data.frame(dataset)
  Actual_Values <- dplyr::pull(dplyr::select(dataset, tidyselect::all_of(c(target))))
  if(class(Actual_Values) == 'factor'){
    Actual_Values <- base::as.numeric(as.character(Actual_Values))
  }
  Predicted_Values <- base::as.numeric(stats::predict(model_object, dataset, type='response'))

  to_return <- base::data.frame(Actual_Values = Actual_Values,
    Predicted_Values = Predicted_Values)

  to_return <- to_return %>%
  dplyr::mutate(Predicted_Values = base::ifelse(Predicted_Values > 0.3,0.3,Predicted_Values))
  return(to_return)
}

one_way_ave(feature_to_plot = 'Age',
    model_object = survival_model,
    target_variable = 'Survived',
    data_set = titanic,
    number_of_buckets = 20,
    upper_percentile_to_cut = 0.1,

```

```

lower_percentile_to_cut = 0.1,
predict_function = a_custom_predict_function,
facetby = 'Pclass')

```

---

predict_outcome	<i>predict_outcome</i>
-----------------	------------------------

---

### Description

Processing to predict response for various actual vs expected plots

### Usage

```

predict_outcome(
  target,
  model_object,
  dataset,
  prediction_type = NULL,
  weights = NULL
)

```

### Arguments

target	String of target variable name.
model_object	Model object. prettyglm currently supports
dataset	This is used to plot the number in each class as a barchart if plotly is TRUE.
prediction_type	type of prediction to be passed to the model object. For ...GLM defaults to ...
weights	weightings to be provided to predictions if required.

### Value

dataframe	Returns a dataframe of Actual and Predicted Values
-----------	--

### Author(s)

Jared Fowler

### See Also

[tidy.lm](#)

---

```
pretty_coefficients  pretty_coefficients
```

---

## Description

Creates a pretty kable of model coefficients including coefficient base levels, type III P.values, and variable importance.

## Usage

```
pretty_coefficients(
  model_object,
  relativity_transform = NULL,
  relativity_label = "relativity",
  type_iii = NULL,
  conf.int = FALSE,
  vimethod = "model",
  spline_seperator = NULL,
  significance_level = 0.05,
  return_data = FALSE,
  ...
)
```

## Arguments

<code>model_object</code>	Model object to create coefficient table for. Must be of type: <a href="#">glm</a> , <a href="#">lm</a> .
<code>relativity_transform</code>	String of the function to be applied to the model estimate to calculate the relativity, for example: 'exp(estimate)-1'. Default is for relativity to be excluded from output.
<code>relativity_label</code>	String of label to give to relativity column if you want to change the title to your use case.
<code>type_iii</code>	Type III statistical test to perform. Default is none. Options are 'Wald' or 'LR'. Warning 'LR' can be computationally expensive. Test performed via <a href="#">Anova</a>
<code>conf.int</code>	Set to TRUE to include confidence intervals in summary table. Warning, can be computationally expensive.
<code>vimethod</code>	Variable importance method to pass to method of <a href="#">vi</a> . Defaults to "model". Currently supports "permute" and "firm", pass any additional arguments to <a href="#">vi</a> in ...
<code>spline_seperator</code>	Separator to look for to identify a spline. If this input is not null, it is assumed any features with this separator are spline columns. For example an age spline from 0 to 25 you could use: AGE_0_25 and "_".
<code>significance_level</code>	Significance level to P-values by in kable. Defaults to 0.05.

return\_data      Set to TRUE to return `data.frame` instead of creating `kable`.  
 ...              Any additional parameters to be past to `vi`

### Value

`kable` if `return_data = FALSE`. `data.frame` if `return_data = TRUE`.

### Examples

```
library(dplyr)
library(prettyglm)
data('titanic')
columns_to_factor <- c('Pclass',
                       'Sex',
                       'Cabin',
                       'Embarked',
                       'Cabintype',
                       'Survived')
meanage <- base::mean(titanic$Age, na.rm=TRUE)

titanic <- titanic %>%
  dplyr::mutate_at(columns_to_factor, list(~factor(.))) %>%
  dplyr::mutate(Age =base::ifelse(is.na(Age)==TRUE,meanage,Age)) %>%
  dplyr::mutate(Age_0_25 = prettyglm::splineit(Age,0,25),
               Age_25_50 = prettyglm::splineit(Age,25,50),
               Age_50_120 = prettyglm::splineit(Age,50,120)) %>%
  dplyr::mutate(Fare_0_250 = prettyglm::splineit(Fare,0,250),
               Fare_250_600 = prettyglm::splineit(Fare,250,600))

# A simple example
survival_model <- stats::glm(Survived ~
                             Pclass +
                             Sex +
                             Age +
                             Fare +
                             Embarked +
                             SibSp +
                             Parch +
                             Cabintype,
                             data = titanic,
                             family = binomial(link = 'logit'))
pretty_coefficients(survival_model)

# A more complicated example with a spline and different importance method
survival_model3 <- stats::glm(Survived ~
                              Pclass +
                              Age_0_25 +
                              Age_25_50 +
                              Age_50_120 +
                              Sex:Fare_0_250 +
                              Sex:Fare_250_600 +
```

```

                                Embarked +
                                SibSp +
                                Parch +
                                Cabintype,
                                data = titanic,
                                family = binomial(link = 'logit'))
pretty_coefficients(survival_model3,
                    relativity_transform = 'exp(estimate)-1',
                    spline_seperator = '_',
                    vimethod = 'permute',
                    target = 'Survived',
                    metric = "roc_auc",
                    event_level = 'second',
                    pred_wrapper = predict.glm,
                    smaller_is_better = FALSE,
                    train = survival_model3$data, # need to supply training data for vip importance
                    reference_class = 0)

```

---

```
pretty_relativities  pretty_relativities
```

---

## Description

Creates a pretty html plot of model relativities including base Levels.

## Usage

```

pretty_relativities(
  feature_to_plot,
  model_object,
  plot_approx_ci = TRUE,
  relativity_transform = "exp(estimate)-1",
  relativity_label = "Relativity",
  ordering = NULL,
  plot_factor_as_numeric = FALSE,
  width = 800,
  height = 500,
  interactionplottype = NULL,
  facatorcolourby = NULL,
  upper_percentile_to_cut = 0.01,
  lower_percentile_to_cut = 0,
  spline_seperator = NULL
)

```

**Arguments**

feature_to_plot	A string of the variable to plot.
model_object	Model object to create coefficient table for. Must be of type: <code>glm</code> , <code>lm</code>
plot_approx_ci	Set to TRUE to include confidence intervals in summary table. Warning, can be computationally expensive.
relativity_transform	String of the function to be applied to the model estimate to calculate the relativity, for example: <code>'exp(estimate)'</code> . Default is for relativity to be <code>'exp(estimate)-1'</code> .
relativity_label	String of label to give to relativity column if you want to change the title to your use case, some users may prefer to refer to this as odds ratio.
ordering	Option to change the ordering of categories on the x axis, only for discrete categories. Default to the ordering of the fitted factor. Other options are: <code>'alphabetical'</code> , <code>'Number of records'</code> , <code>'Average Value'</code>
plot_factor_as_numeric	Set to TRUE to return <code>data.frame</code> instead of creating <code>kable</code> .
width	Width of plot
height	Height of plot
interactionplottype	If plotting the relativity for an interaction variable you can <code>"facet"</code> or <code>"colour"</code> by one of the interaction variables. Defaults to null.
facetorcolourby	If <code>interactionplottype</code> is not Null, then this is the variable in the interaction you want to colour or facet by.
upper_percentile_to_cut	For continuous variables this is what percentile to exclude from the upper end of the distribution. Defaults to 0.01, so the maximum percentile of the variable in the plot will be 0.99. Cutting off some of the distribution can help the views if outlier's are present in the data.
lower_percentile_to_cut	For continuous variables this is what percentile to exclude from the lower end of the distribution. Defaults to 0.01, so the minimum percentile of the variable in the plot will be 0.01. Cutting off some of the distribution can help the views if outlier's are present in the data.
spline_seperator	string of the spline separator. For example <code>AGE_0_25</code> would be <code>"_"</code> .

**Value**

plotly plot of fitted relativities.

**Examples**

```

library(dplyr)
library(prettyglm)
data('titanic')

columns_to_factor <- c('Pclass',
                      'Sex',
                      'Cabin',
                      'Embarked',
                      'Cabintype',
                      'Survived')
meanage <- base::mean(titanic$Age, na.rm=TRUE)

titanic <- titanic %>%
  dplyr::mutate_at(columns_to_factor, list(~factor(.))) %>%
  dplyr::mutate(Age =base::ifelse(is.na(Age)==TRUE,meanage,Age)) %>%
  dplyr::mutate(Age_0_25 = prettyglm::splineit(Age,0,25),
               Age_25_50 = prettyglm::splineit(Age,25,50),
               Age_50_120 = prettyglm::splineit(Age,50,120)) %>%
  dplyr::mutate(Fare_0_250 = prettyglm::splineit(Fare,0,250),
               Fare_250_600 = prettyglm::splineit(Fare,250,600))

survival_model3 <- stats::glm(Survived ~
                             Pclass:Embarked +
                             Age_0_25 +
                             Age_25_50 +
                             Age_50_120 +
                             Sex:Fare_0_250 +
                             Sex:Fare_250_600 +
                             SibSp +
                             Parch +
                             Cabintype,
                             data = titanic,
                             family = binomial(link = 'logit'))

# categorical factor
pretty_relativities(feature_to_plot = 'Cabintype',
                    model_object = survival_model3)

# continuous factor
pretty_relativities(feature_to_plot = 'Parch',
                    model_object = survival_model3)

# splined continuous factor
pretty_relativities(feature_to_plot = 'Age',
                    model_object = survival_model3,
                    spline_seperator = '_',
                    upper_percentile_to_cut = 0.01,
                    lower_percentile_to_cut = 0.01)

# factor factor interaction
pretty_relativities(feature_to_plot = 'Pclass:Embarked',

```

```

        model_object = survival_model3,
        interactionplottype = 'colour',
        facetcoulorby = 'Pclass')

# Continuous spline and categorical by colour
pretty_relativities(feature_to_plot = 'Sex:Fare',
                    model_object = survival_model3,
                    spline_seperator = '_')

# Continuous spline and categorical by facet
pretty_relativities(feature_to_plot = 'Sex:Fare',
                    model_object = survival_model3,
                    spline_seperator = '_',
                    interactionplottype = 'facet')

```

---

splineit

*splineit*


---

## Description

Splines a continuous variable

## Usage

```
splineit(var, min, max)
```

## Arguments

var	Continuous vector to spline.
min	Min of spline.
max	Max of spline.

## Value

Splined Column

## Examples

```

library(dplyr)
library(prettyglm)
data('titanic')

columns_to_factor <- c('Pclass',
                      'Sex',
                      'Cabin',
                      'Embarked',
                      'Cabintype',
                      'Survived')

meanage <- base::mean(titanic$Age, na.rm=TRUE)

```

```
titanic <- titanic %>%
  dplyr::mutate_at(columns_to_factor, list(~factor(.))) %>%
  dplyr::mutate(Age =base::ifelse(is.na(Age)==TRUE,meanage,Age)) %>%
  dplyr::mutate(Age_0_25 = prettyglm::splineit(Age,0,25),
               Age_25_50 = prettyglm::splineit(Age,25,50),
               Age_50_120 = prettyglm::splineit(Age,50,120)) %>%
  dplyr::mutate(Fare_0_250 = prettyglm::splineit(Fare,0,250),
               Fare_250_600 = prettyglm::splineit(Fare,250,600))
```

---

titanic

*Titanic Data*


---

### Description

The sinking of the Titanic is one of the most infamous shipwrecks in history. On April 15, 1912, during her maiden voyage, the widely considered “unsinkable” RMS Titanic sank after colliding with an iceberg. Unfortunately, there weren’t enough lifeboats for everyone onboard, resulting in the death of 1502 out of 2224 passengers and crew. While there was some element of luck involved in surviving, it seems some groups of people were more likely to survive than others. In this challenge, we ask you to build a predictive model that answers the question: “what sorts of people were more likely to survive?” using passenger data (ie name, age, gender, socio-economic class, etc).

### Usage

```
data(titanic)
```

### Format

An object of class “data.frame”

**survival** Survival

**pclass** Ticket class

**sex** Sex

**Age** Age in years

**sibsp** number of siblings / spouses

**parch** number of parents / children

**ticket** Ticket number

**fare** Passenger fare

**cabin** Cabin Number

**cabin type** Type of cabin

**embarked** Port of Embarkation

**References**

This data set sourced from <https://www.kaggle.com/c/titanic/data?select=train.csv>

**Examples**

```
data(titanic)
head(titanic)
```

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